



# Last lecture (7)

- Particle motion in magnetosphere
- Aurora

# Today's lecture (8)

- Aurora on other planets
- How to measure currents in space
- Magnetospheric dynamics



# Today

<u>Activity</u>	<u>Date</u>	<u>Time</u>	<u>Room</u>	<u>Subject</u>	<u>Litterature</u>
L1	2/9	10-12	Q33	Course description, Introduction, The Sun 1, Plasma physics 1	<b>CGF</b> Ch 1, 5, (p 110-113)
L2	4/9	10-12	Q21	The Sun 2, Plasma physics 2	<b>CGF</b> Ch 5 (p 114-121), 6.3
L3	8/9	13-15	Q36	Solar wind, The ionosphere and atmosphere 1, Plasma physics 3	<b>CGF</b> Ch 6.1, 2.1-2.6, 3.1-3.2, 3.5, <b>LL</b> Ch III, Extra material
T1	10/9	10-12	Q33	Mini-group work 1	
L4	15/9	13-15	Q31	The ionosphere 2, Plasma physics 4	<b>CGF</b> Ch 3.4, 3.7, 3.8
T2	17/9	10-12	Q33	Mini-group work 2	
L5	19/9	15-17	Q31	The Earth's magnetosphere 1, Plasma physics 5	<b>CGF</b> 4.1-4.3, <b>LL</b> Ch I, II, IV.A
L6	23/9	8-10	Q31	The Earth's magnetosphere 2, Other magnetospheres	<b>CGF</b> Ch 4.6-4.9, <b>LL</b> Ch V.
T3	24/9	14-16	Q21	Mini-group work 3	
L7	29/9	11-13	Q36	<b>Aurora, Measurement methods in space plasmas and data analysis 1</b>	<b>CGF</b> Ch 4.5, 10, <b>LL</b> Ch VI, Extra material
T4	1/10	15-17	Q31	Mini-group work 4	
L8	2/10	15-17	Q34	<b>Space weather and geomagnetic storms</b>	<b>CGF</b> Ch 4.4, <b>LL</b> Ch IV.B-C, VII.A-C
L9	8/10	13-15	Q36	Interstellar and intergalactic plasma, Cosmic radiation, Swedish and international space physics research.	<b>CGF</b> Ch 7-9
T5	9/10	15-17	Q31	Mini-group work 5	
L10	13/10	15-17	Q33	Guest lecture (preliminary): Swedish astronaut Christer Fuglesang	
T6	16/10	10-12	Q36	Round-up	
Written examination	30/10	8-13	M33, M37, M38		

# Mini-groupwork 4

a)

$$\rho_{SW} v_{SW}^2 = \left[ \frac{\mu_0 a}{4\pi r^3} \right]^2 / 2\mu_0 \Rightarrow$$

$$r = \left( \frac{\mu_0 a}{4\pi} \right)^{1/3} \left( 2\mu_0 \rho_{SW} v_{SW}^2 \right)^{-1/6}$$

Assuming the solar wind consists of protons

$$\rho_{SW} = n_{e,SW} m_p = 1.7 \cdot 10^{-22} \text{ kg m}^{-3}$$

Thus

$$r = 2.7 \cdot 10^9 \text{ m} \approx 38 R_J$$

# Mini-groupwork 4

b)

$$\rho_{SW} v_{SW}^2 = \left[ \frac{\mu_0 a}{4\pi} \frac{1}{r^3} \right]^2 / 2\mu_0 + 2n_e k_B T \Rightarrow$$

$$\rho_{SW} v_{SW}^2 = \left[ \frac{\mu_0 a}{4\pi} \frac{1}{r^3} \right]^2 / 2\mu_0 + 2n_{e0} \left( \frac{R_J}{r} \right)^3 k_B T$$

Substitute  $x = 1/r^3$ . This gives you an equation on the form

$$ax^2 + bx + c = 0$$

with

$$a = \left[ \frac{\mu_0 a}{4\pi} \right]^2 / 2\mu_0 = 1.02 \cdot 10^{46}$$

$$b = 2n_{e0} R_J^3 k_B T = 3.6 \times 10^{18}$$

$$c = -\rho_{SW} v_{SW}^2 = -2.7 \cdot 10^{-11}$$

$$\begin{aligned} x &= \frac{-b}{2a} \pm \sqrt{\frac{b^2}{4a^2} - \frac{c}{a}} = -1.8 \cdot 10^{-28} + \sqrt{3.24 \cdot 10^{-56} + 2.635 \cdot 10^{-57}} = \\ &= -1.8 \cdot 10^{-28} + 1.87 \cdot 10^{-28} = 7.18 \cdot 10^{-30} \end{aligned}$$

From this you get  $r \approx 73 R_J$

# Magnetic mirror

$mv^2/2$  constant (energy conservation) →

$$\frac{\sin^2 \alpha}{B} = \text{konst}$$

particle turns when  $\alpha = 90^\circ$  →

$$B_{\text{turn}} = B / \sin^2 \alpha$$

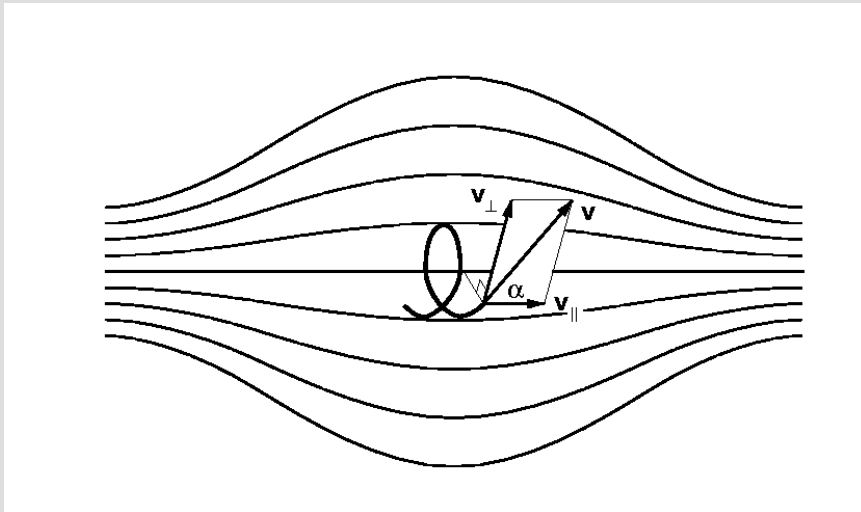
If maximal B-field is  $B_{\text{max}}$  a particle with pitch angle  $\alpha$  can only be turned around if

$$B_{\text{turn}} = B / \sin^2 \alpha \leq B_{\text{max}} \rightarrow$$

$$\alpha > \alpha_{lc} = \arcsin \sqrt{B / B_{\text{max}}}$$

Particles in  
loss cone :

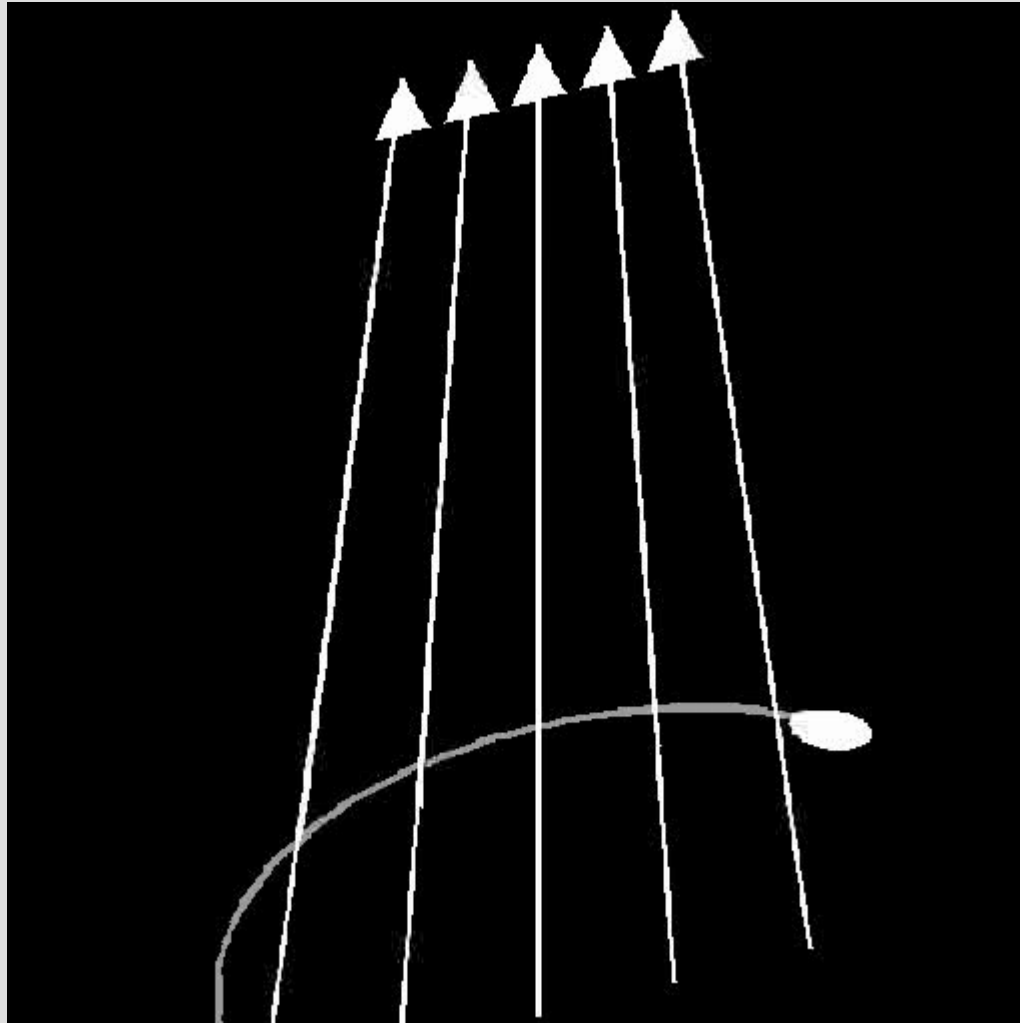
$$\alpha < \alpha_{lc}$$



The magnetic moment  $\mu$  is an *adiabatic invariant*.

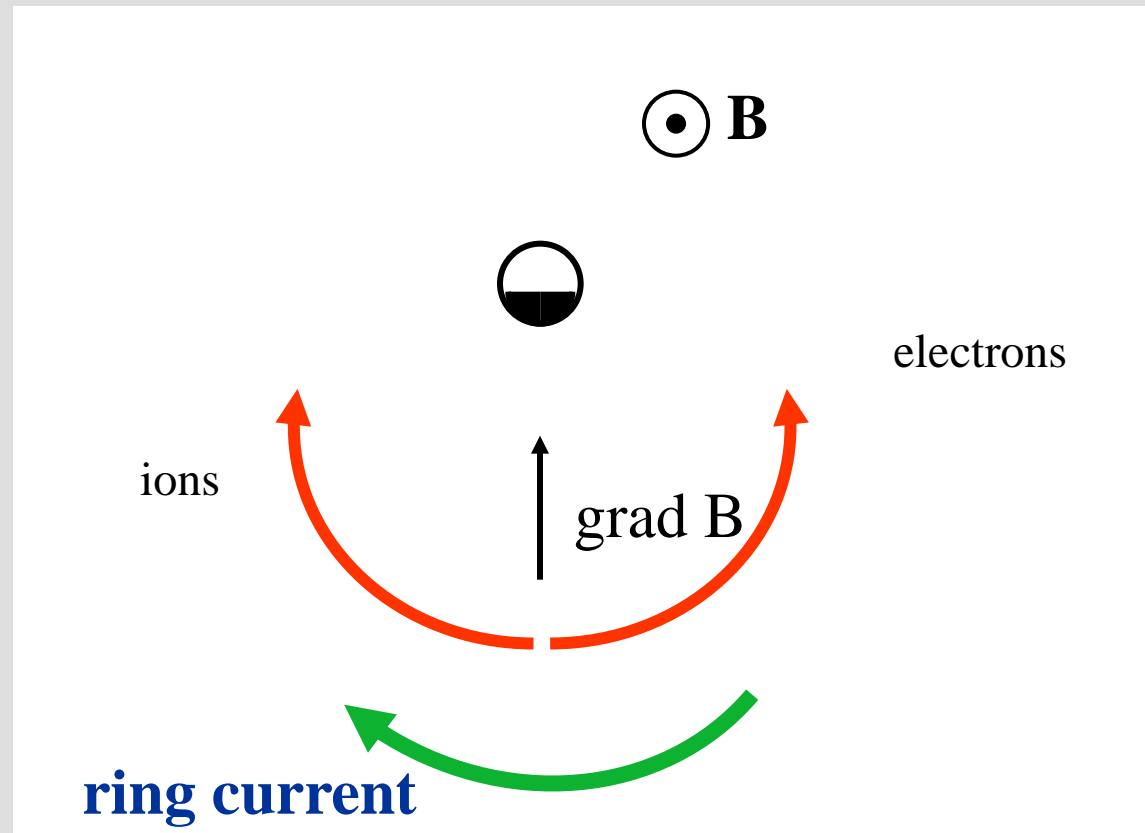
$$\mu = \frac{mv_{\perp}^2}{2B} = \frac{mv^2 \sin^2 \alpha}{2B}$$

# Magnetic mirror

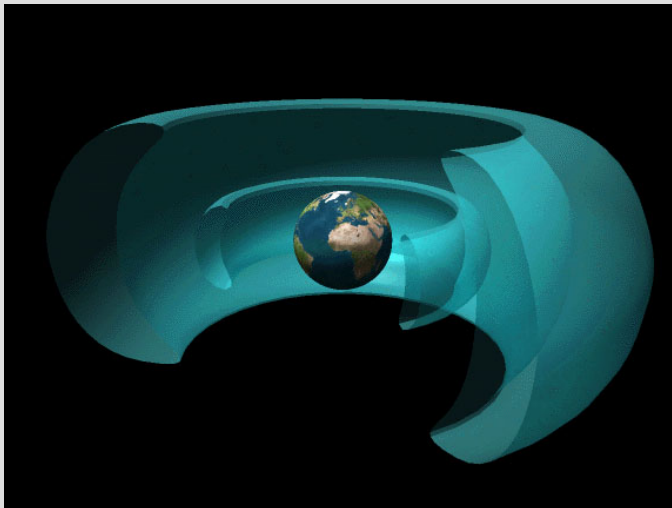
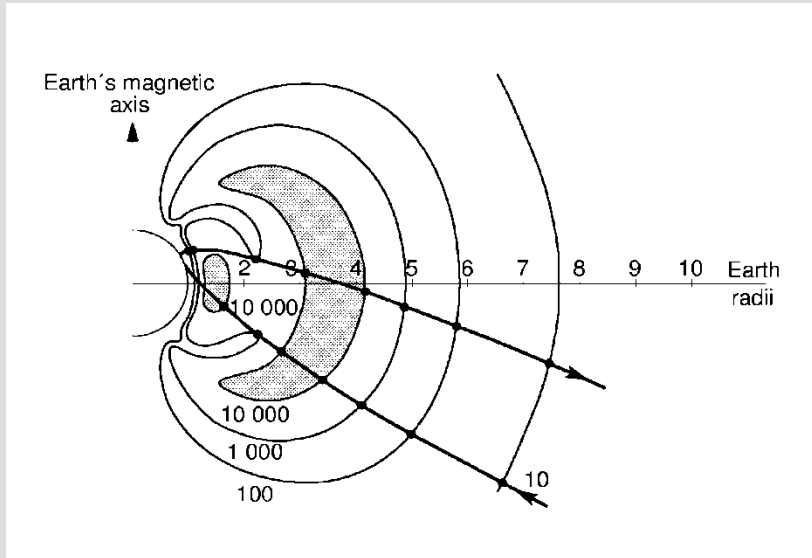


# Ring current and particle motion

$$\mathbf{u} = -\frac{\mu \nabla B \times \mathbf{B}}{qB^2}$$



# Radiation belts



## I. Van Allen belts

- Discovered in the 50s , Explorer 1
- Inner belt contains protons with energies of  $\sim 30$  MeV
- Outer belt (Explorer IV, Pioneer III): electrons,  $W > 1.5$  MeV



# CRAND (Cosmic Ray Albedo Neutron Decay)

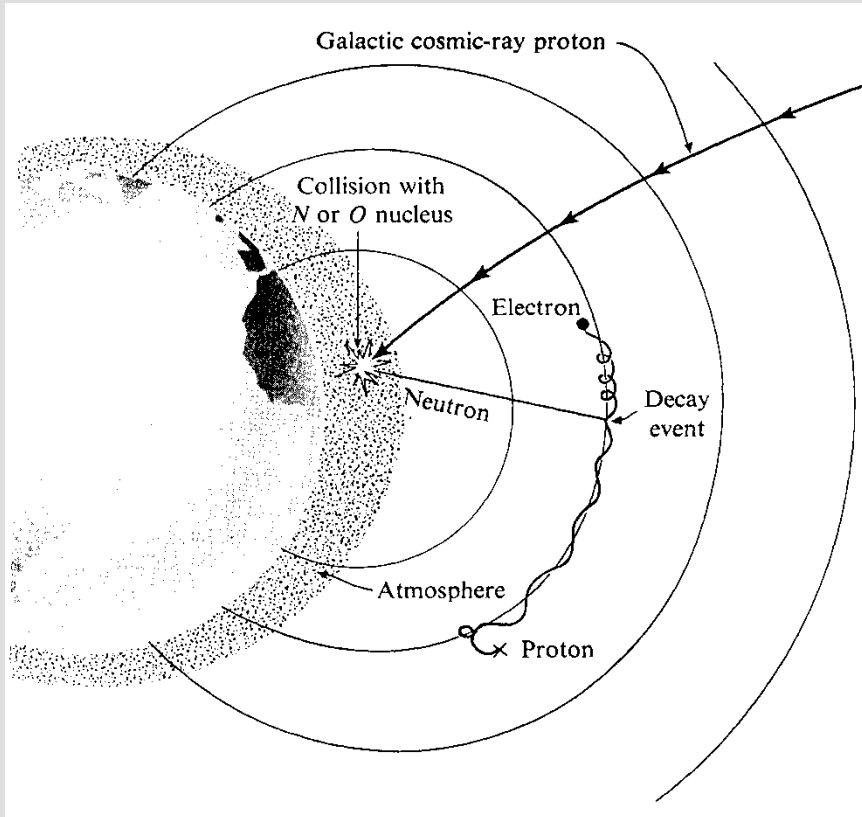


Figure 8. An illustration of the CRAND process for populating the inner radiation belts [Hess, 1968].

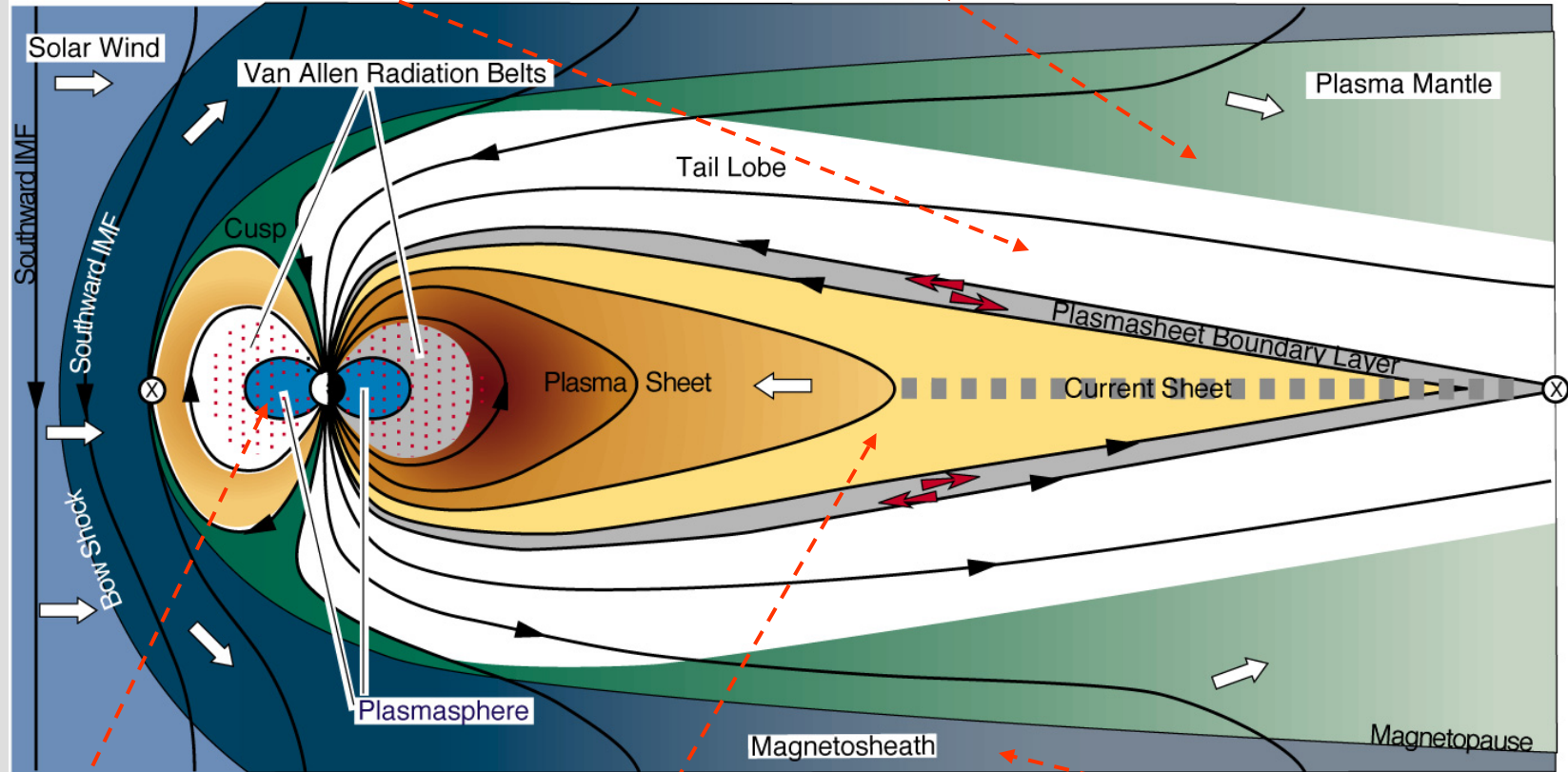
Collisions between cosmic ray particles and the Earth create new particles. Among these are neutrons, that are not affected by the magnetic field. They decay, soon after they happen to be in the radiation belts. The resulting protons and electrons are trapped in the radiation belts.

This contribution to the radiation belts are called the ***neutron albedo***.

# Magnetospheric structure

polar plumes = tail lobe  
 $n_e \sim 0,01 \text{ cm}^{-3}$ ,  $T_e \sim 10^6 \text{ K}$

plasma mantle  
 $n_e \sim 0,1-1 \text{ cm}^{-3}$ ,  $T_e \sim 10^6 \text{ K}$



plasmasphere:  
 $n_e \sim 10-100 \text{ cm}^{-3}$ ,  $T_e \sim 1000 \text{ K}$

plasma sheet:  
 $n_e \sim 1 \text{ cm}^{-3}$ ,  $T_e \sim 10^7 \text{ K}$

magnetosheath:  
 $n_e \sim 5 \text{ cm}^{-3}$ ,  $T_e \sim 10^6 \text{ K}$

# Planetary magnetospheres

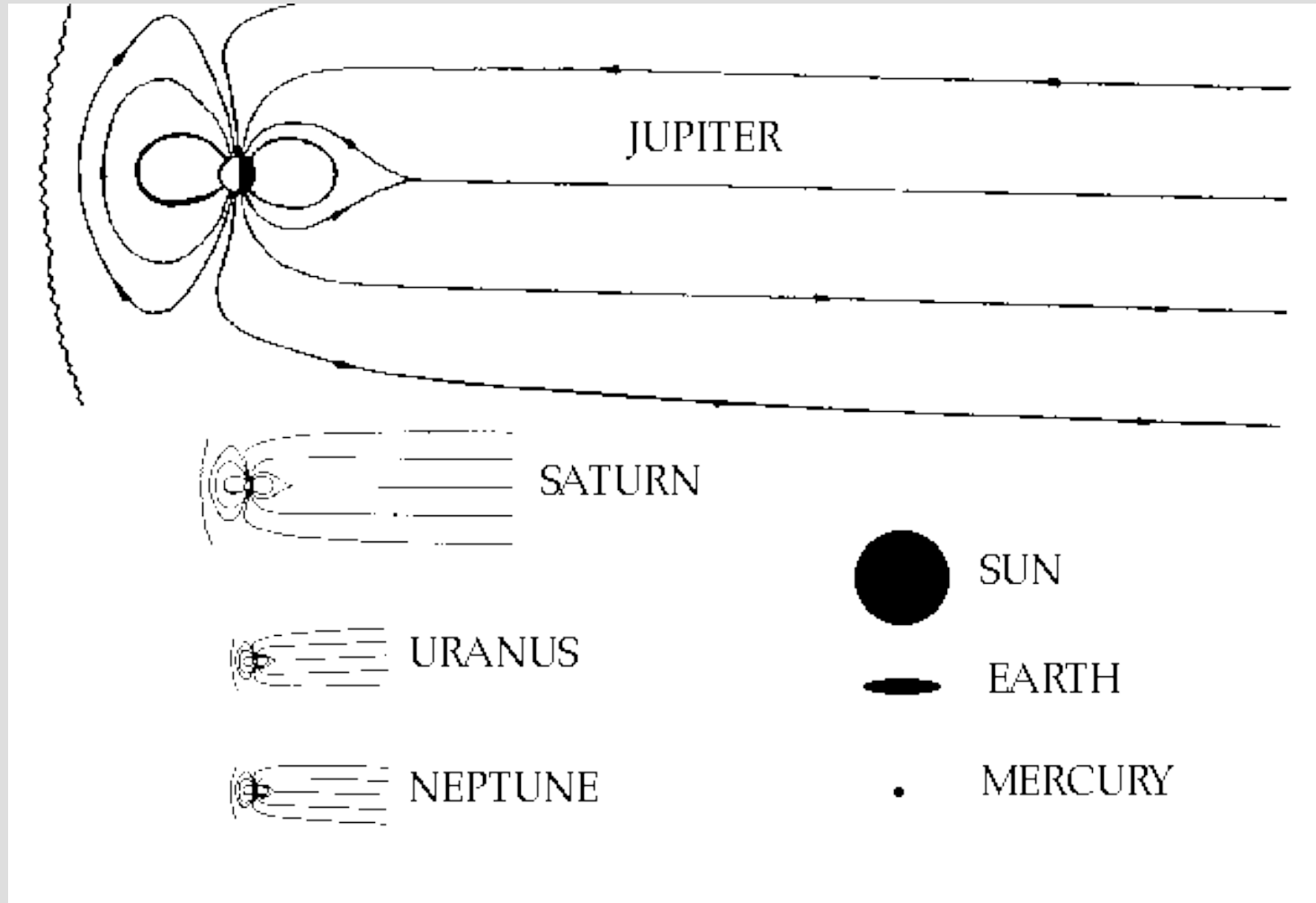
	Radius Earth radii	Spin period (days)	Equatorial field strength ( $\mu\text{T}$ )	Magnetic axis direction relative to spin axis	Polarity relative to Earth's	Typical magnetopause distance (planetary radii)
Mercury	0.38	58.6	0.35	$10^\circ$	Same	1.1
Venus	0.95	243	< 0.03	-	-	1.1
Earth	1.0	1	31	$11.5^\circ$	Same	10
Mars	0.53	1.02	0.065	-	Opposite	?
Jupiter	11.18	0.41	410	$10^\circ$	Opposite	60-100
Saturn	9.42	0.44	40	$<1^\circ$	Opposite	20-25
Uranus	3.84	0.72	23	$60^\circ$	Opposite	18-25
Neptune	3.93	0.74	20-150 <sup>*)</sup>	$47^\circ$	Opposite	26 <sup>**)</sup>

\*) The magnetic field differs greatly from a dipole field. The numbers represent maximum and minimum strength at the planetary surface

\*\*\*) Based on single passage

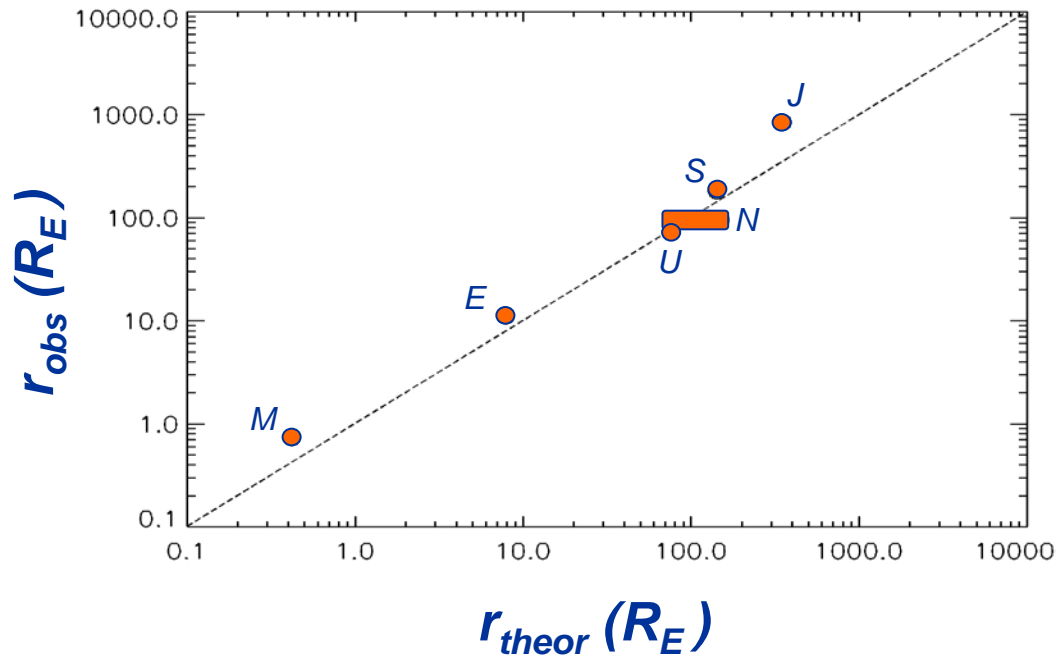
Very weak magnetic fields

# Relative size of the magnetospheres



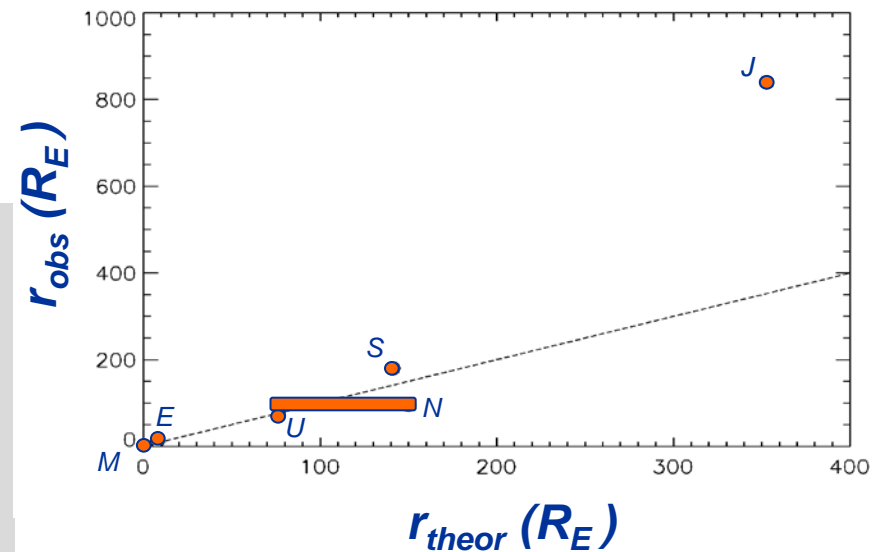
# Comparative magnetospheres

## Observed vs. theoretical standoff-distance



$$r_{theor} = \left( \frac{\mu_0 a}{4\pi} \right)^{1/3} \left( 2\mu_0 \rho_{SW} v_{SW}^2 \right)^{-1/6}$$

- Model reasonably valid over three orders of magnitude
- Size of Jupiter's (and maybe Saturn's) magnetosphere underestimated



# The aurora



# The aurora



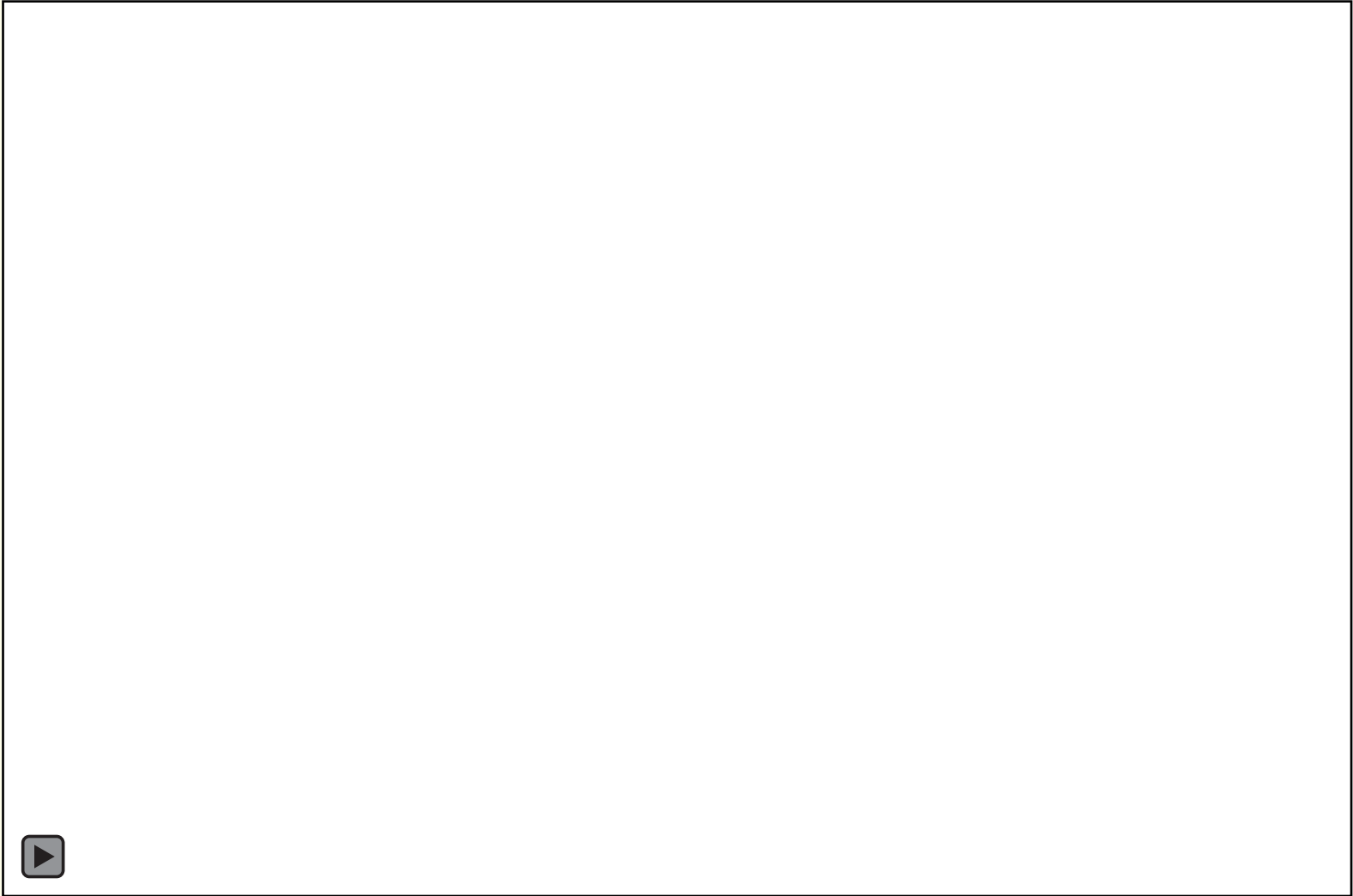
# The aurora



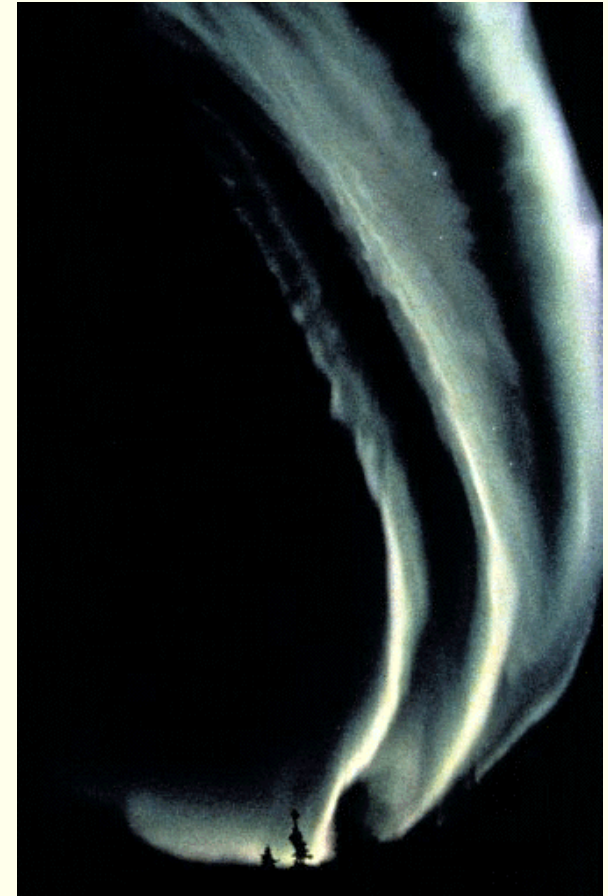




# The aurora



# Homogenous auroral arcs



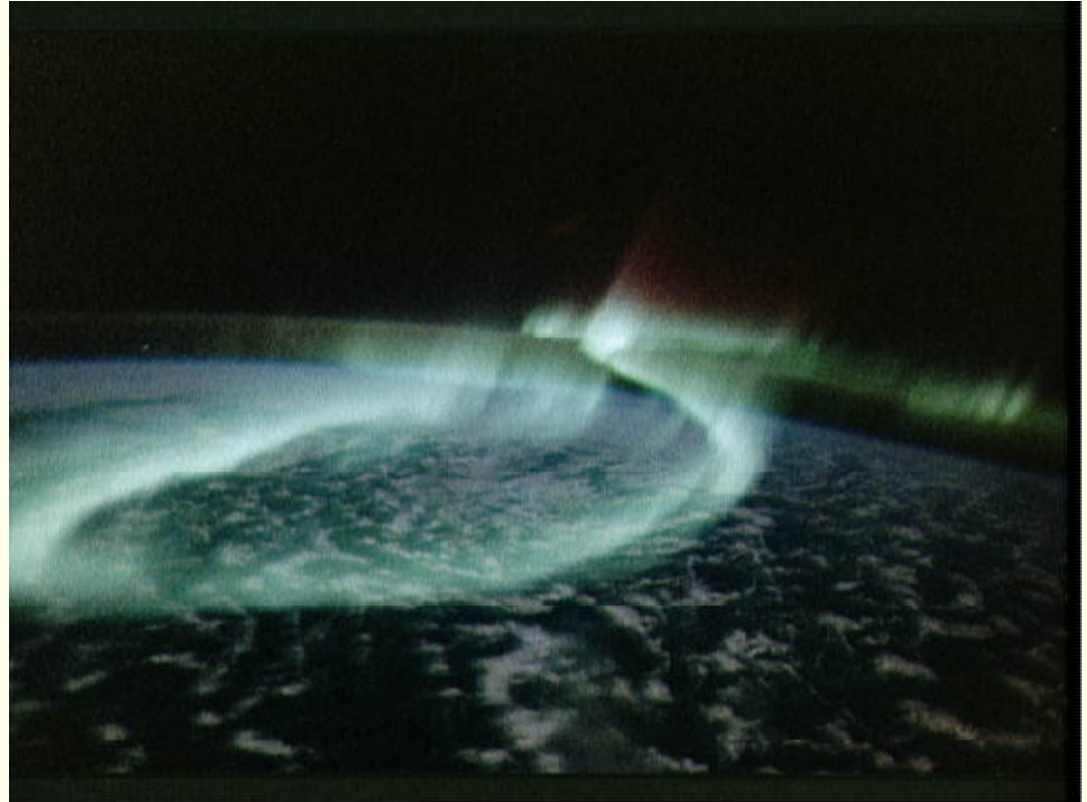
# Rays, curtains

Rays are formed in the direction of the local magnetic field.



Drapes develop from homogenous arcs, often when they increase in intensity.

# Auroral spirals

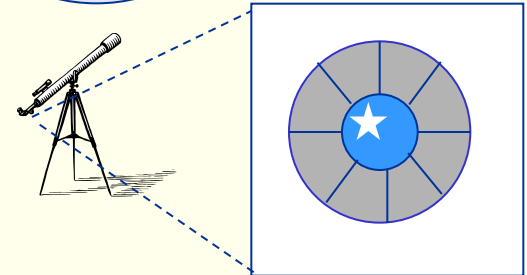
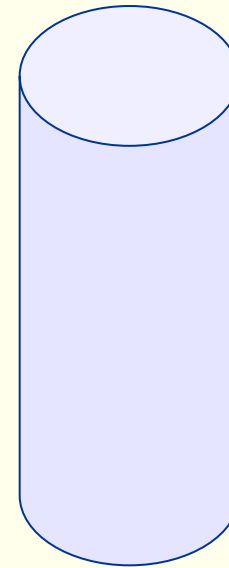


Develop when arcs become unstable

# Auroral corona



Geometric effect of perspective when you look towards magnetic zenith.  
Compare the figure.



# Aurora - altitude

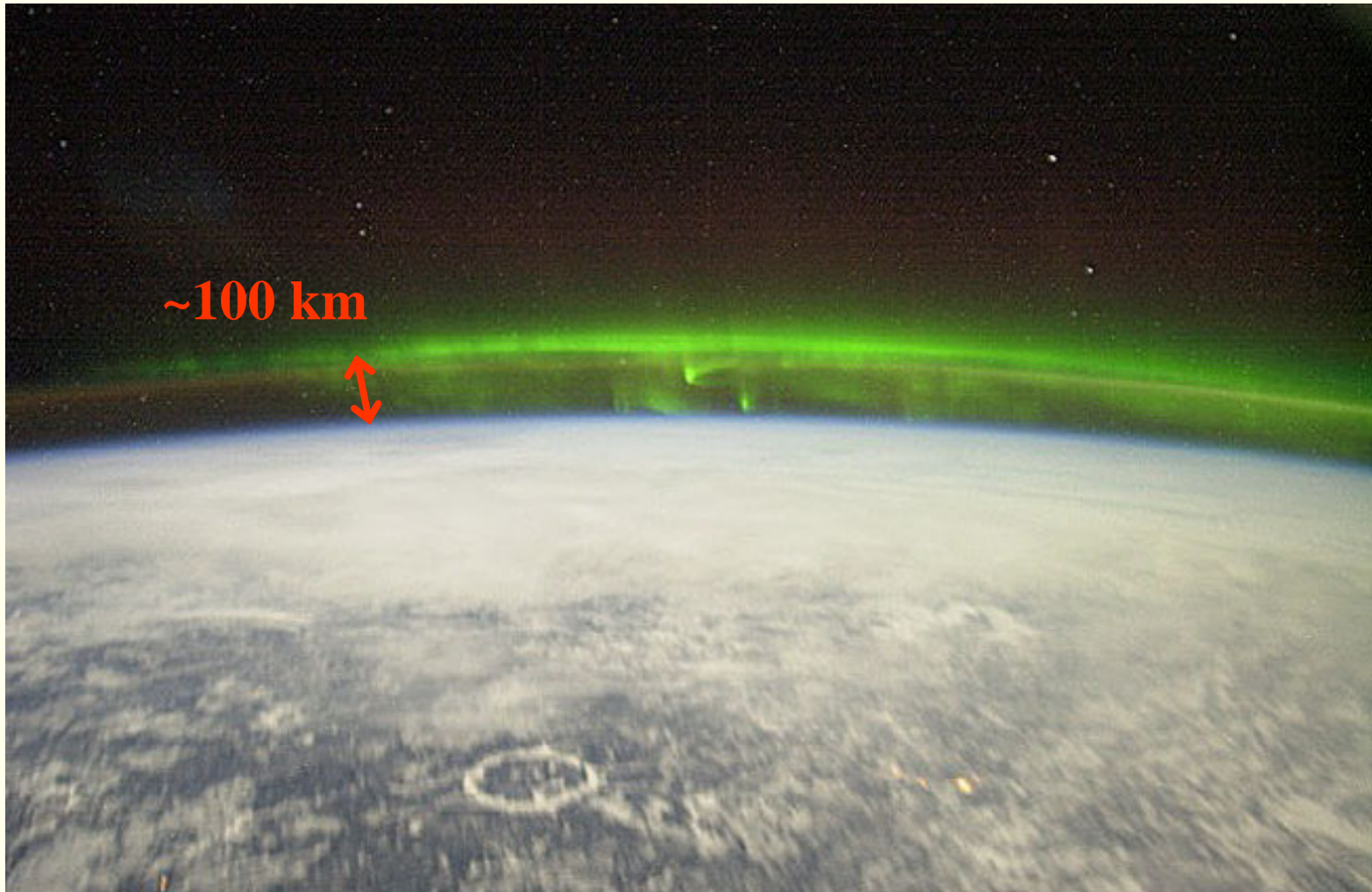


Foto from International Space Station

# Early notions



Woodcut from Böhmen 1570.



Anders Celsius documented that compass needles were strongly affected during auroral activity in 1733.



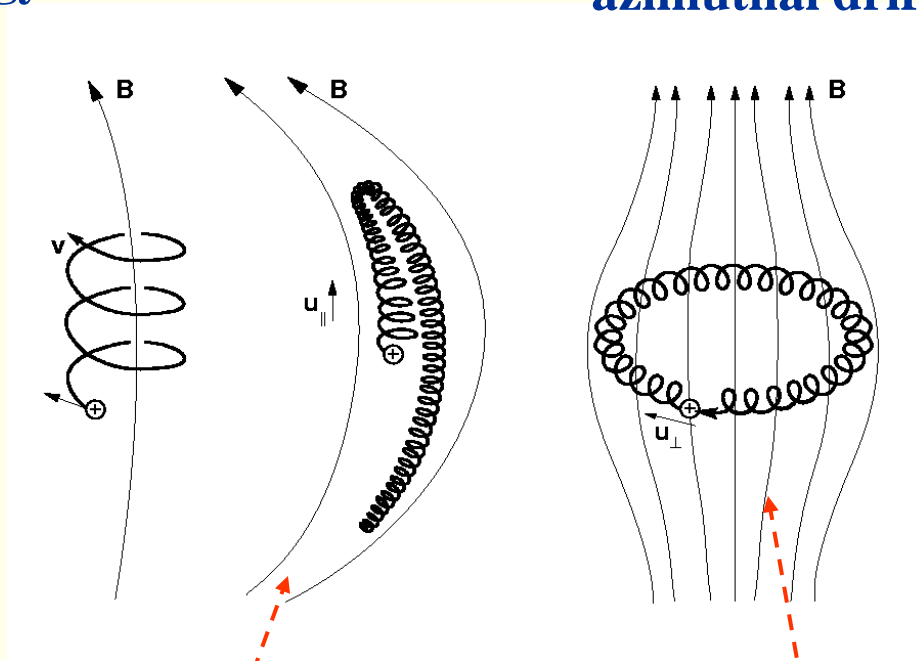
# What causes the aurora?



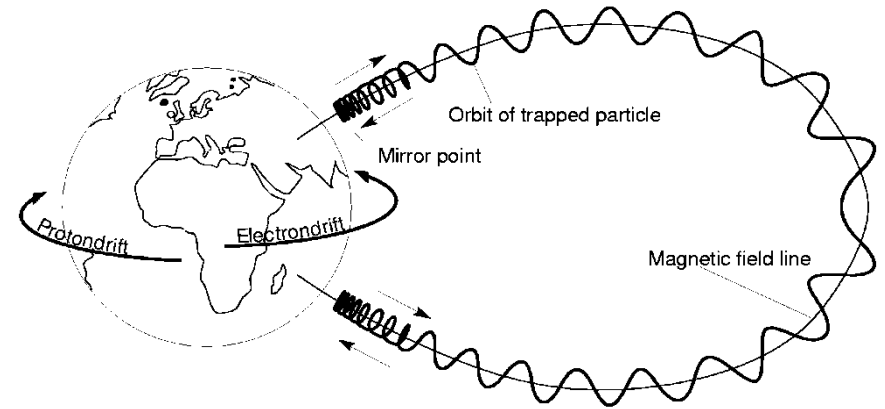
# Particle motion in geomagnetic field

## longitudinal oscillation

### gyration



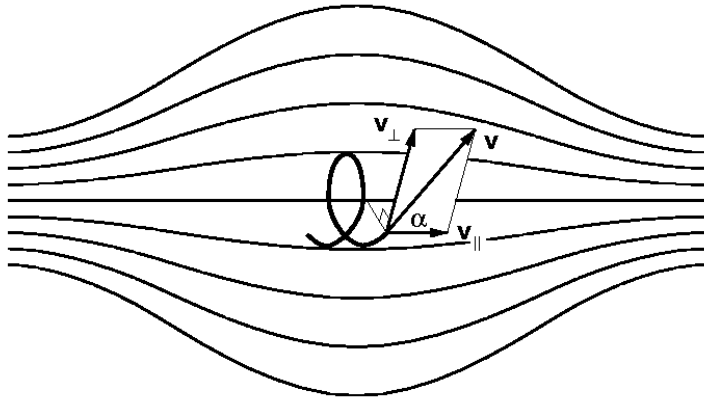
### azimuthal drift



Magnetic mirror

grad B drift

# Magnetic mirror



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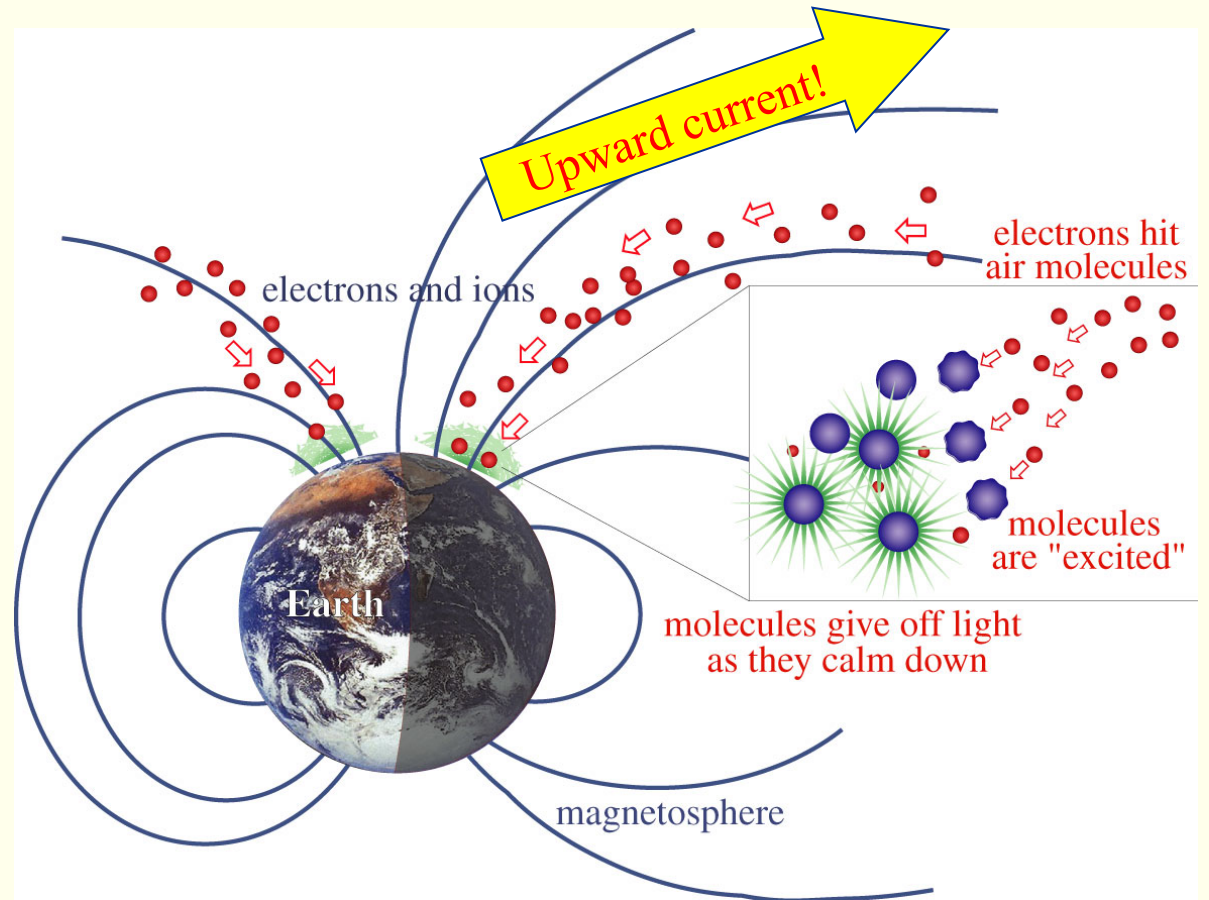
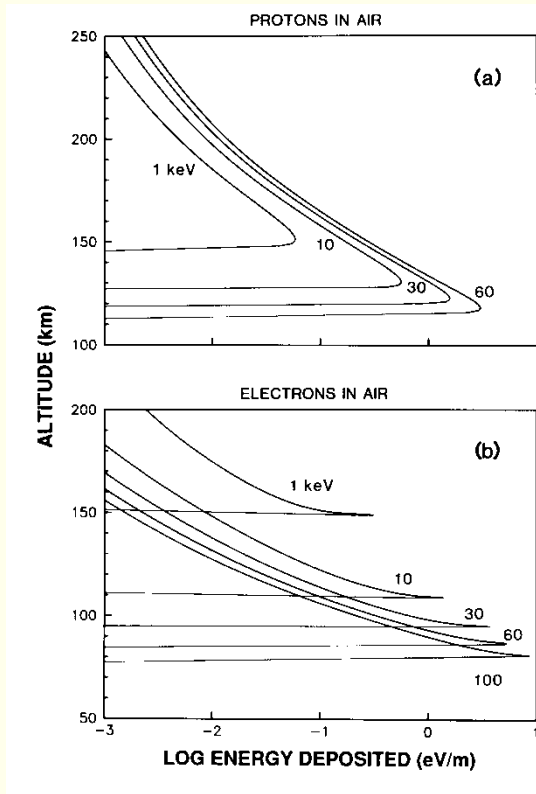
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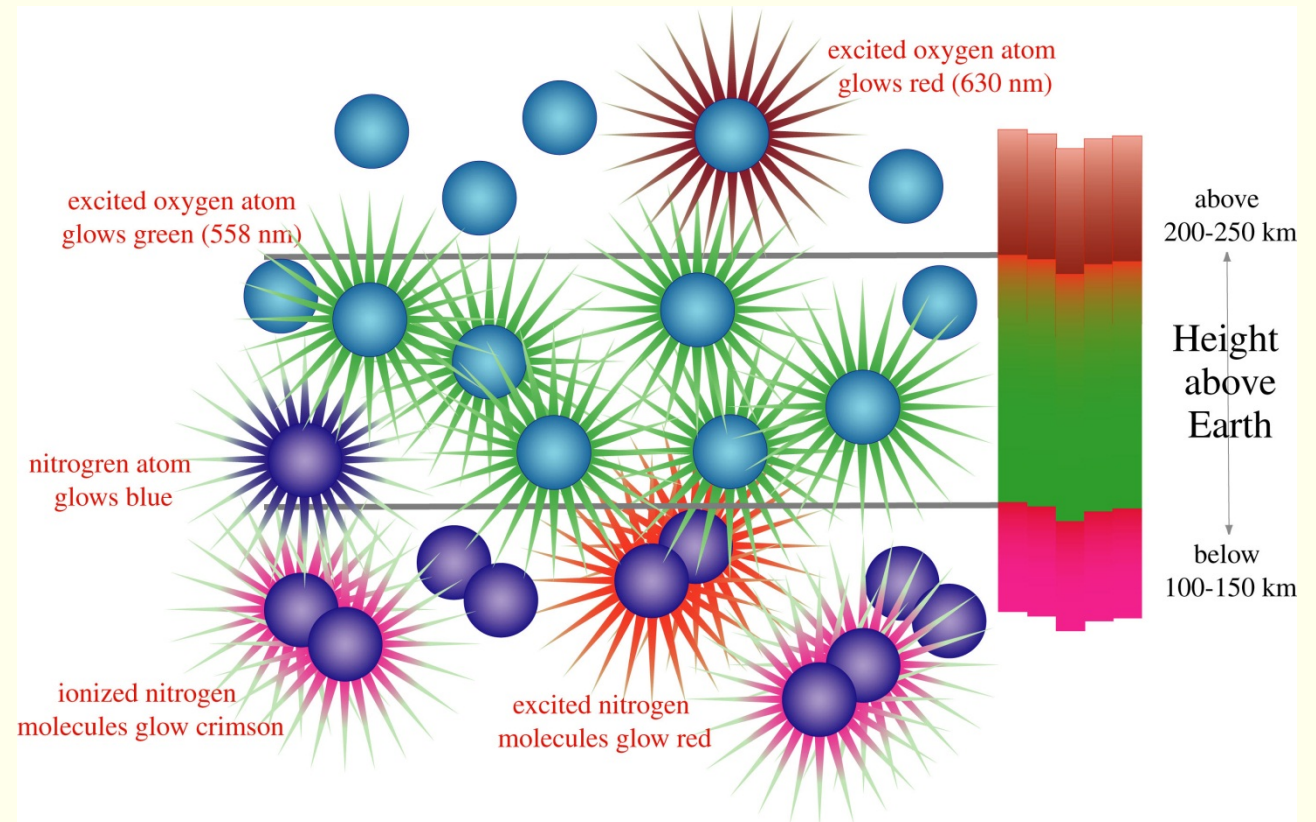
Particles in  
*loss cone* :

$$\alpha < \alpha_{lc}$$

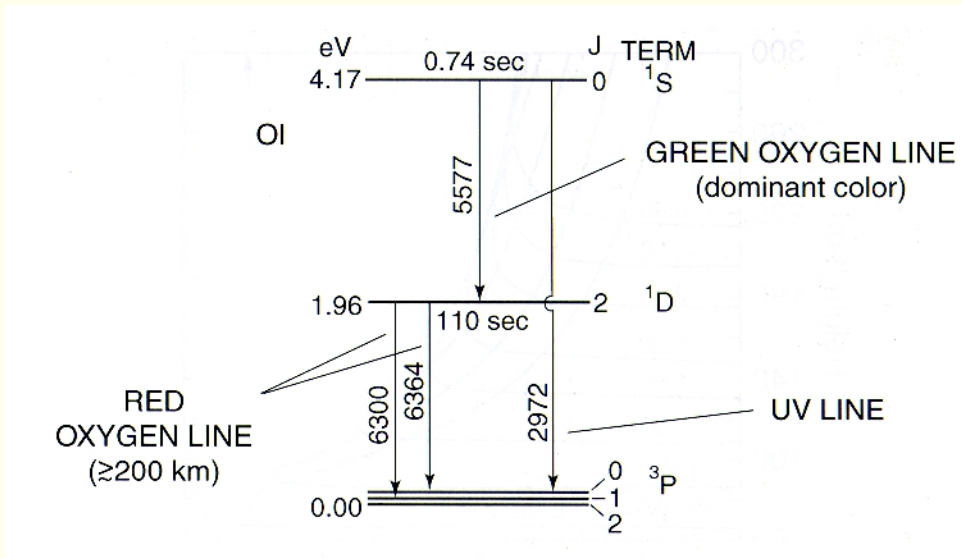
# Collisions - emissions



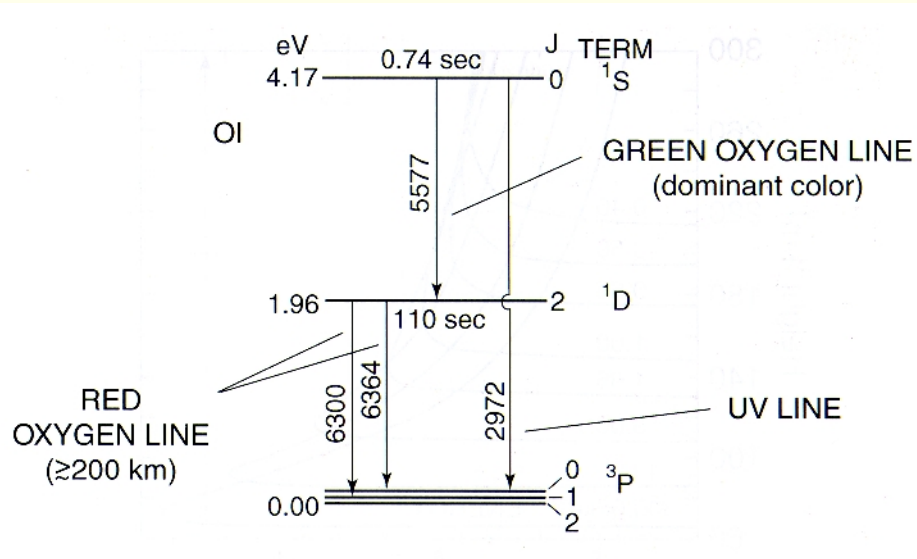
# Emissions



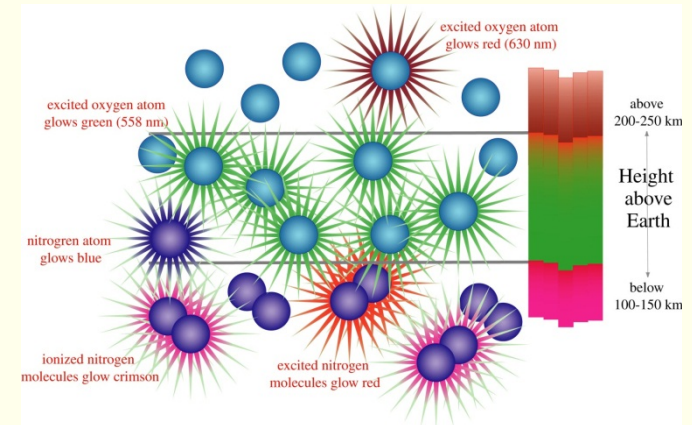
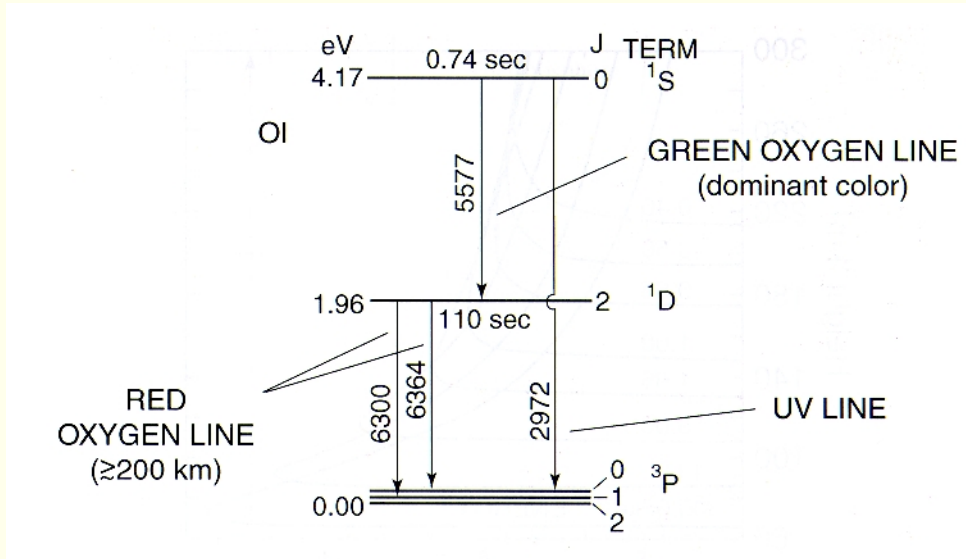
# Oxygen emissions



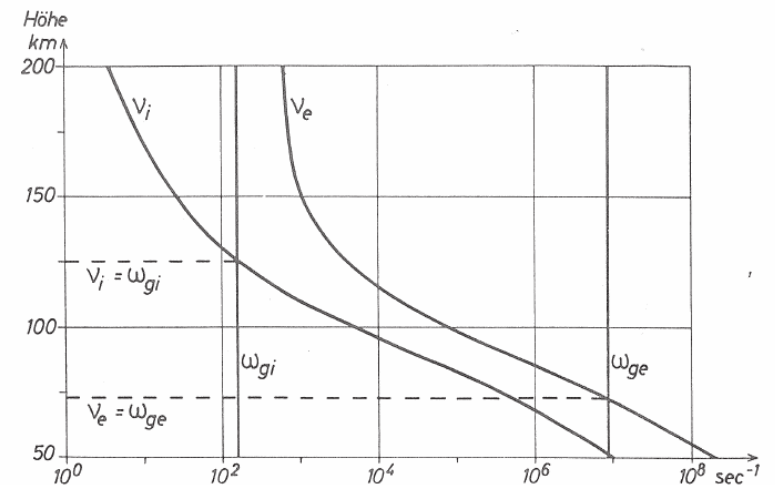
# Why is there no red emissions at lower altitude?



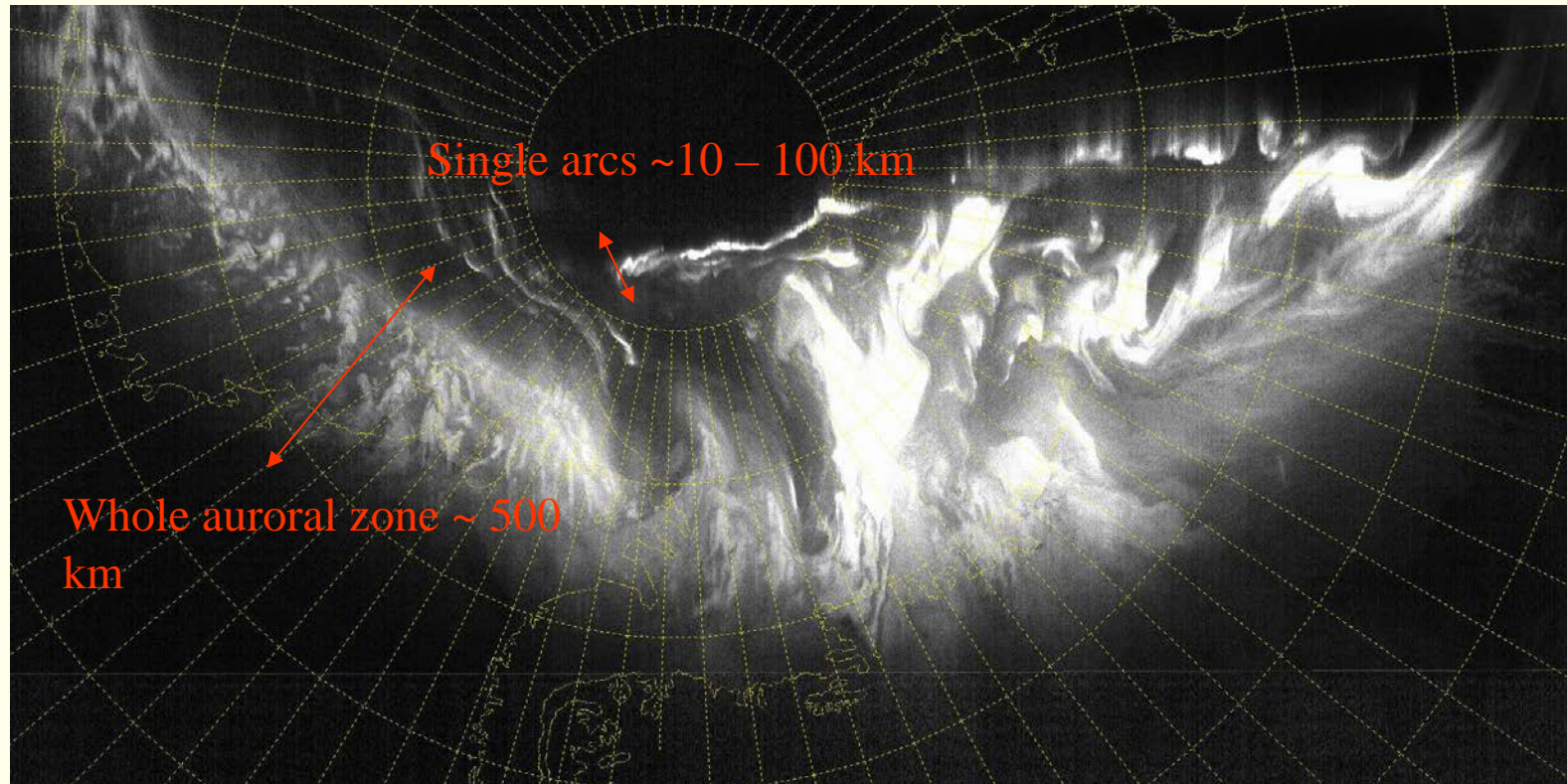
# Oxygen emissions



The red emission line is suppressed by collisions at lower altitudes due to its long transition time. (When an excited atom collides with another atom, it is de-excited without any emission.)



# Larger scales

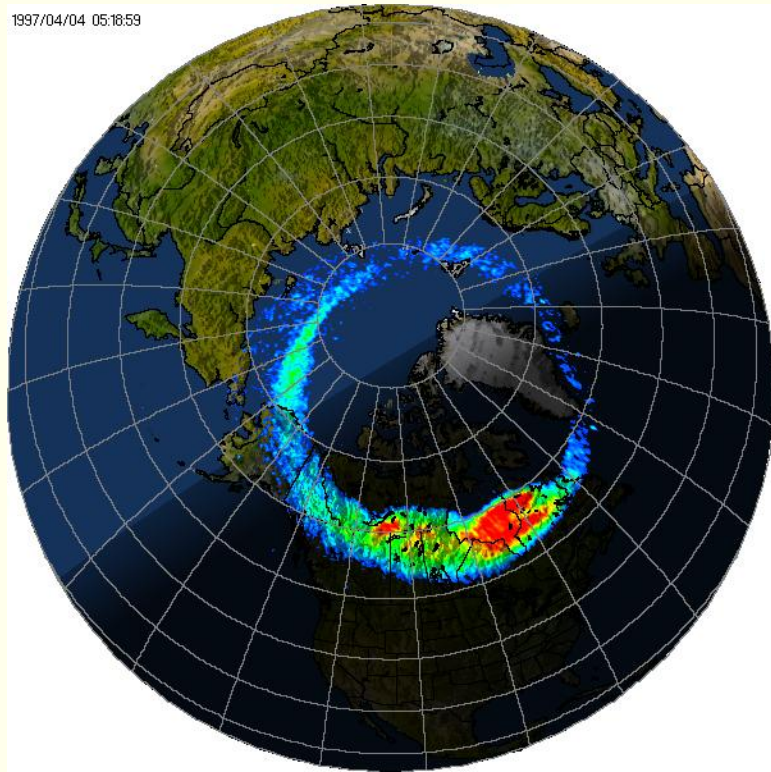


*Foto från DMSP-satelliten*

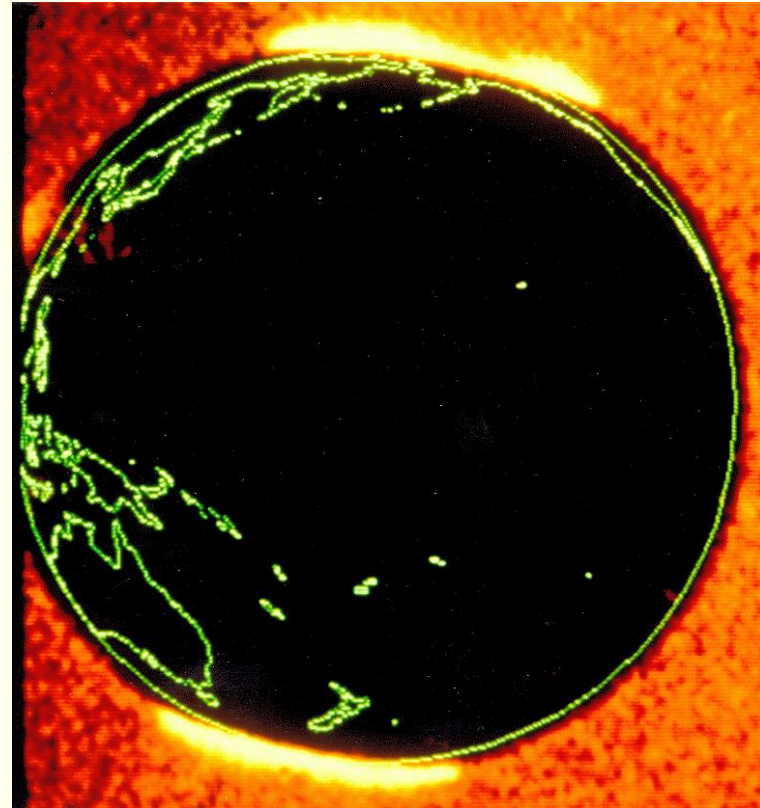


# Auroral ovals

1997/04/04 05:18:59



Polar

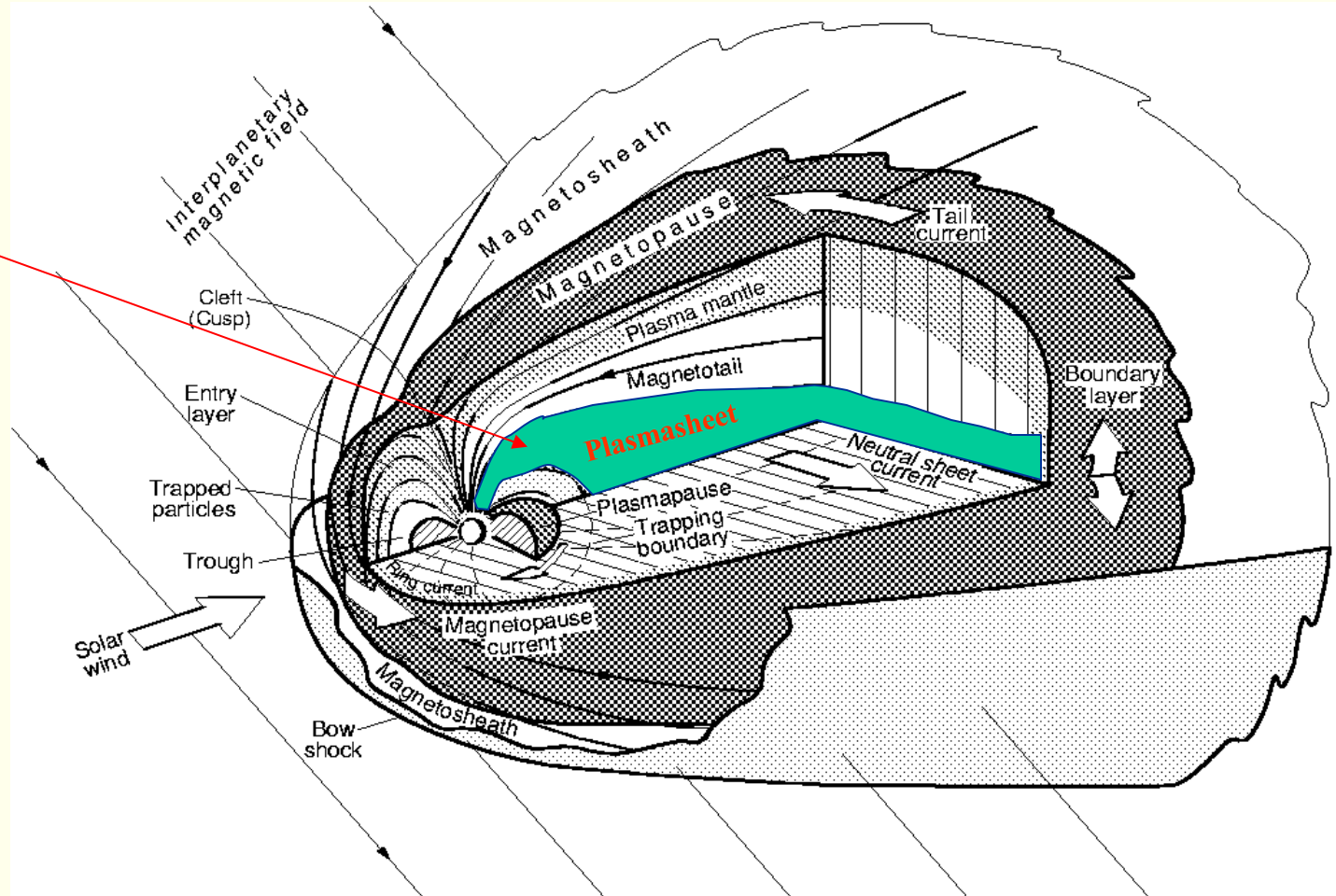


Dynamics Explorer

# The auroral oval is the projection of the plasmasheet onto the atmosphere

## Mystery!

The particles in the plasmasheet do not have high enough energy to create aurora visible to the eye.



# Magnetic mirror

$mv^2/2$  constant (energy conservation) →

$$\frac{\sin^2 \alpha}{B} = \text{konst}$$

particle turns when  $\alpha = 90^\circ$  →

$$B_{\text{turn}} = B / \sin^2 \alpha$$

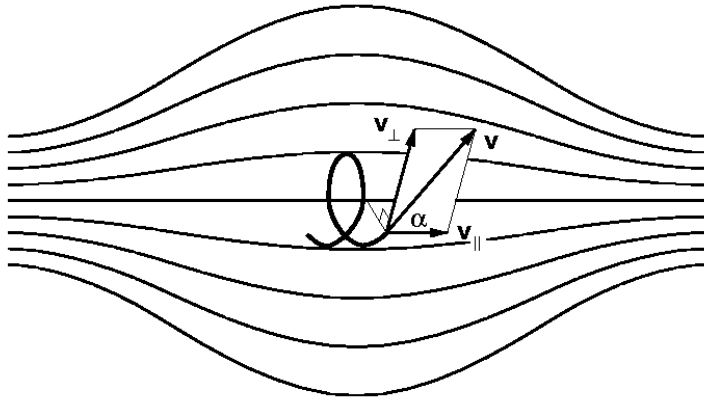
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Particles in  
*loss cone* :

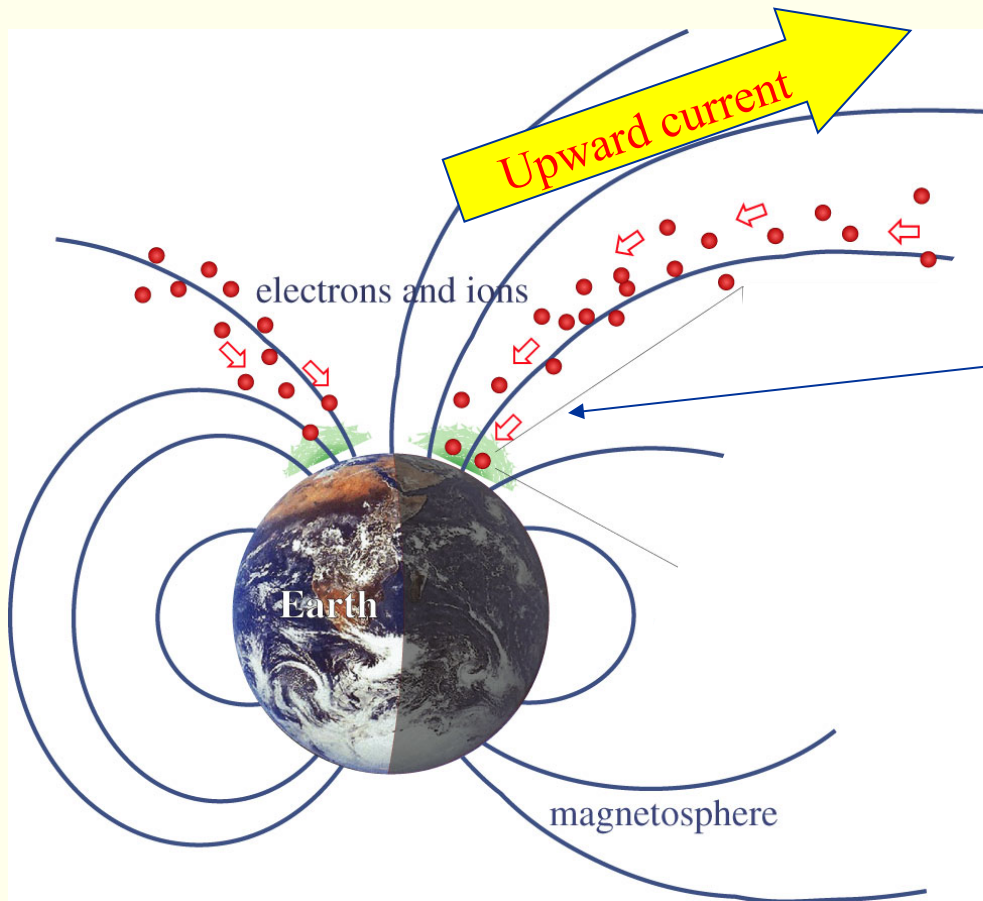
$$\alpha < \alpha_{fl}$$



The magnetic moment  $\mu$  is an *adiabatic invariant*.

$$\mu = \frac{mv_{\perp}^2}{2B} = \frac{mv^2 \sin^2 \alpha}{2B}$$

# Why particle acceleration?



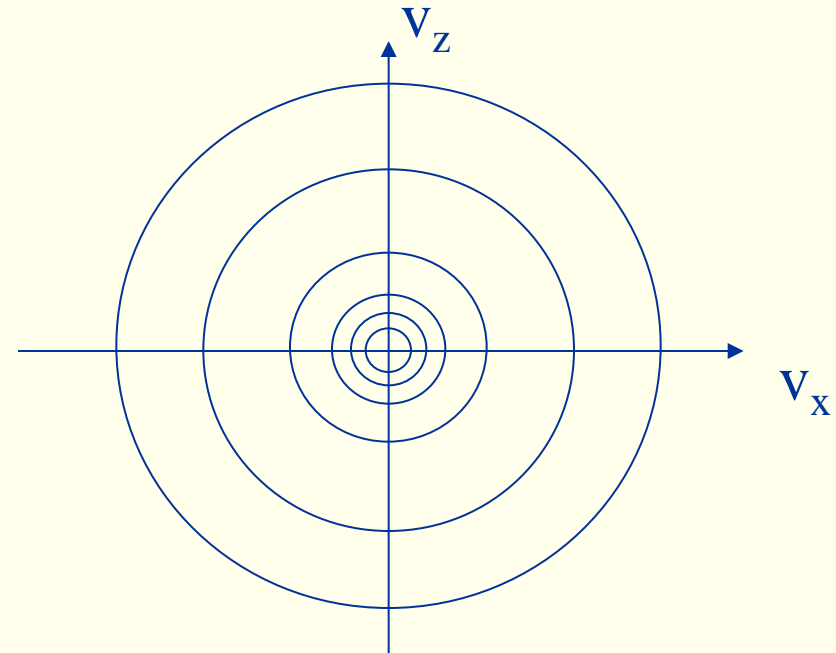
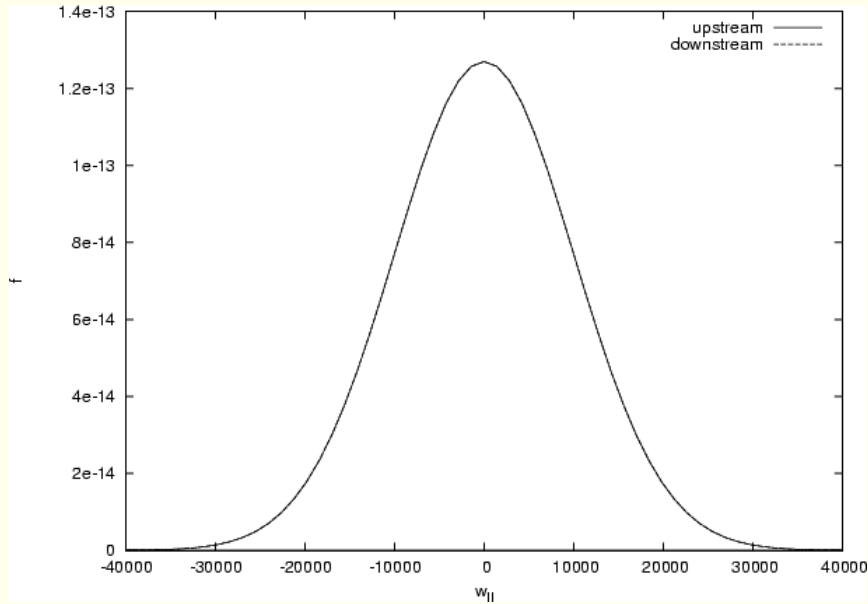
- The magnetosphere often seems to act as a current generator.
- The lower down you are on the field line, the more particles have been reflected by the magnetic mirror.
- At low altitudes there are not enough electrons to carry the current.

# Why particle acceleration?



- Electrons are accelerated downwards by upward E-field.
- This increases the pitch-angle of the electrons, and more electrons can reach the ionosphere, where the current can be closed.

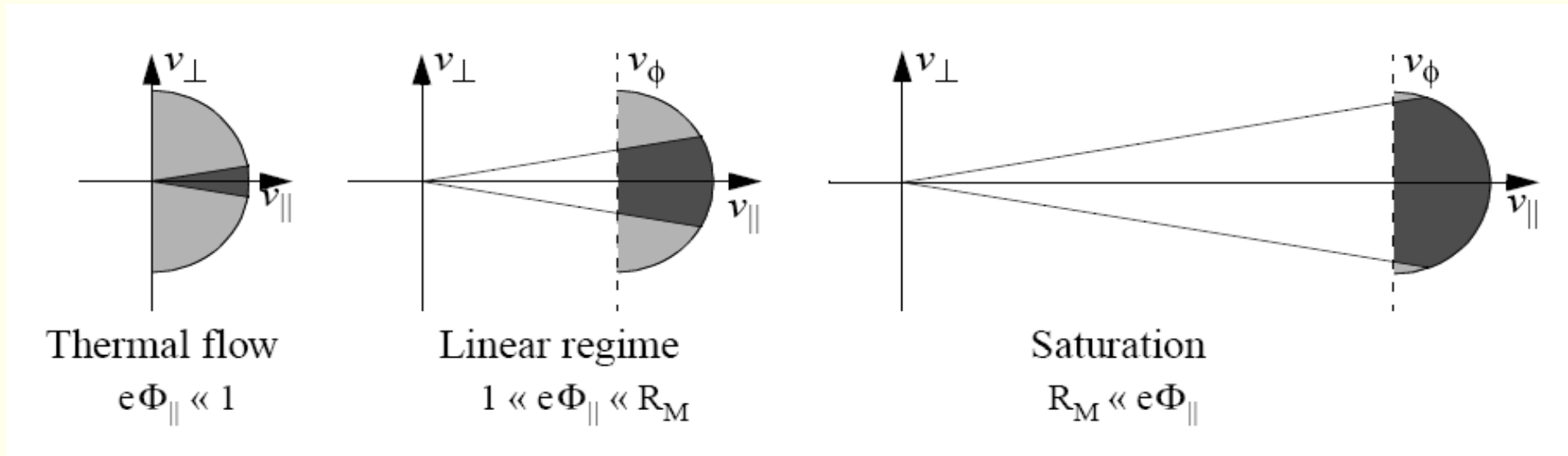
# Distribution function



Example:  
Maxwellian  
distribution

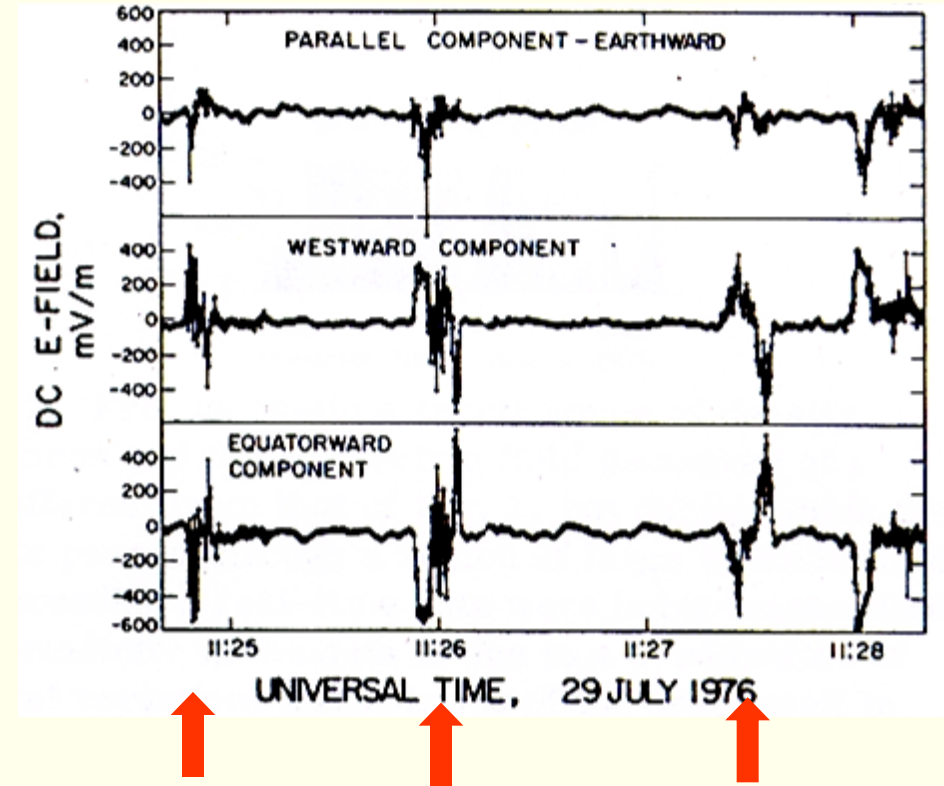
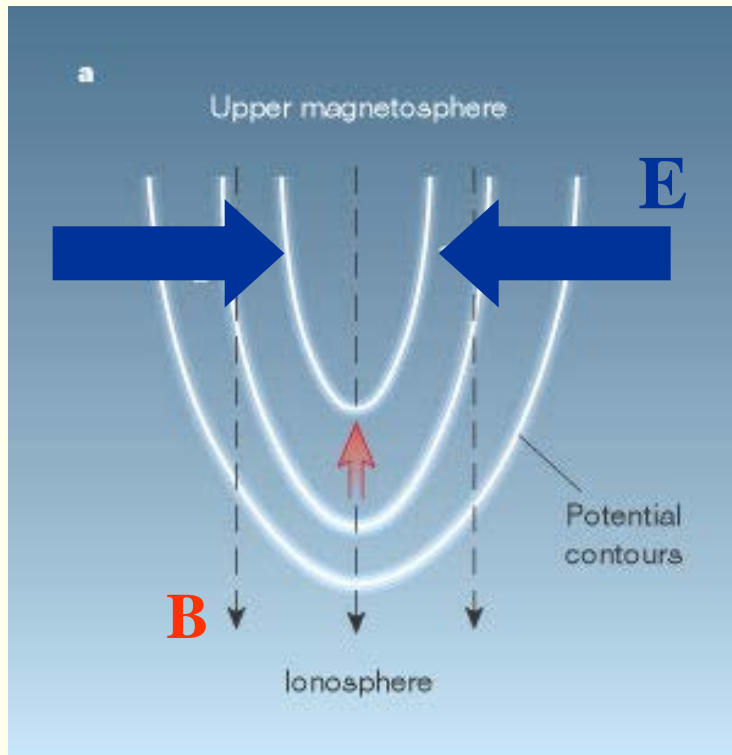
$$f = \frac{n}{\sqrt{(2\pi RT)^3}} \exp\left(-\frac{m(v_x^2 + v_y^2 + v_z^2)}{2kT}\right)$$

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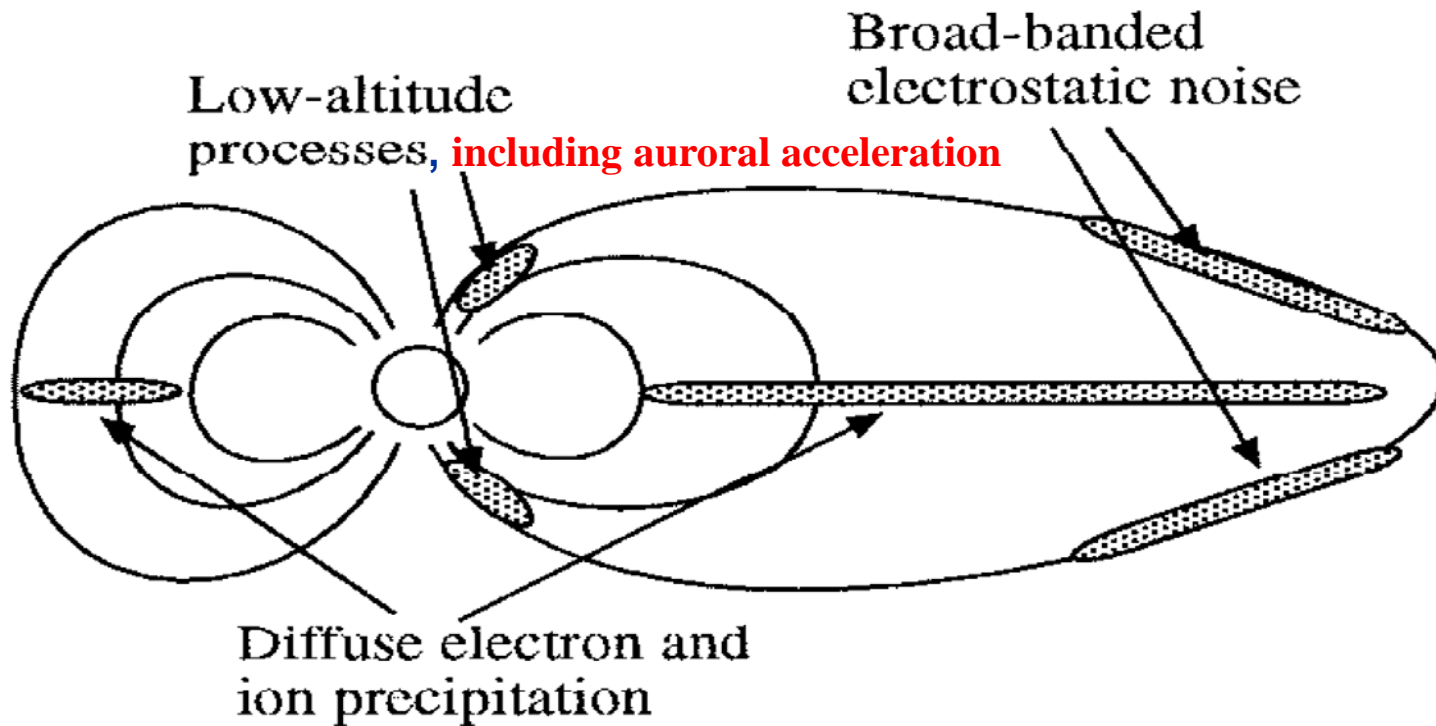
# Satellite signatures of U potential



Measurements made by the ISEE satellite (Mozer et al., 1977)

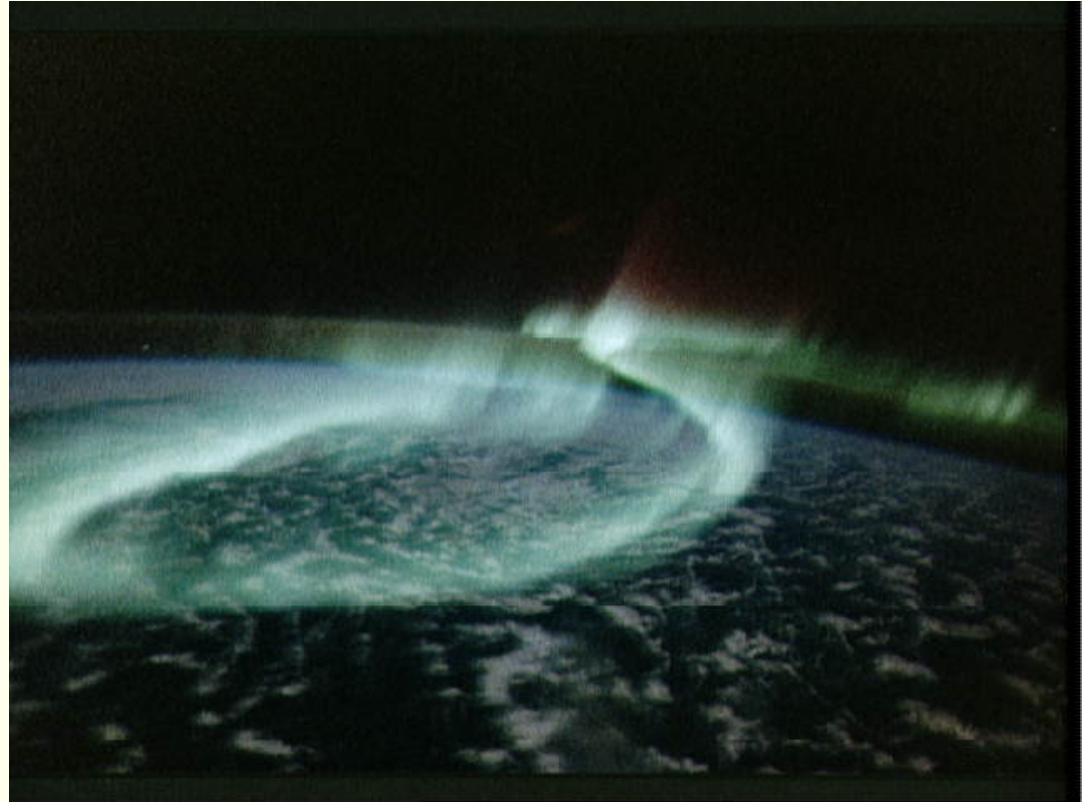


# Acceleration regions



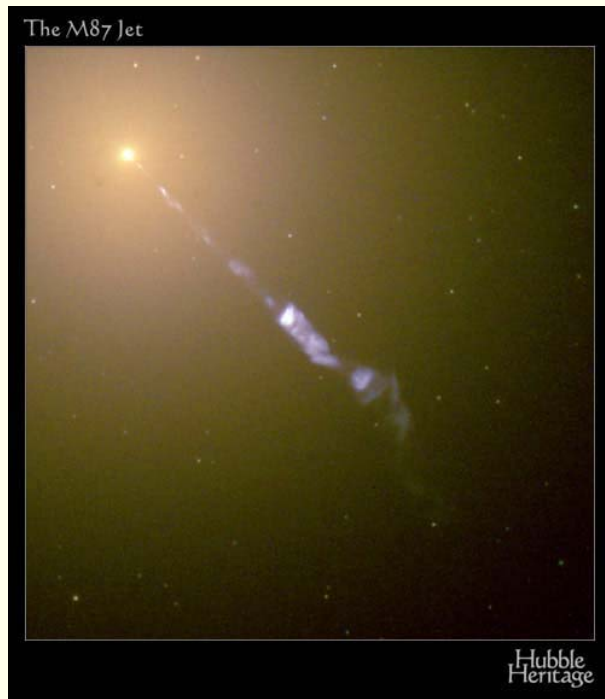
Auroral acceleration region typically situated at altitude of 1-3  $R_E$

# Auroral spirals

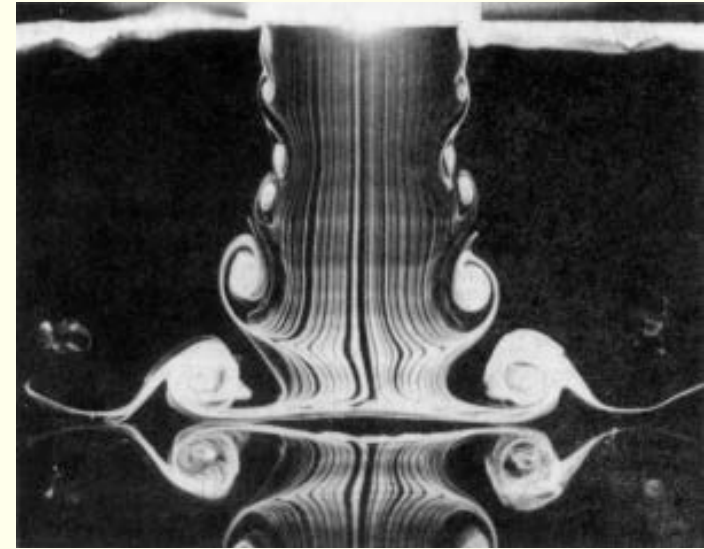


Develop when arcs become unstable

# Kelvin-Helmholtz- instability – a general phenomenon



Extragalactic jet (M87)



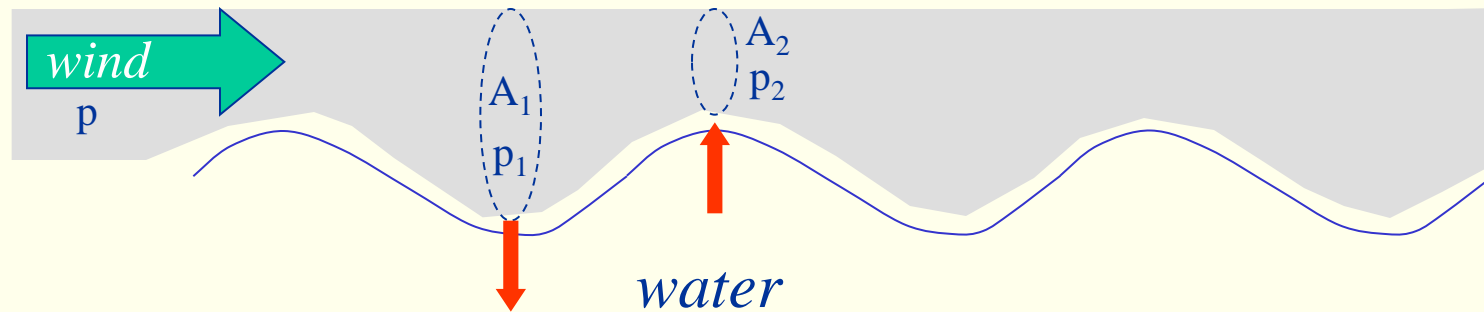
Aero- and fluid dynamics



Cluds

# Kelvin-Helmholtz instability

## Example: water waves



Continuity equation:

$$A_1 v_1 = A_2 v_2$$

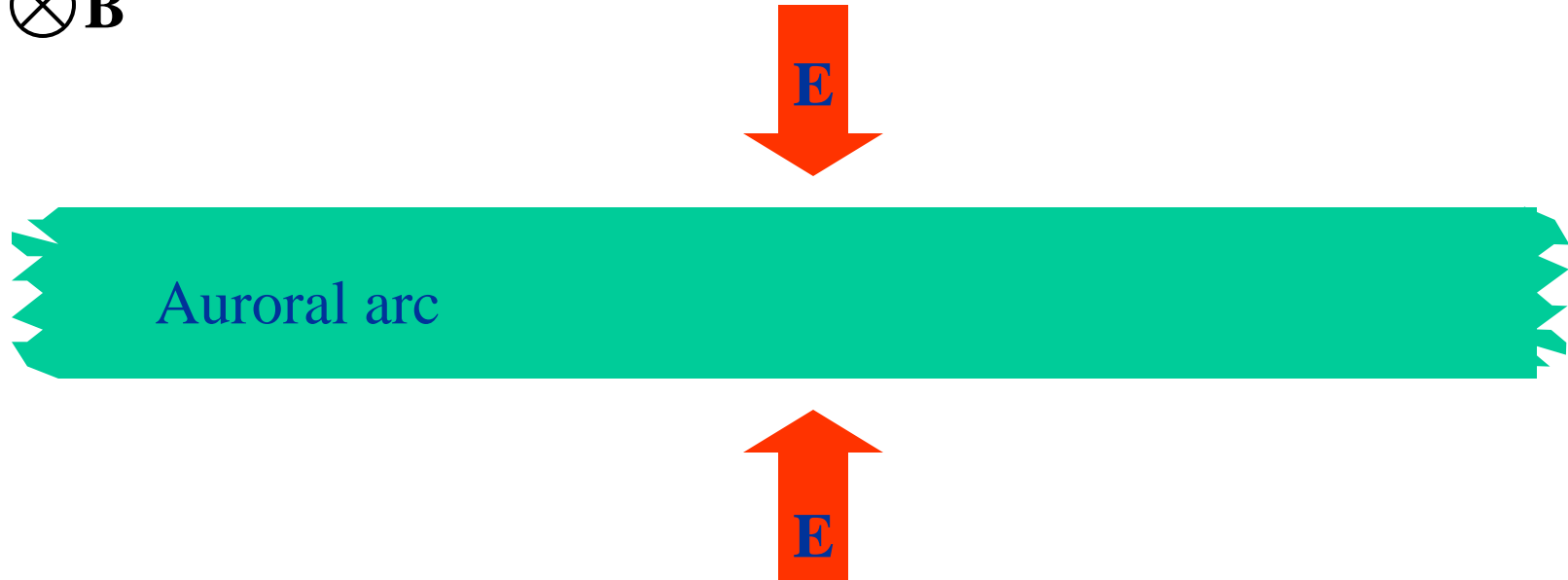
Bernoulli's equation:

$$p_1 + \rho v_1^2 = p_2 + \rho v_2^2 = \text{const.}$$

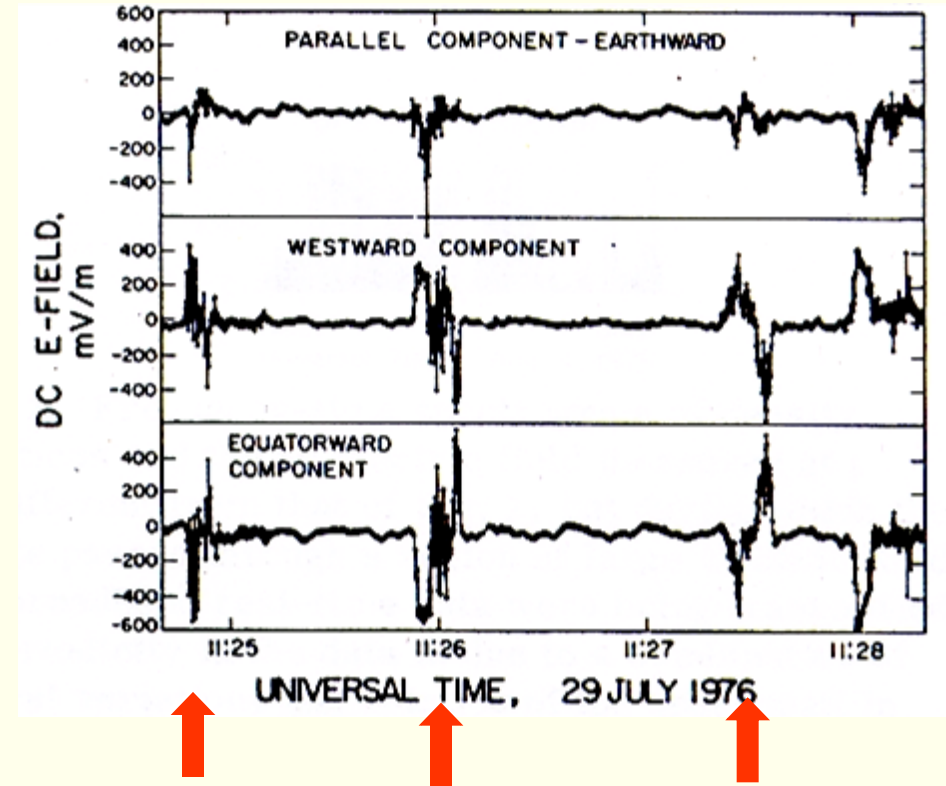
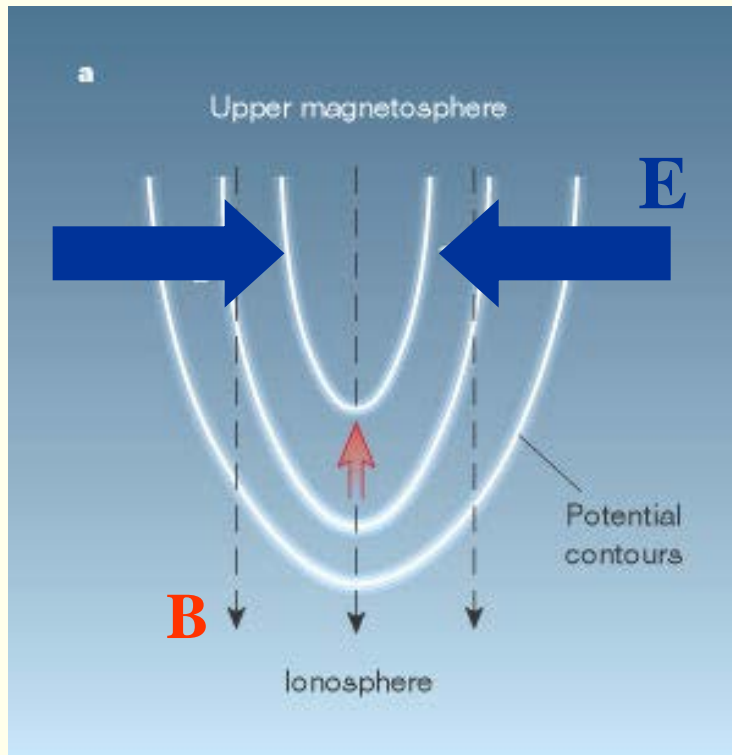
$$\therefore p_1 > p > p_2$$

# Spirals – Kelvin-Helmholz instability

$\otimes$  B

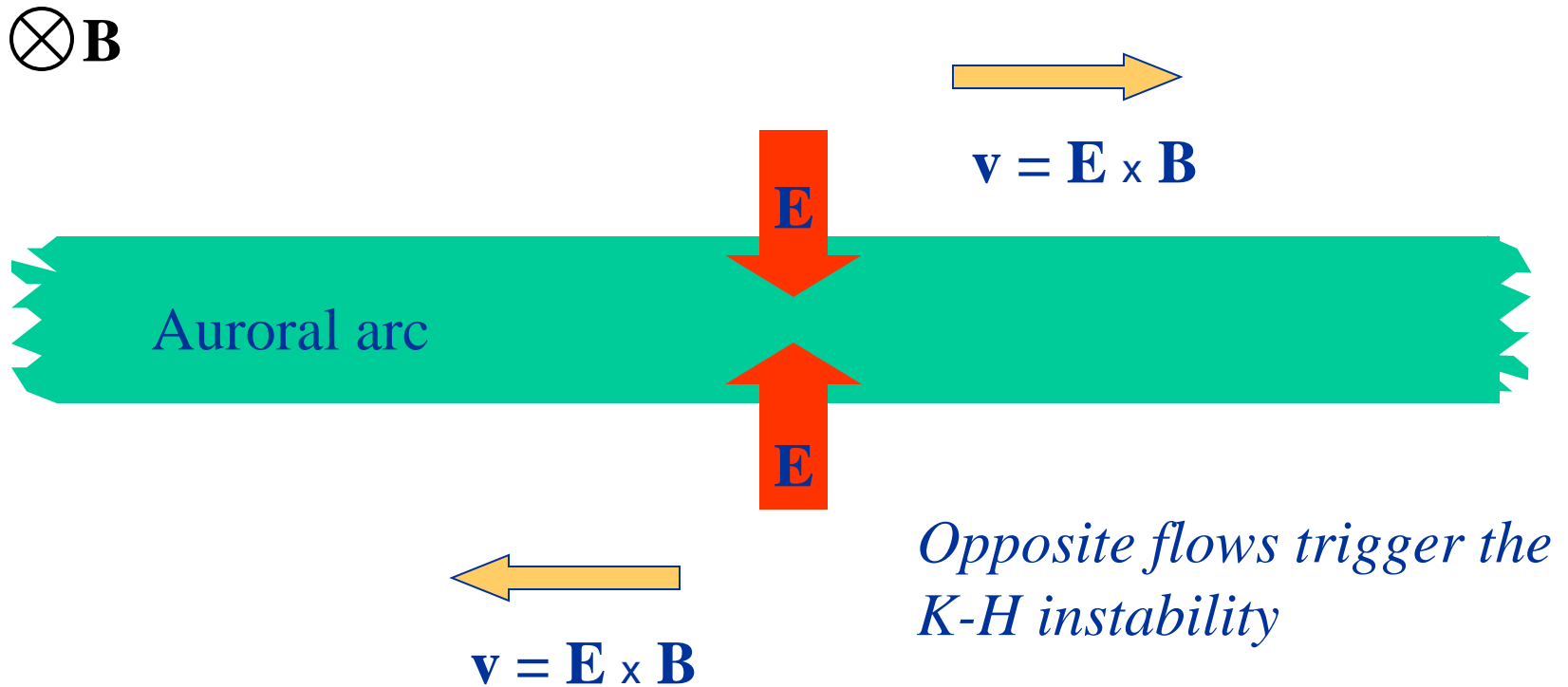


# Satellite signatures of U potential

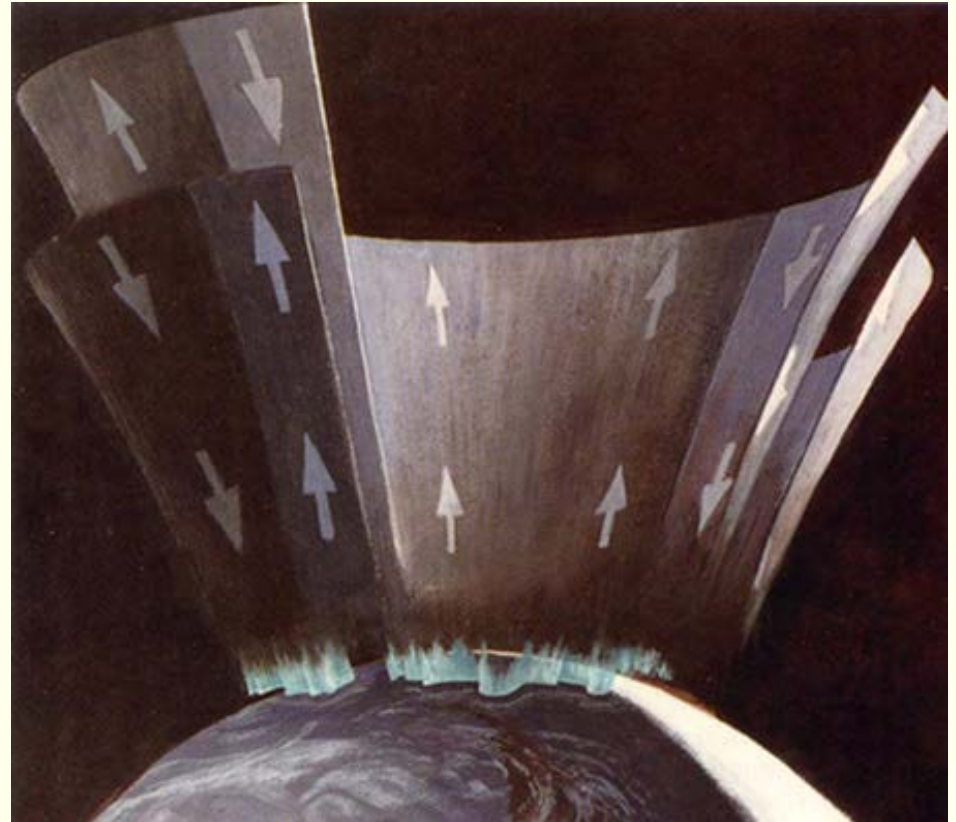
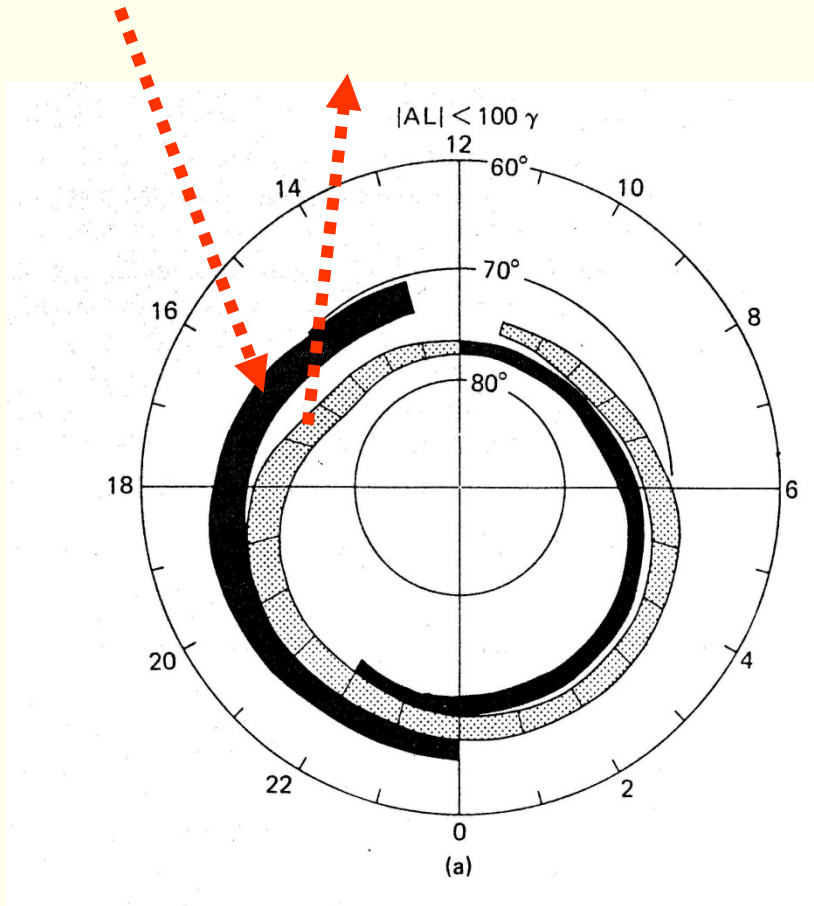


Measurements made by the ISEE satellite  
(Mozer et al., 1977)

# Spirals – Kelvin-Helmholz instability

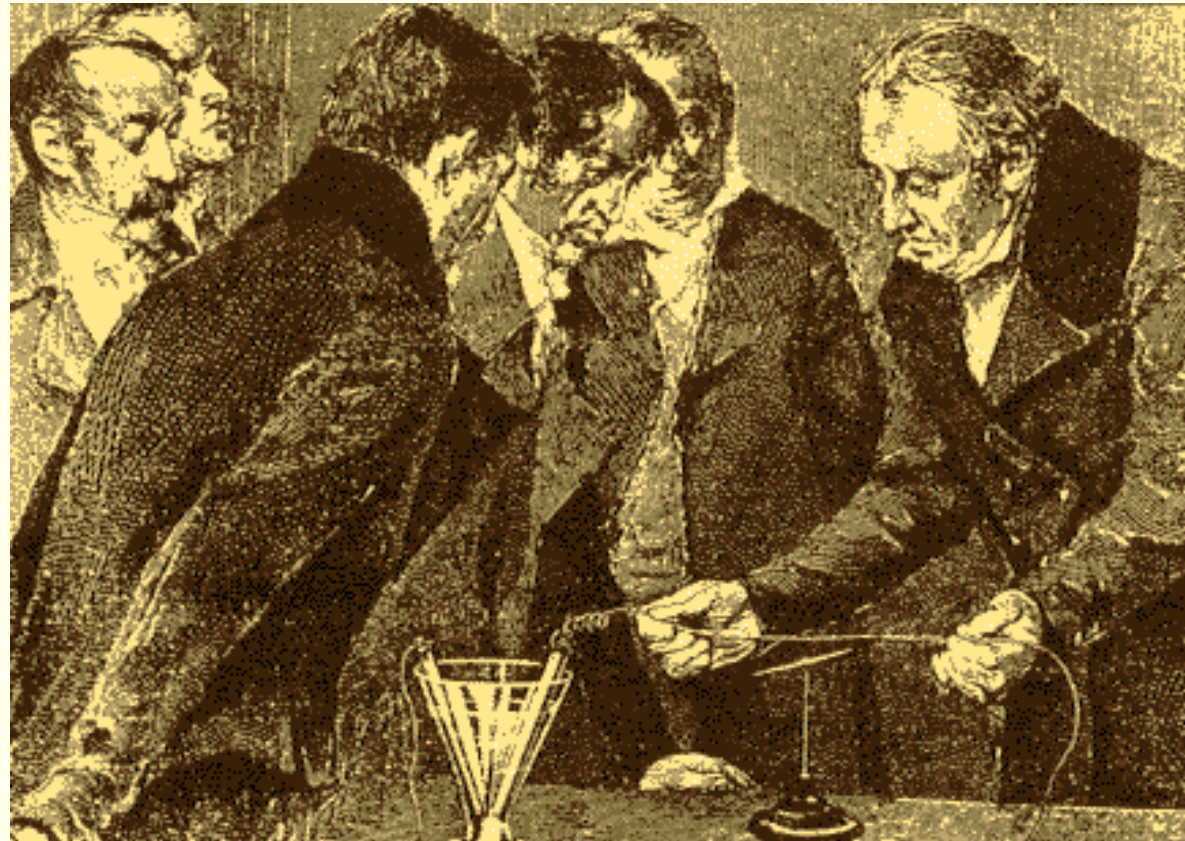


# Birkeland currents in the auroral oval

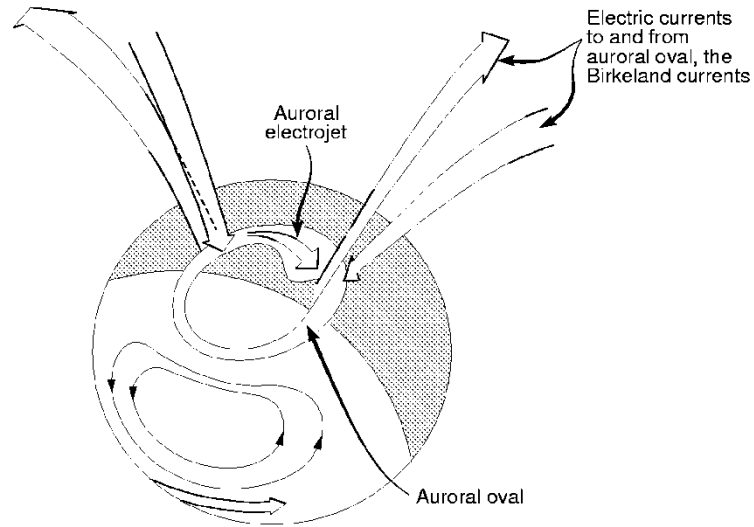




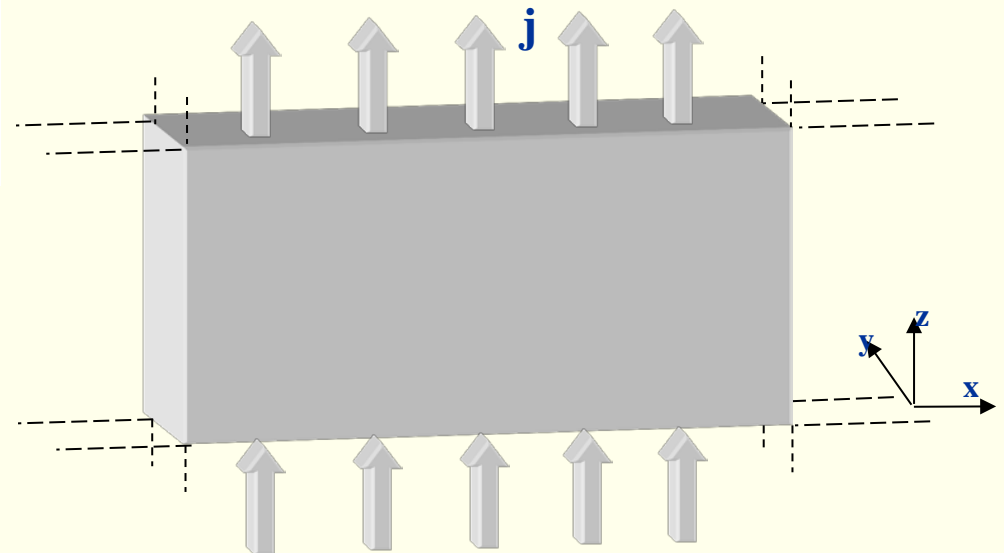
# How can you measure currents in space?



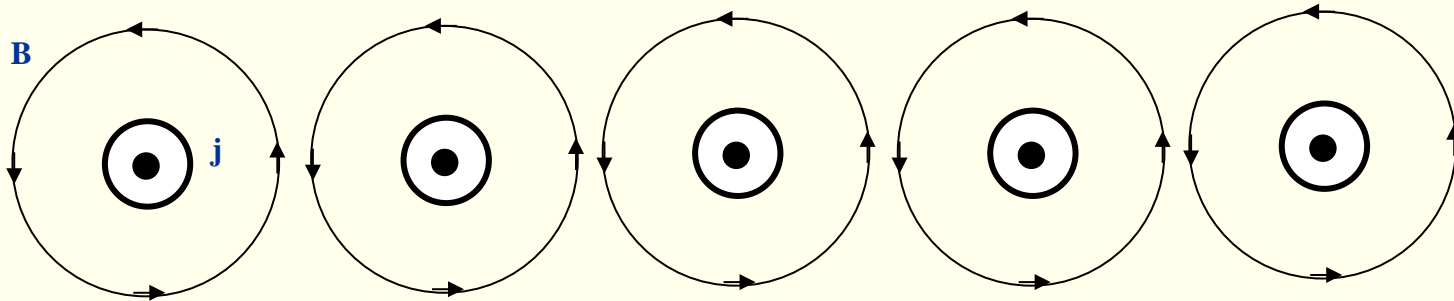
# Current sheet approximation



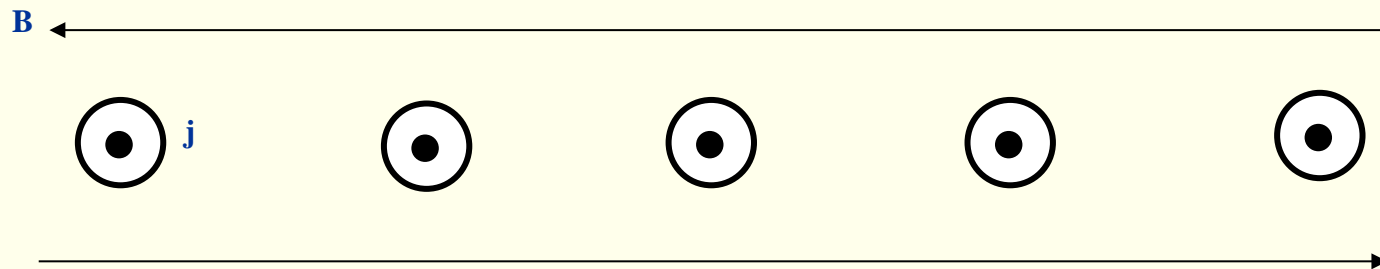
Approximate currents by thin current sheets with infinite size in the  $x$ - and  $z$ -directions.



# Current sheet approximation

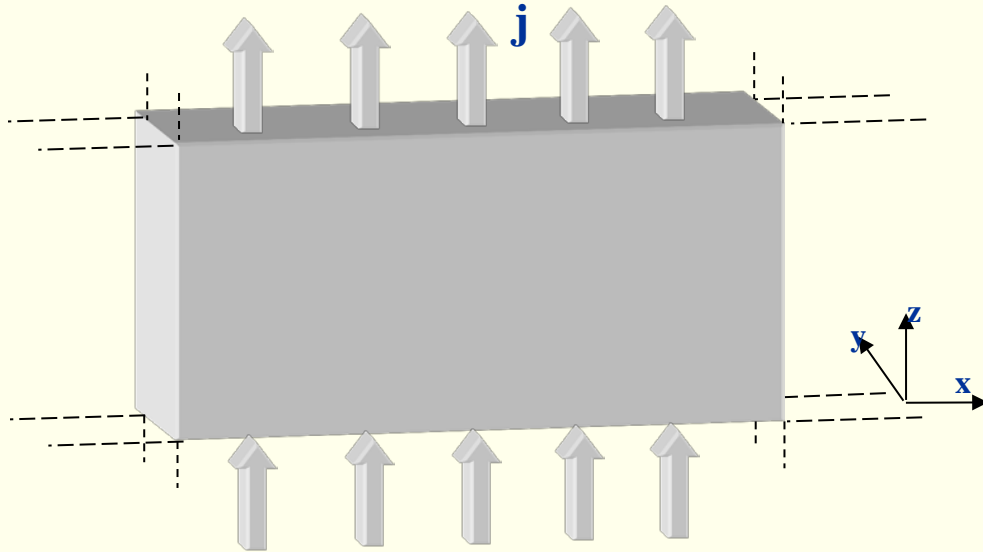


What will the magnetic field around such a current configuration be? Start by approximating with line currents to get a qualitative picture.



The closer you place the line currents, the more the magnetic fields between the line currents will cancel

# Current sheet approximation and Ampère's law



$$\left( \frac{\partial B_z}{\partial y} - \frac{\partial B_y}{\partial z}, \frac{\partial B_x}{\partial z} - \frac{\partial B_z}{\partial x}, \frac{\partial B_y}{\partial x} - \frac{\partial B_x}{\partial y} \right) = \mu_0 (j_x, j_y, j_z)$$

But  $\frac{\partial}{\partial x} = 0$  and  $\frac{\partial}{\partial z} = 0$

$$\left( \frac{\partial B_z}{\partial y}, 0, -\frac{\partial B_x}{\partial y} \right) = \mu_0 (0, 0, j_z)$$

eller

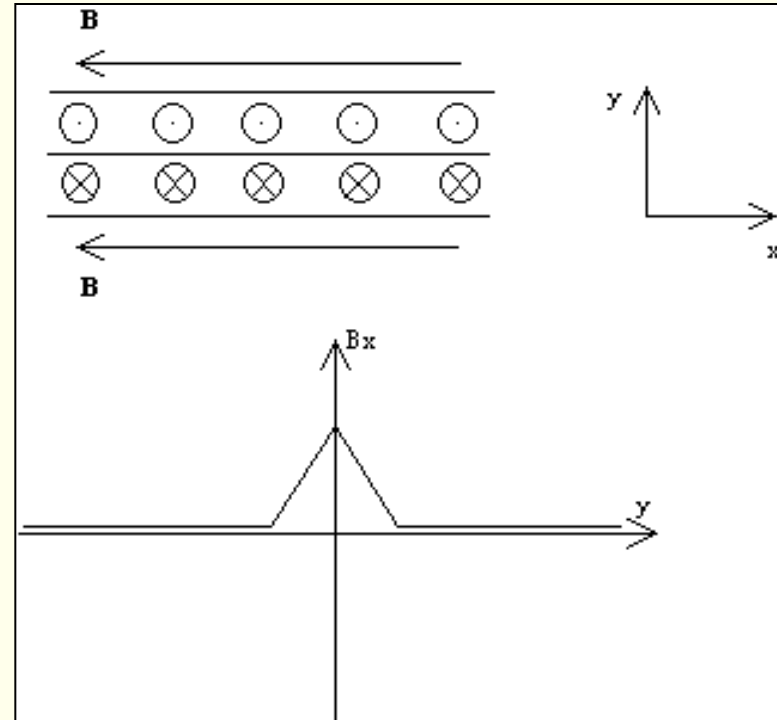
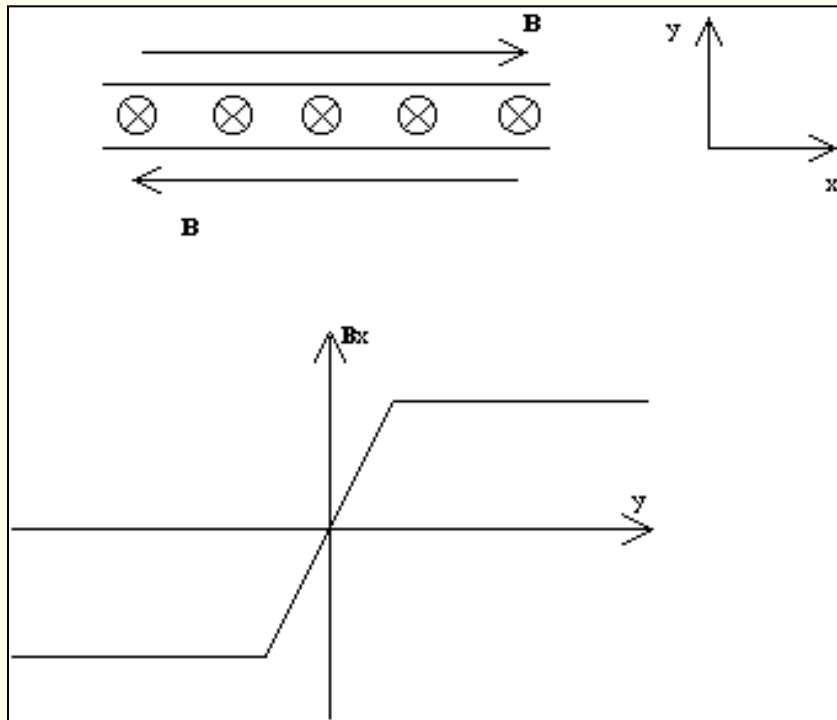
Ampère's law (no time dependence):

$$\nabla \times \mathbf{B} = \mu_0 \mathbf{j}$$

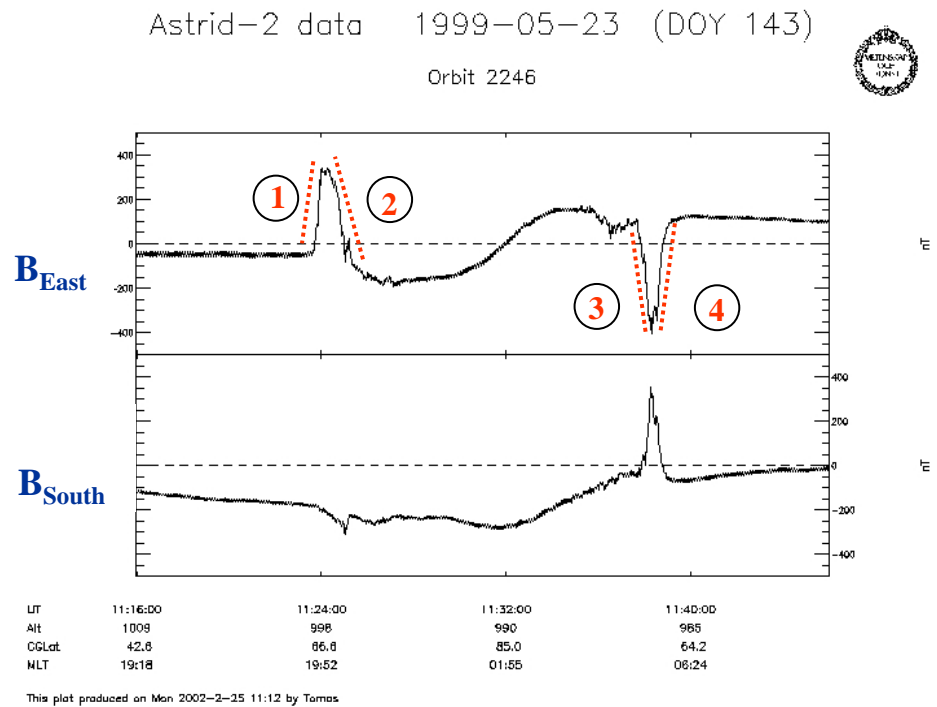
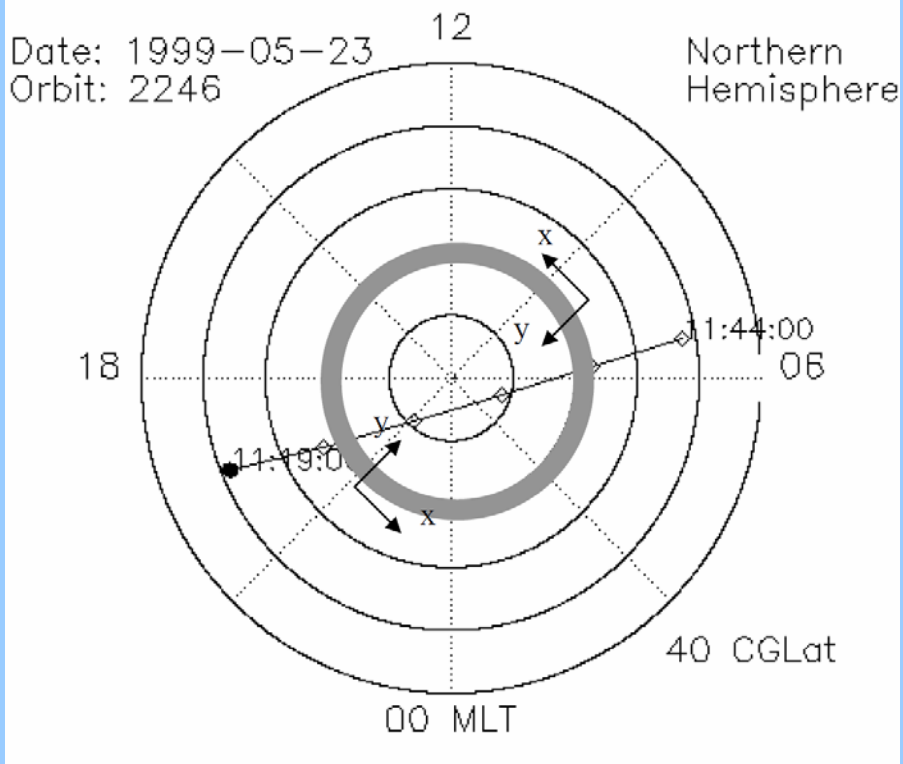


$$j_z = -\frac{1}{\mu_0} \frac{\partial B_x}{\partial y}$$

# Current sheet - example



$$j_z = -\frac{1}{\mu_0} \frac{\partial B_x}{\partial y}$$



What is the direction of the current in current sheet 1?

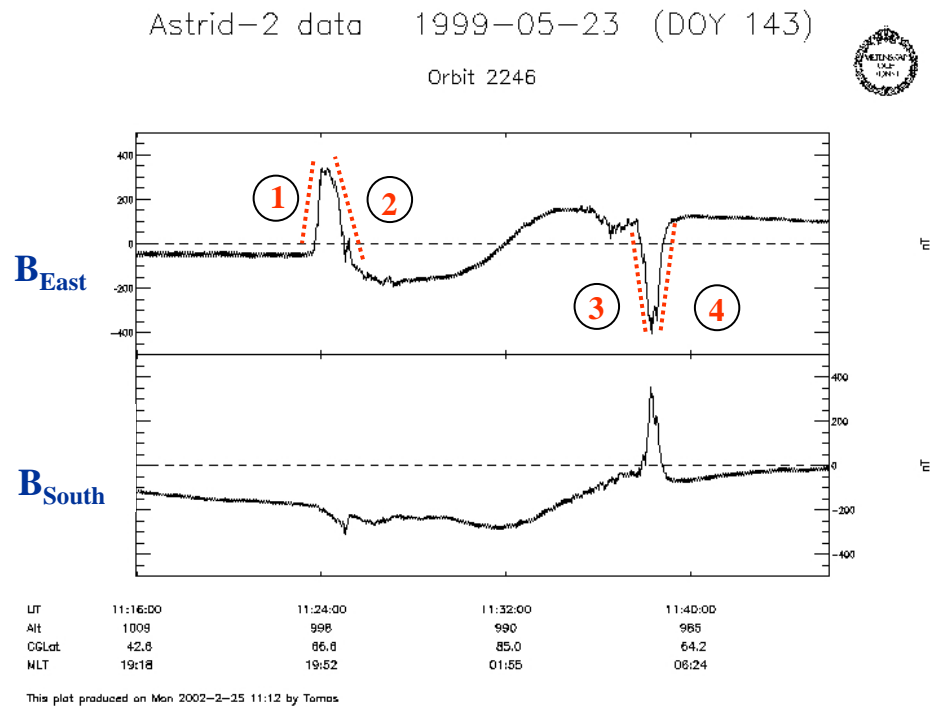
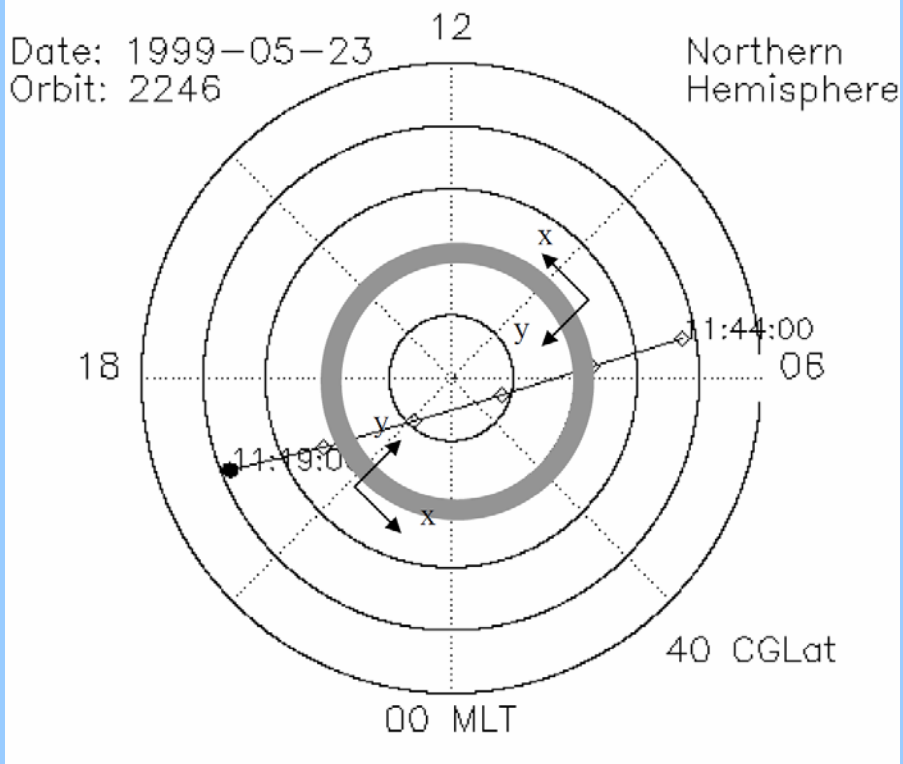
$$j_z = -\frac{1}{\mu_0} \frac{\partial B_x}{\partial y}$$

Blue

Into the ionosphere

Red

Out of the ionosphere



What is the direction of the current in current sheet 1?

$$j_z = -\frac{1}{\mu_0} \frac{\partial B_x}{\partial y}$$

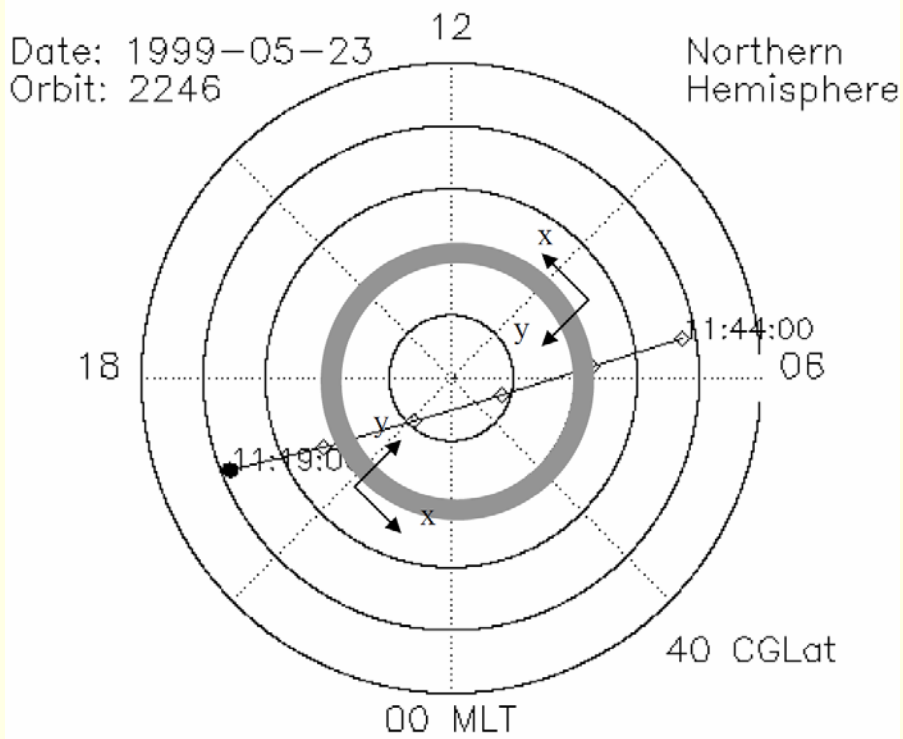
$$\frac{\partial B_x}{\partial y} = \frac{\partial B_{East}}{\partial y} > 0$$

Blue

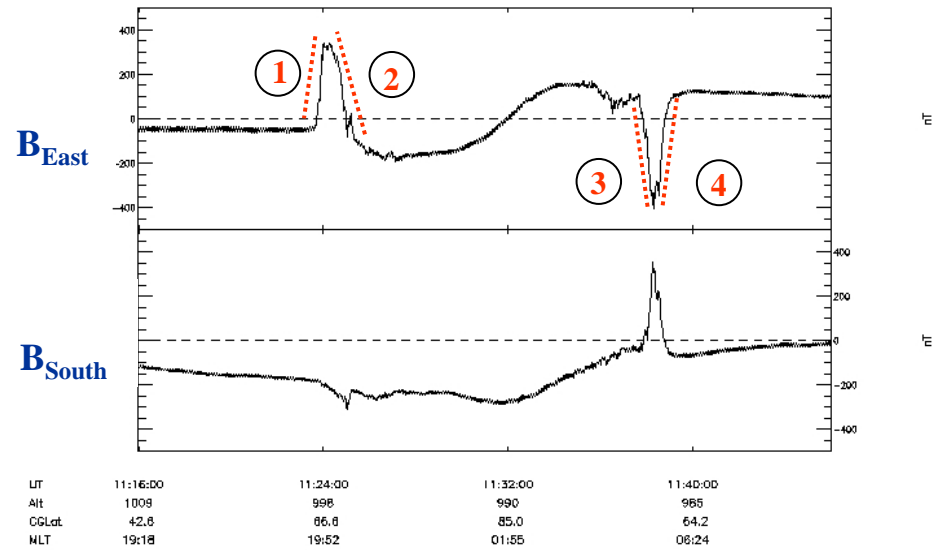
Into the ionosphere

$\Rightarrow$

$$j_z < 0$$



Astrid-2 data 1999-05-23 (DOY 143)  
Orbit 2246



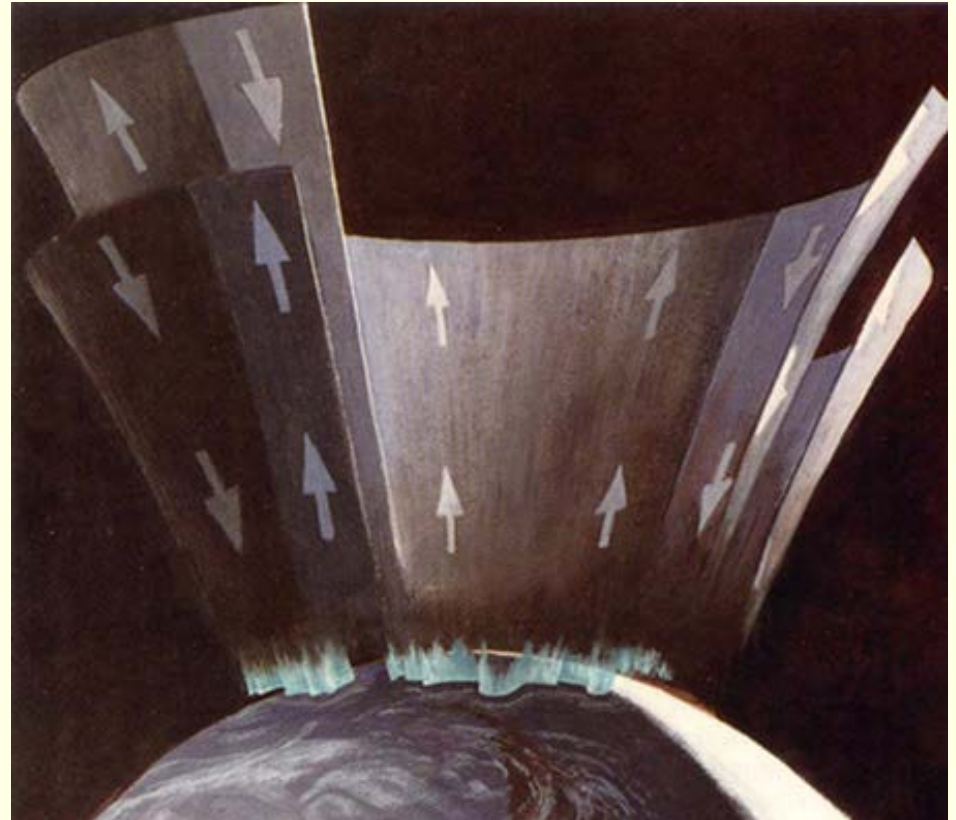
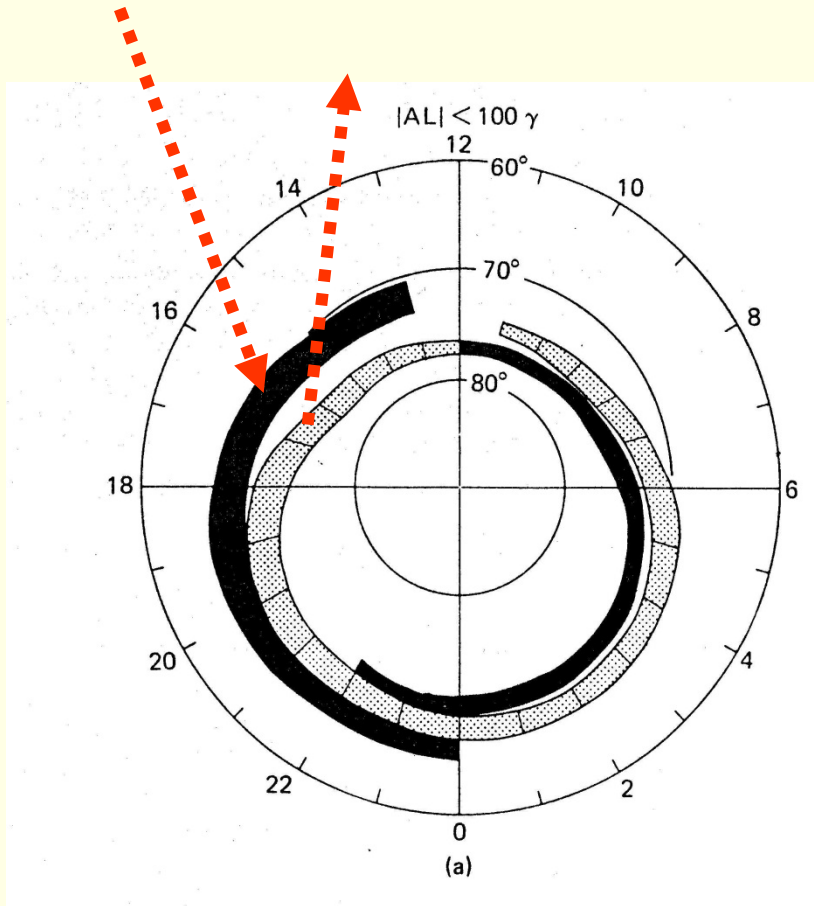
This plot produced on Mon 2002-2-25 11:12 by Tomas

$$j_z = -\frac{1}{\mu_0} \frac{\partial B_x}{\partial y}$$

- |    |                                       |               |           |                       |
|----|---------------------------------------|---------------|-----------|-----------------------|
| 1) | $\frac{\partial B_x}{\partial y} > 0$ | $\Rightarrow$ | $j_z < 0$ | Into the ionosphere   |
| 2) | $\frac{\partial B_x}{\partial y} < 0$ | $\Rightarrow$ | $j_z > 0$ | Out of the ionosphere |
| 3) | $\frac{\partial B_x}{\partial y} > 0$ | $\Rightarrow$ | $j_z < 0$ | Into the ionosphere   |
| 4) | $\frac{\partial B_x}{\partial y} < 0$ | $\Rightarrow$ | $j_z > 0$ | Out of the ionosphere |



# Birkeland currents in the auroral oval





# At what planets do you expect aurora to exist?

Blue

Earth, Mercury,  
Jupiter, Saturn

Yellow

Earth, Venus, Jupiter,  
Saturn, Uranus,  
Neptune

Green

Earth, Mars, Jupiter,  
Saturn, Uranus,  
Neptune

Red

Earth, Jupiter, Saturn,  
Uranus, Neptune



# What do we need to have an aurora?

- Magnetic field (to guide the plasma particles towards the planet)
- Atmosphere (to create emissions)

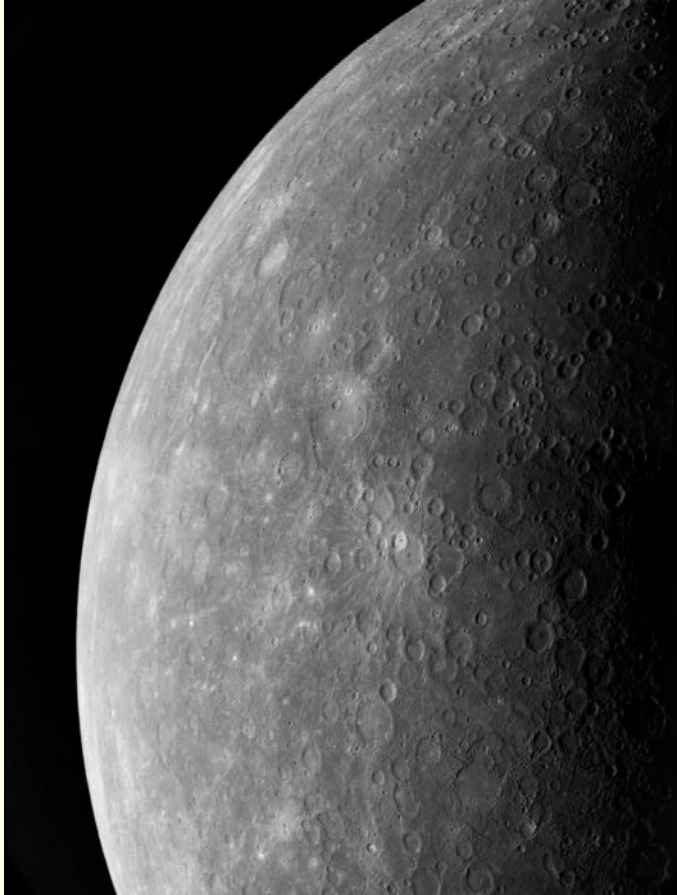


# At what planets do you expect aurora to exist?

Red

Earth, Jupiter, Saturn,  
Uranus, Neptune

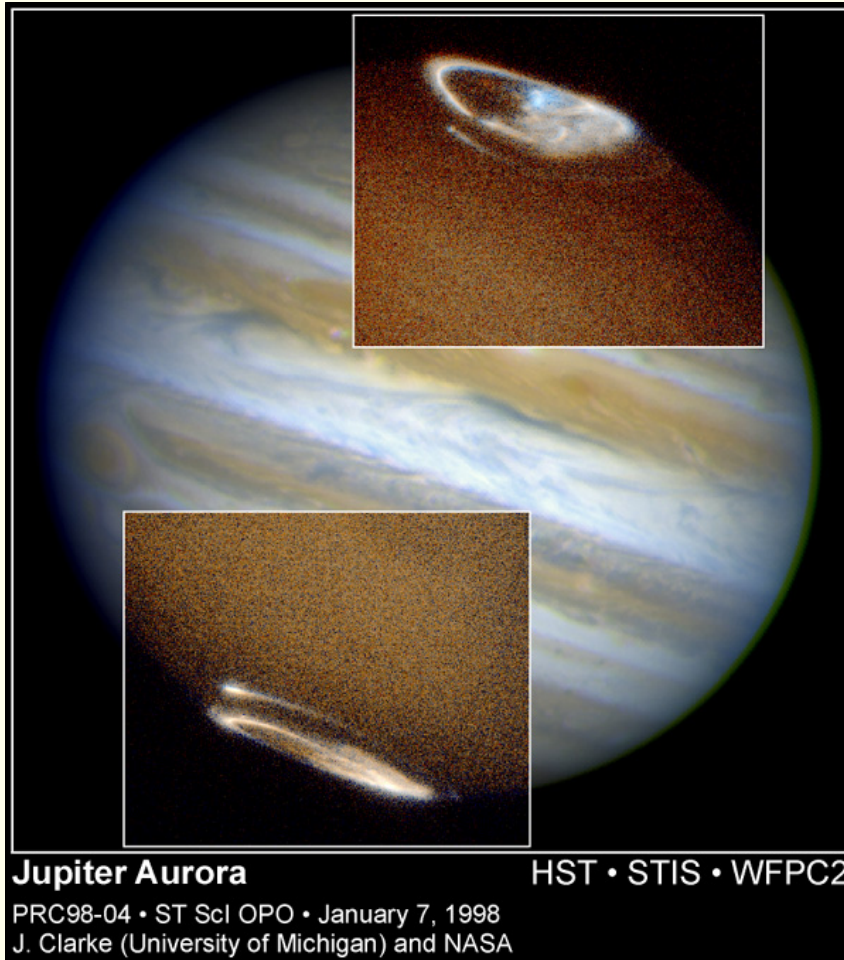
# Mercury



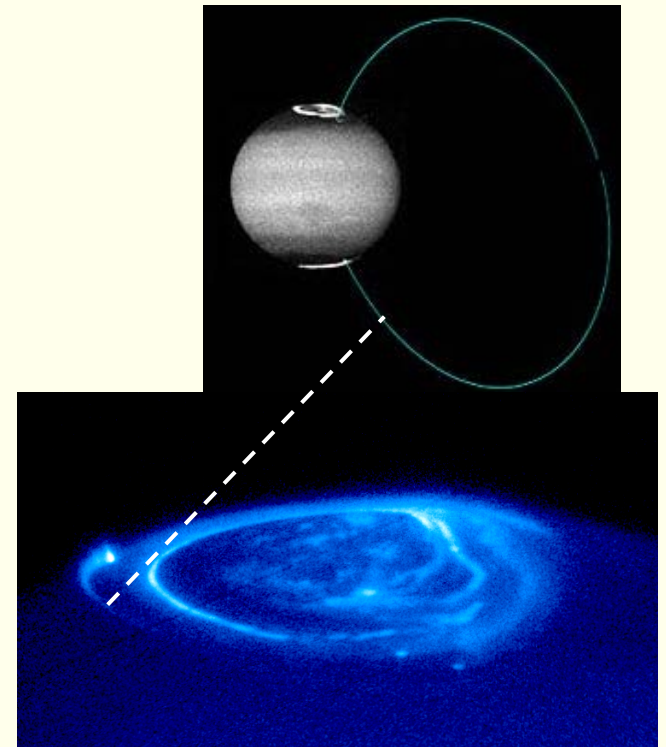
- No atmosphere
- X-ray aurora???  
*Can possibly be created by electrons colliding directly with the planetary surface and lose their energy in one single collision.*

# Jupiter aurora

- Jupiter's aurora has a power of  $\sim 1000$  TW (*compare Earth:  $\sim 100$  GW, nuclear power plant:  $\sim 1$  GW*)
- Note the “extra” oval on Io's flux tube!

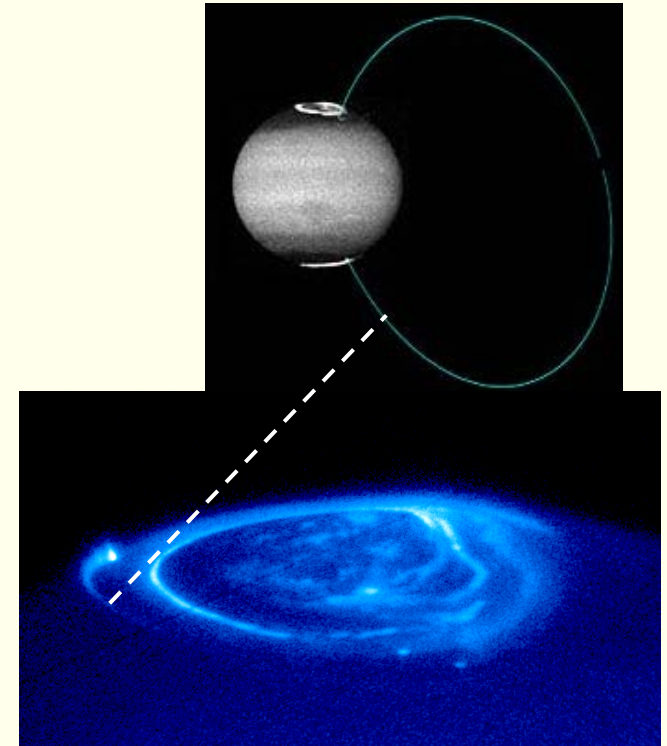
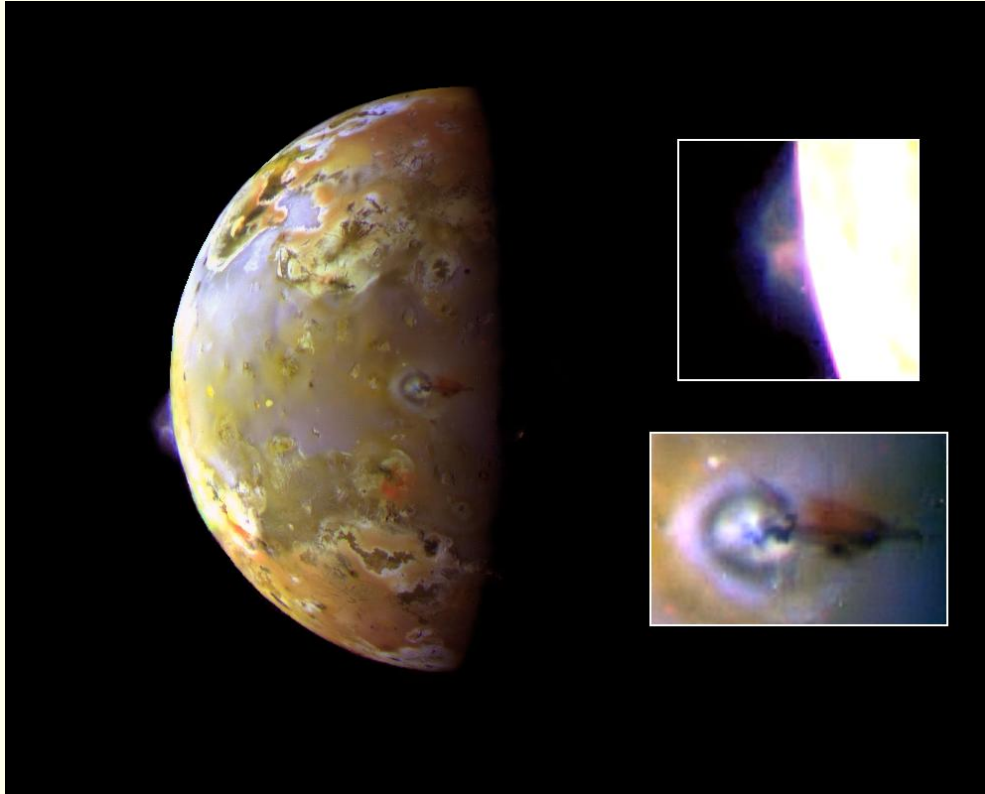


*Foto från Hubble Space Telescope*



# Jupiter and Io

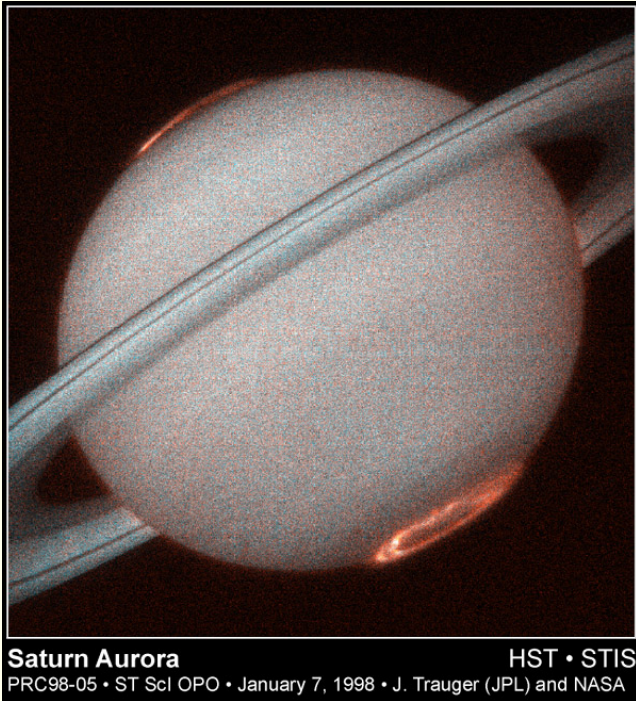
*Photo from rymdsonden Galileo*



The Jupiter moon Io is very volcanically active, and deposits large amounts of dust and gas in Jupiter's magnetosphere. This is ionized by the sunlight, and the charged plasma particles follow Jupiter's magnetic field lines towards the atmosphere and cause auroral emissions.

# Aurora of the other planets

## Saturn



*Uranus: Auora detected in UV.  
Probably associated with Uranus' ring  
current/radiation belts and not very  
dynamic.*

*Neptunus: weak UV aurora detected.*

*Mars, Venus: No aurora.*

*Saturnus' aurora: not noticeably different  
from Jupiter's, but much weaker. (Total  
power about the same as Earth's aurora.)*



# Prerequisites for...



## Life

- Energy source (sun)
- Atmosphere
- Magnetic field
- Water



## Aurora

- Energy source (sun)
- Atmosphere
- Magnetic field



# On space weather and viewing aurora

## Some space weather sites

<http://spaceweather.com/>

<http://www.esa-spaceweather.net/>

<http://sunearthday.nasa.gov/swac/>

[http://www.noaawatch.gov/themes/spac  
e.php](http://www.noaawatch.gov/themes/spac<br/>e.php)

[http://www.windows2universe.org/spac  
e  
weather/more\\_details.html](http://www.windows2universe.org/spac<br/>e<br/>weather/more_details.html)

## Kiruna

Kiruna all-sky camera:

<http://www.irf.se/allsky/rtasc.php>

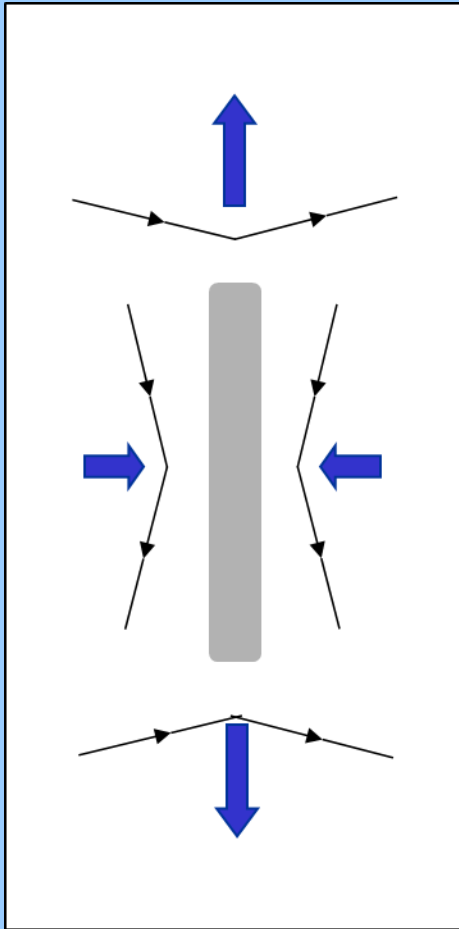
[http://sunearthday.nasa.gov/swac/  
tutorials/aur\\_kiruna.php](http://sunearthday.nasa.gov/swac/<br/>tutorials/aur_kiruna.php)

Forecasts:

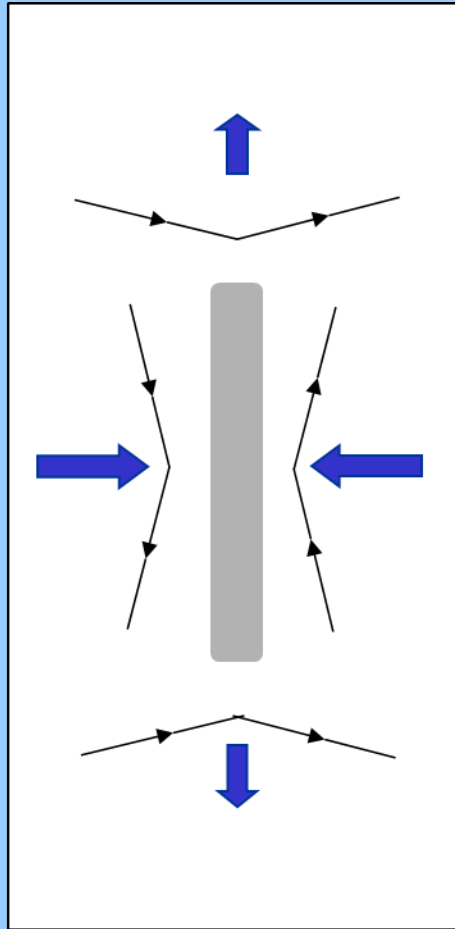
<http://flare.lund.irf.se/rwc/aurora/>

[http://www.irf.se/Observatory/?li  
nk\[All-  
skycamera\]=Aurora\\_sp\\_statistics](http://www.irf.se/Observatory/?li<br/>nk[All-<br/>skycamera]=Aurora_sp_statistics)

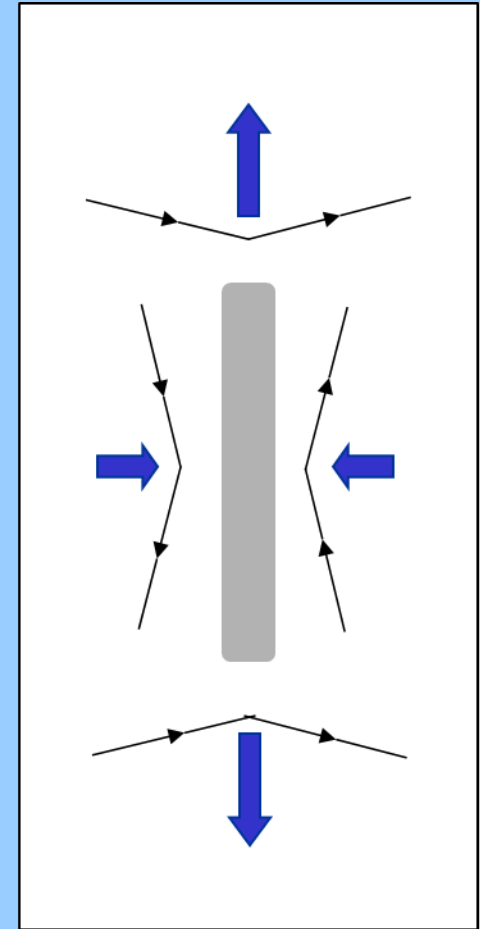
# Magnetic reconnection



Green

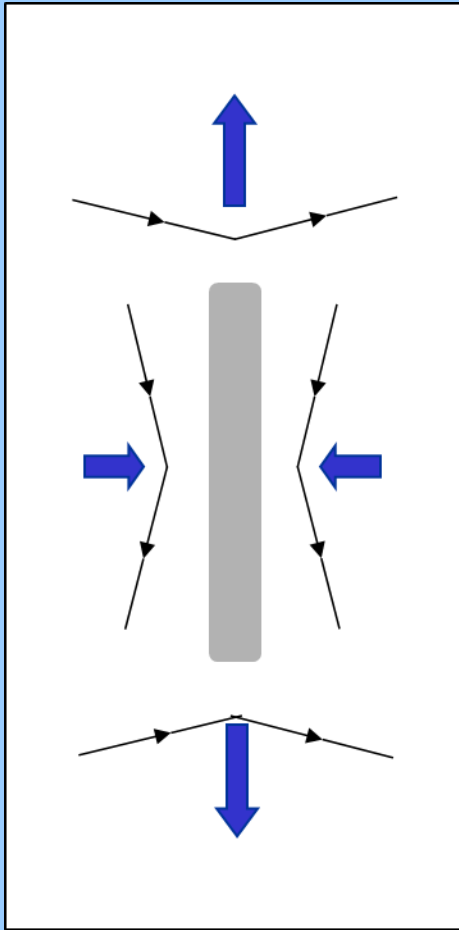


Yellow

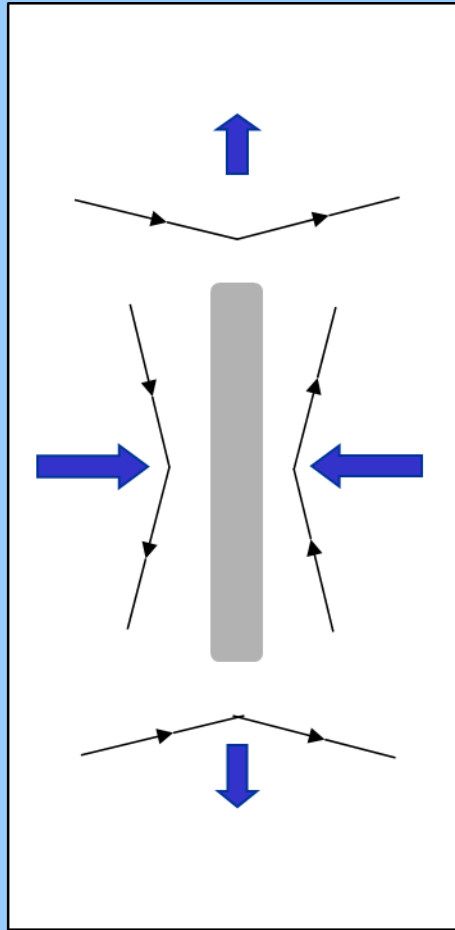


Red

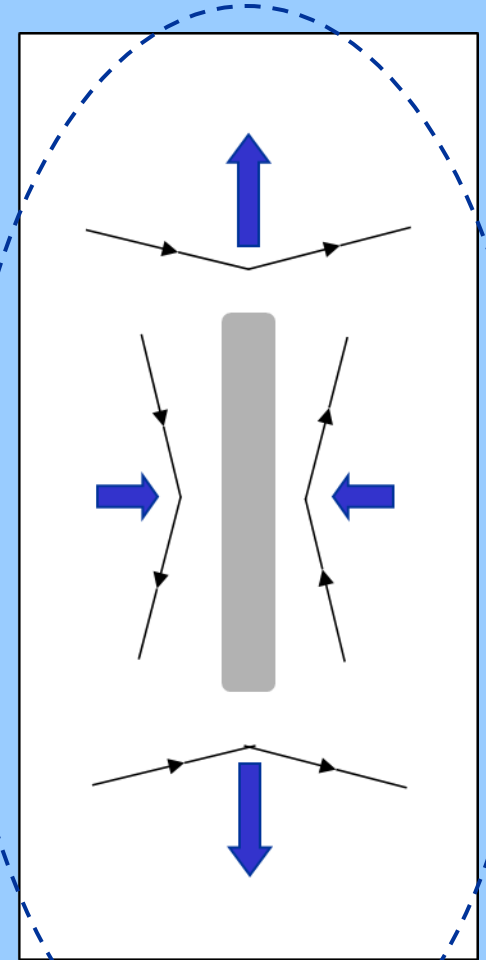
# Magnetic reconnection



Green

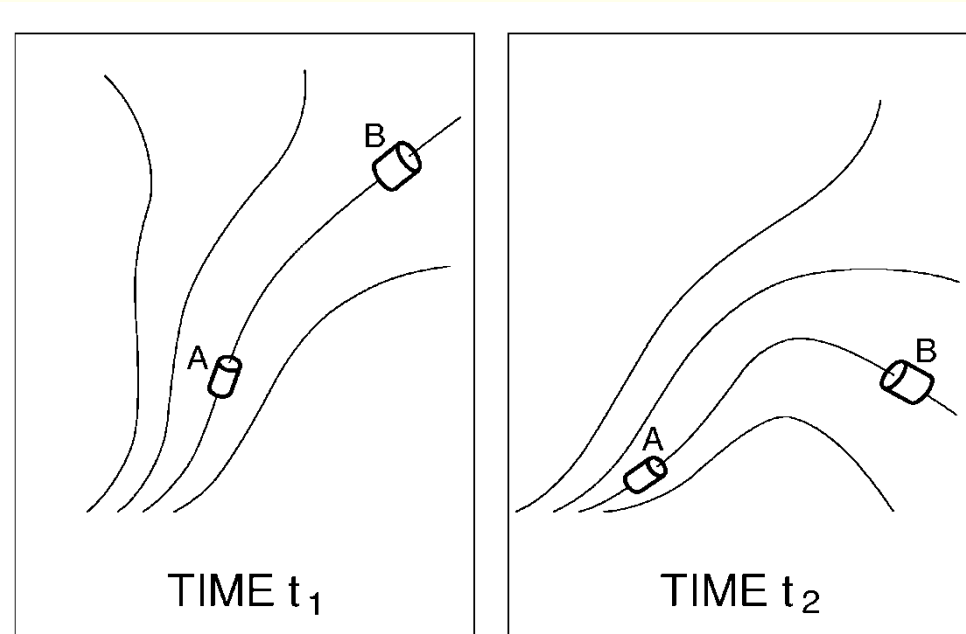


Yellow



Red

# Frozen in magnetic field lines

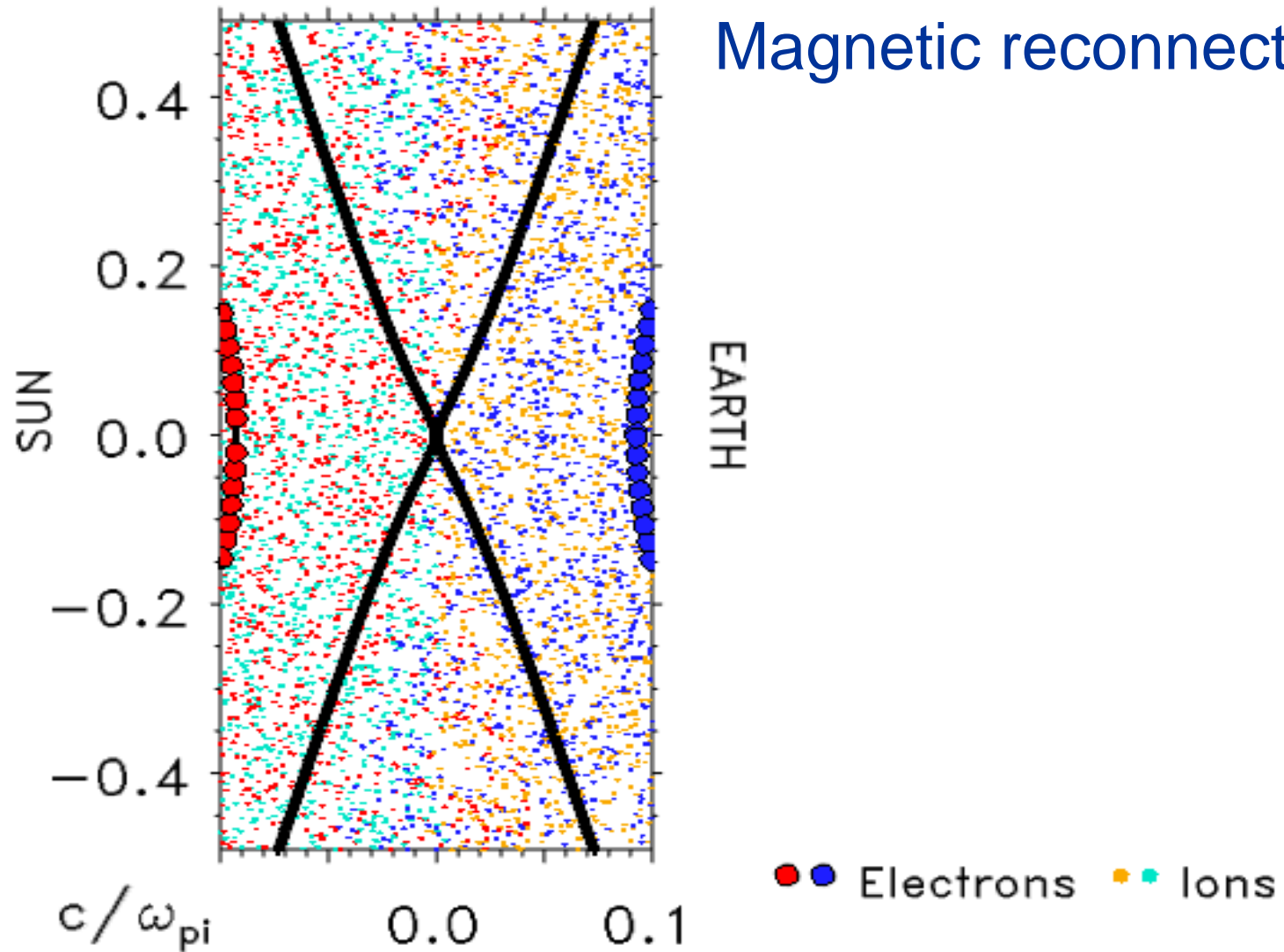


In fluid description of plasma two plasma elements that are connected by a common magnetic field line at time  $t_1$  will be so at any other time  $t_2$ .

This applies if the magnetic Reynolds number is large:

$$R_m = \mu_0 \sigma l_c v_c \gg 1$$

*An example of the collective behaviour of plasmas.*



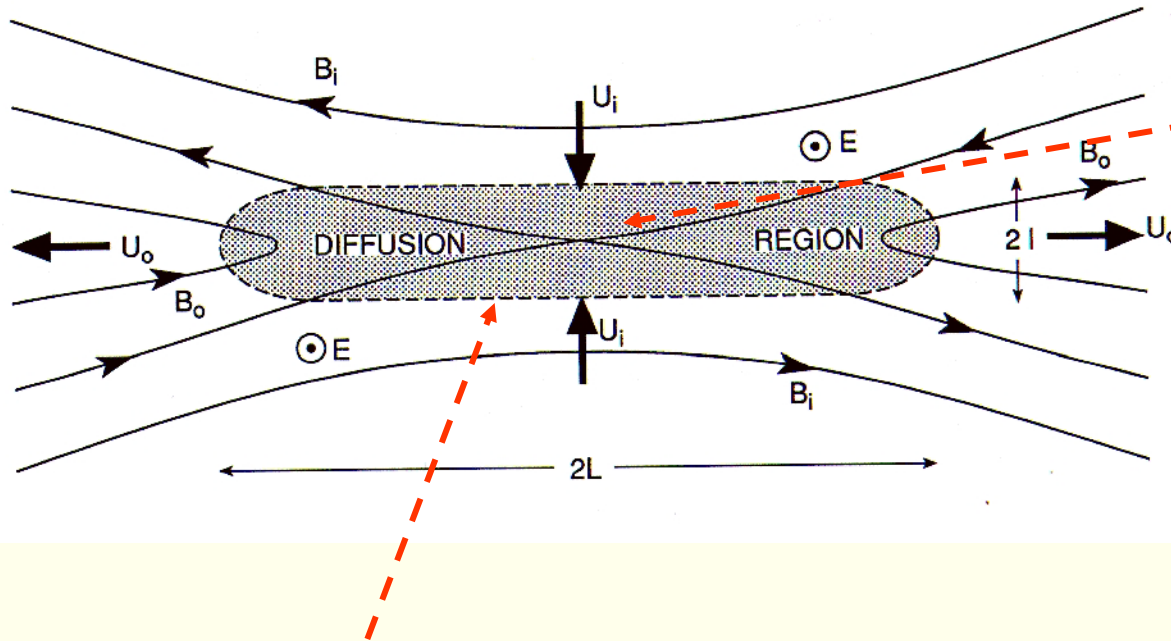
# Reconnection

In 'diffusion region':

$$R_m = \mu_0 \sigma l v \sim 1$$

Thus: **condition** for frozen-in magnetic field breaks down.

A second **condition** is that there are two regions of magnetic field pointing in *opposite* direction:

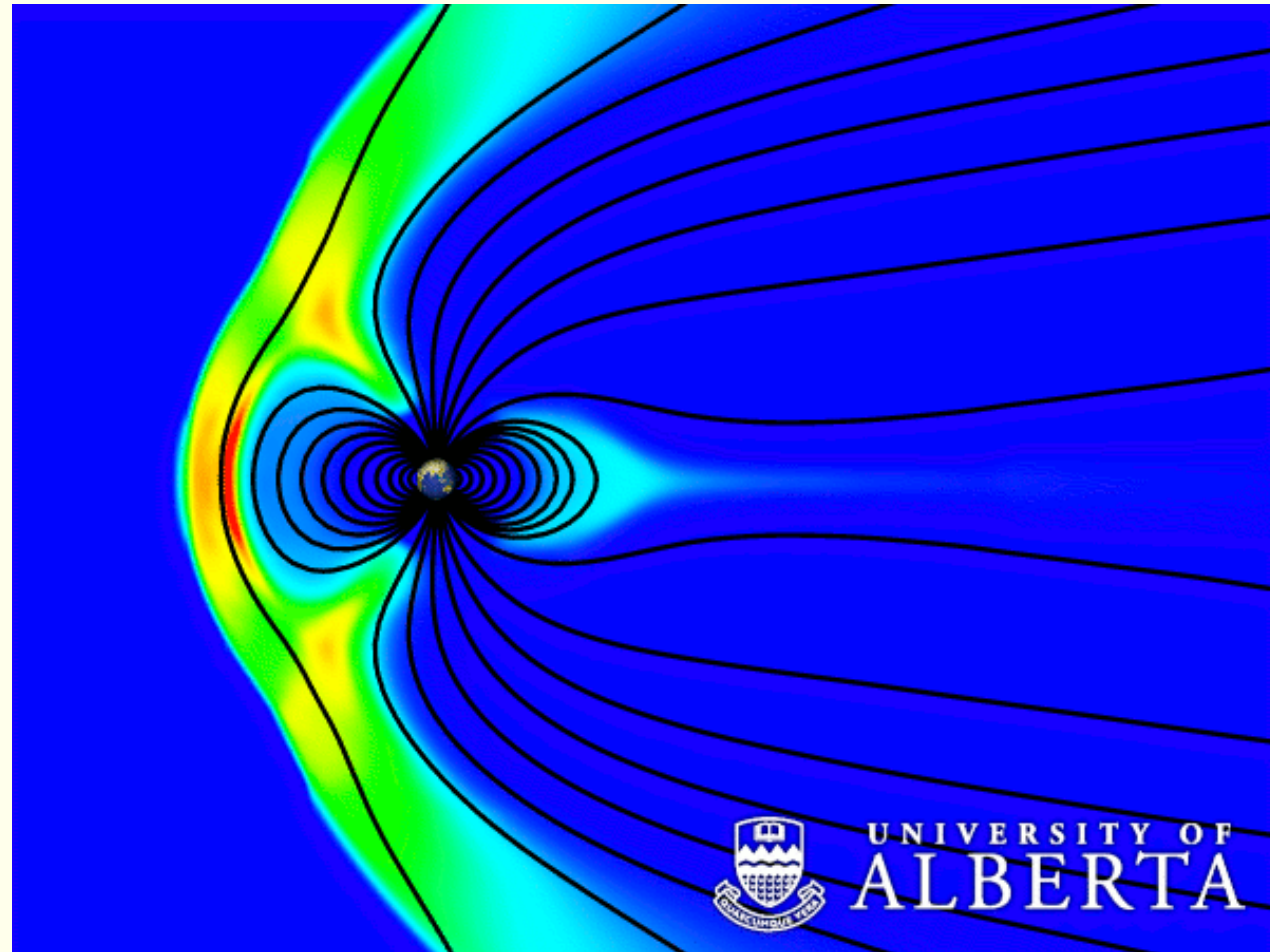


- Field lines are “cut” and can be re-connected to other field lines
- **Magnetic energy is transformed into kinetic energy ( $U_o \gg U_i$ )**
- **Plasma from different field lines can mix**

# Reconnection and plasma convection



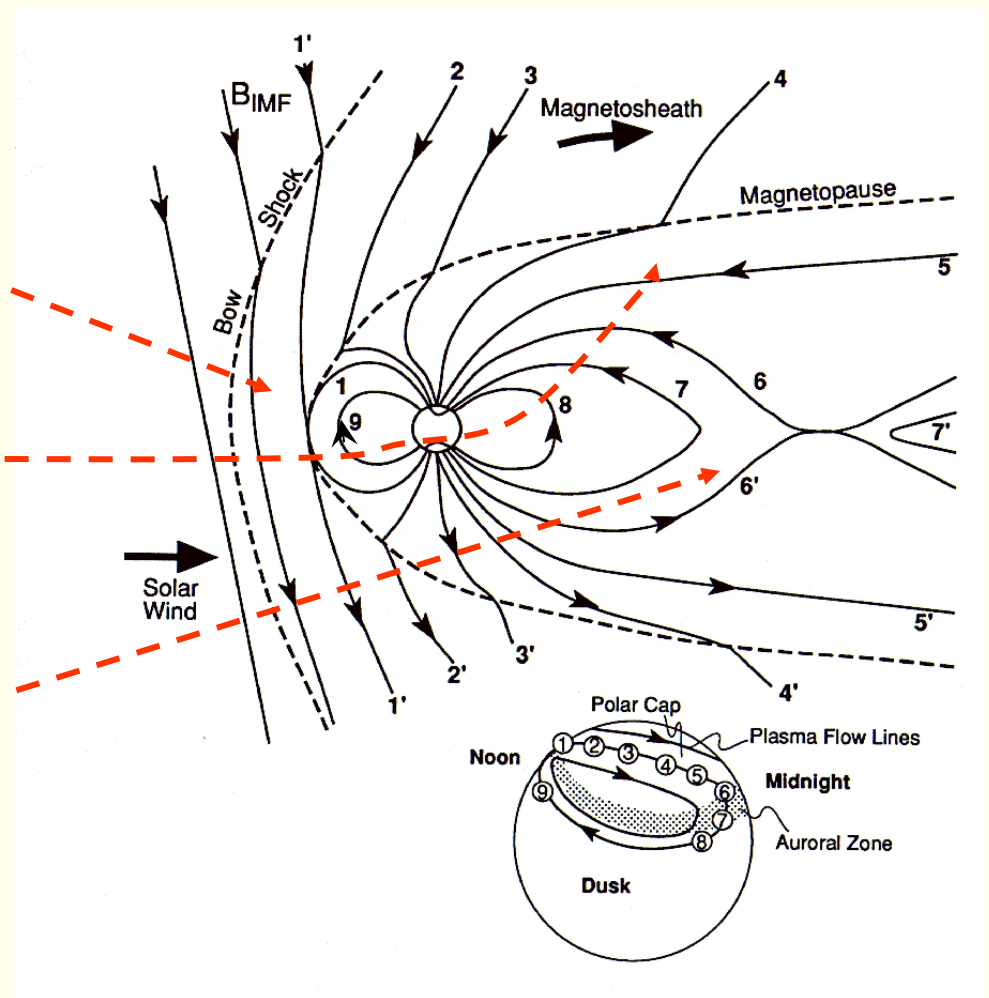
Solar wind



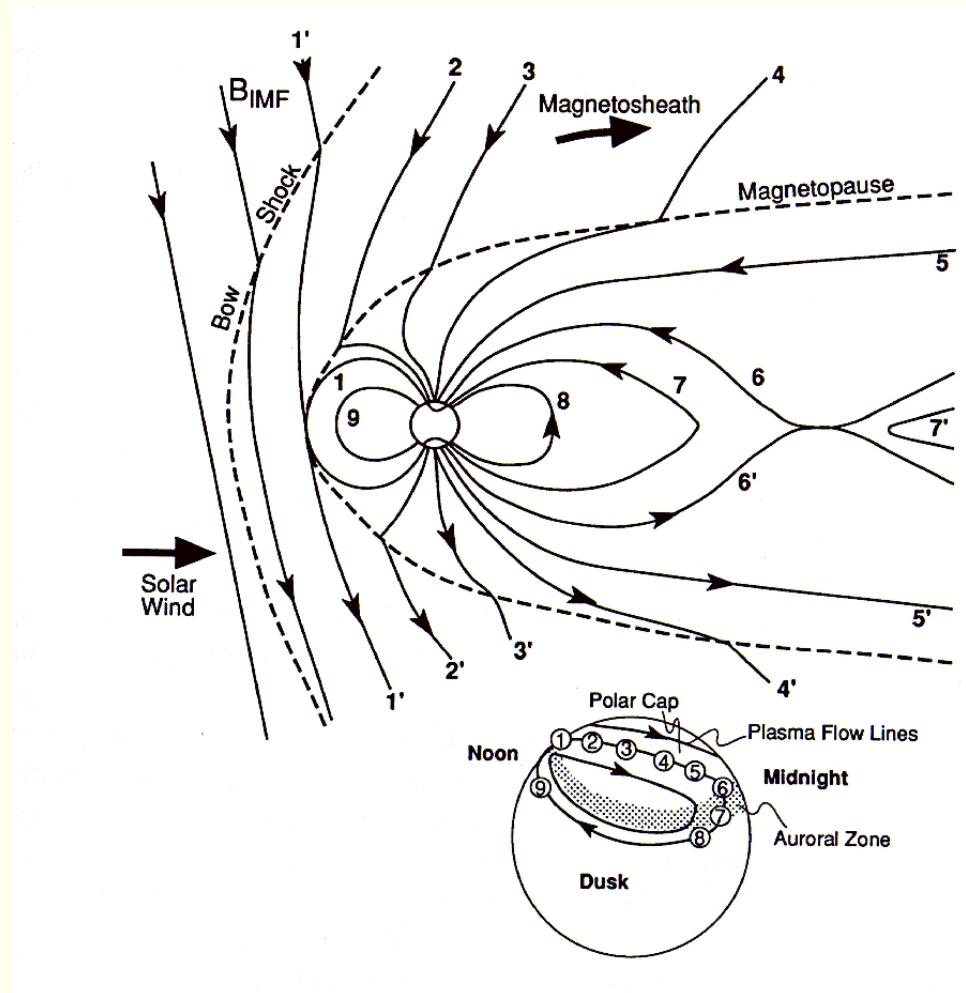


# Reconnection och plasma convection

- Reconnection on the dayside “re-connects” the solar wind magnetic field and the geomagnetic field
- In this way the plasma convection in the outer magnetosphere is driven
- In the night side a second reconnection region drives the convection in the inner magnetosphere. The reconnection also heats the plasmasheet plasma.

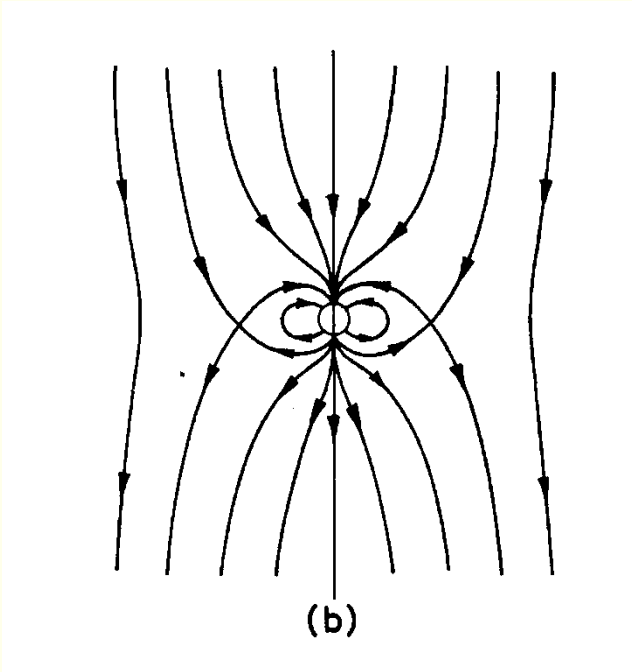


# What happens if IMF is northward instead?

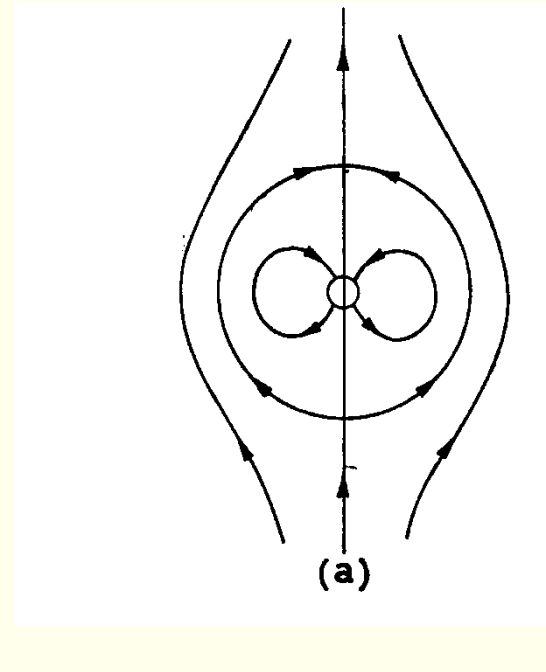


# Magnetospheric dynamics

*open magnetosphere*



*closed magnetosphere*



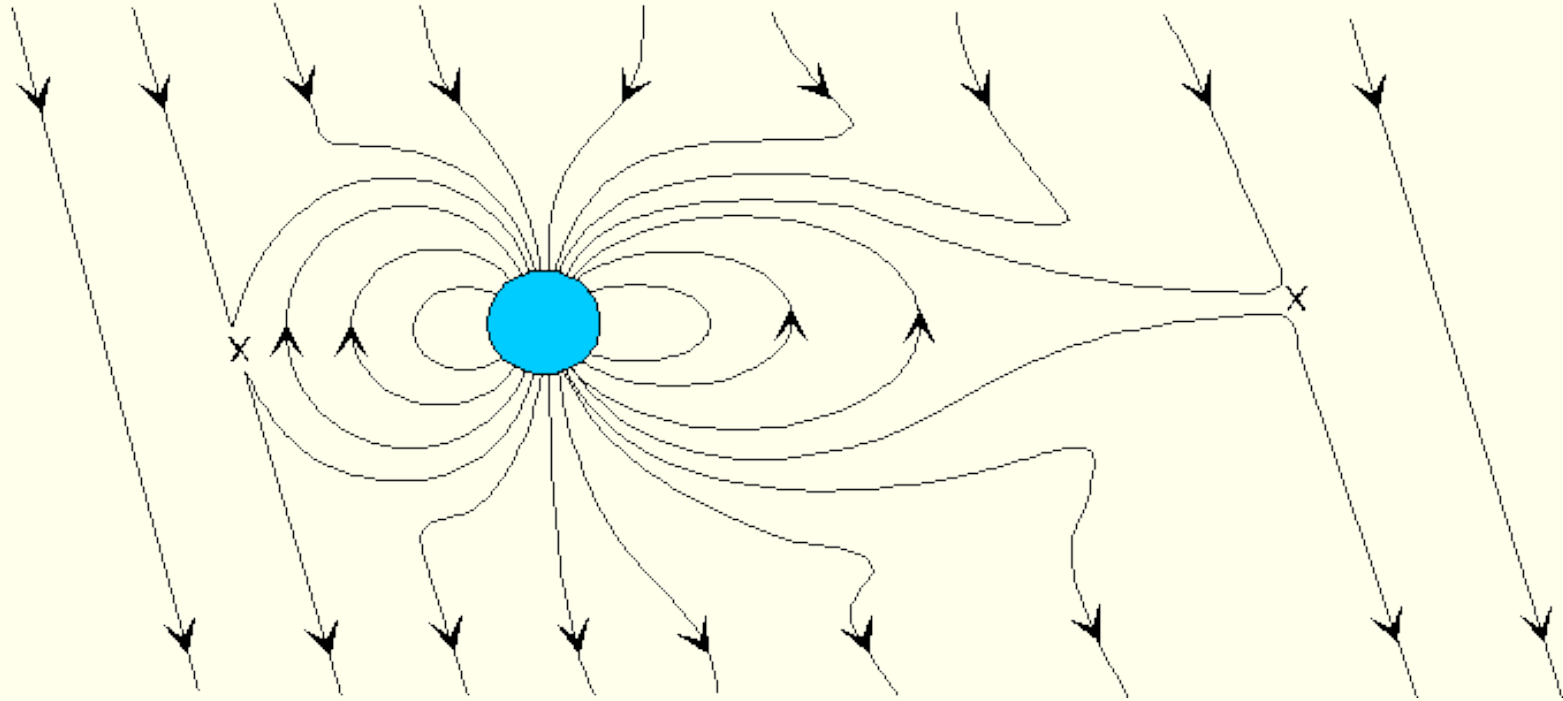
southward  


Interplanetary  
magnetic field (IMF)

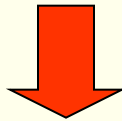
 northward

# Magnetospheric dynamics

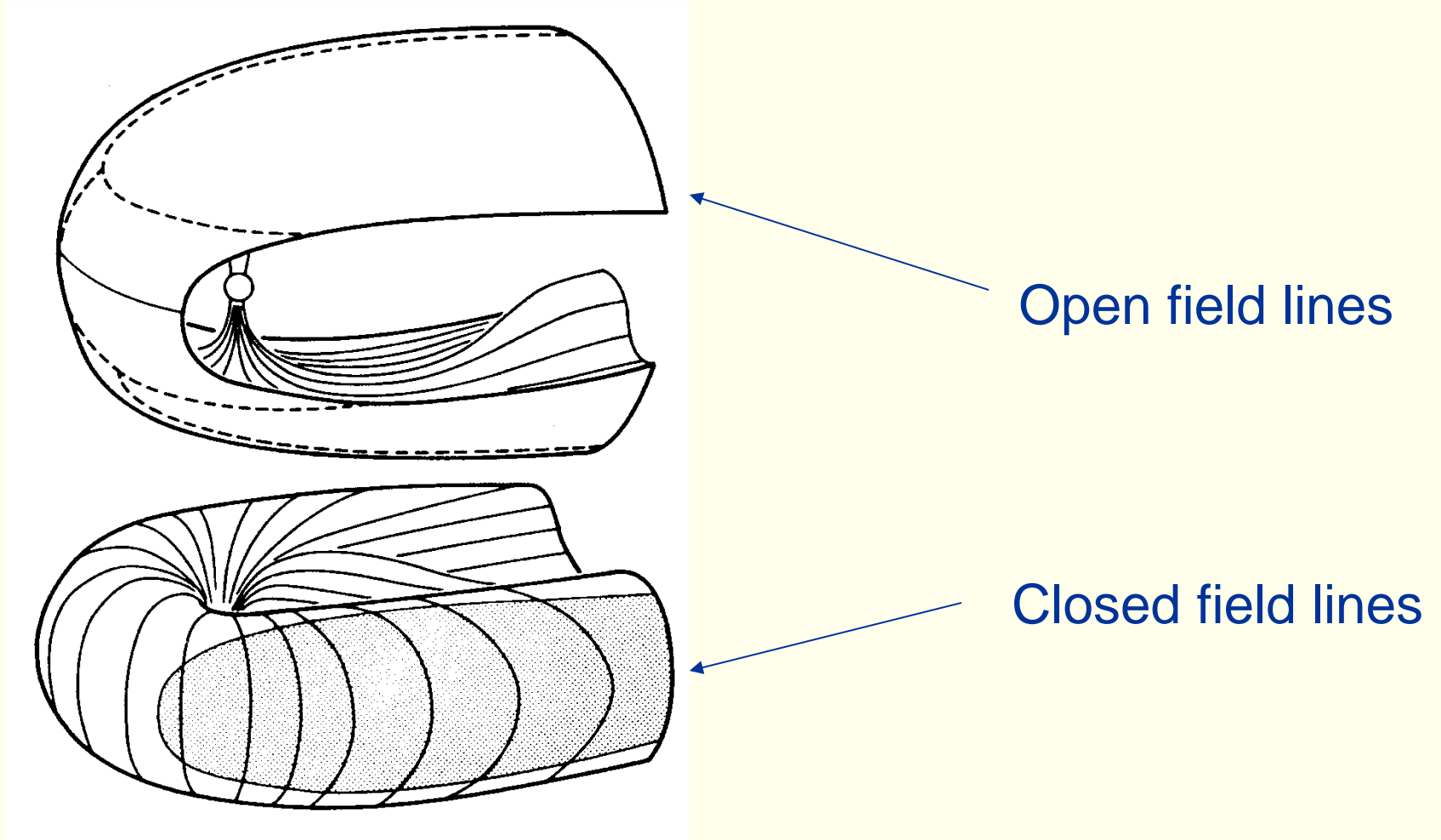
*open magnetosphere*



**Southward  
IMF**



# Magnetospheric topology



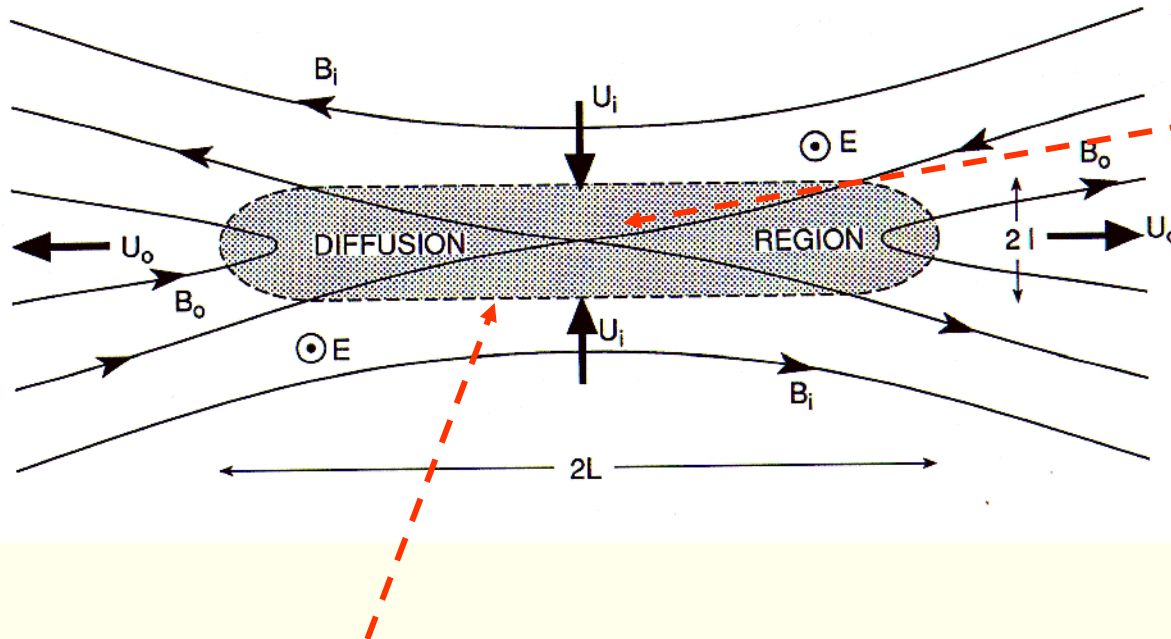
# Reconnection

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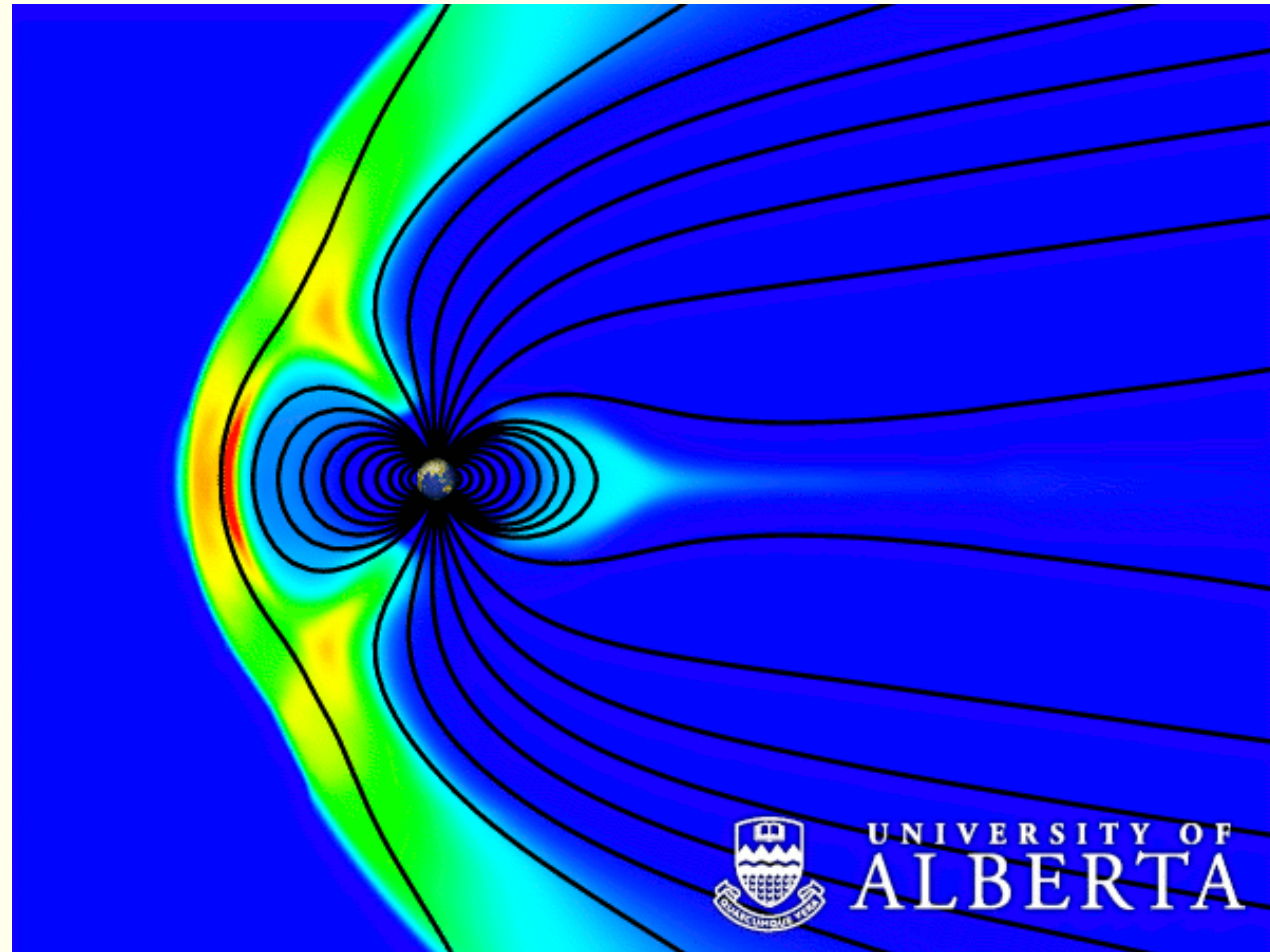


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# Reconnection and plasma convection

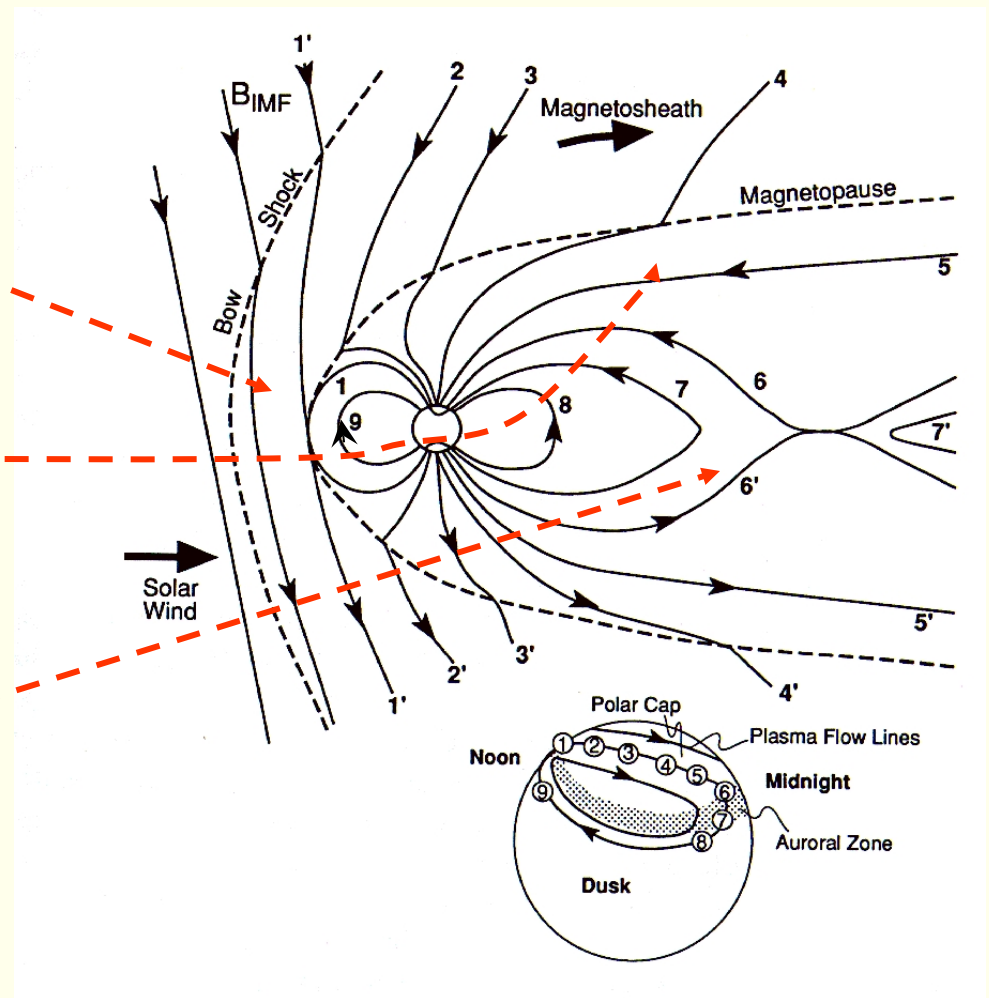


Solar wind



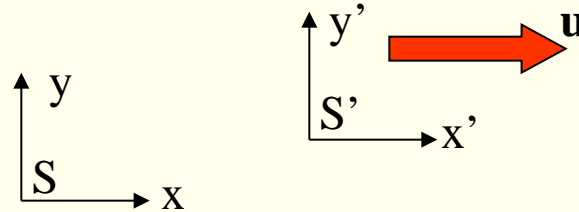
# Reconnection och plasma convection

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- In the night side a second reconnection region drives the convection in the inner magnetosphere. The reconnection also heats the plasmashet plasma.





# Field transformations (relativistic)



*Relativistic transformations  
(perpendicular to the velocity  $u$ ):*

$$\mathbf{E}' = \frac{\mathbf{E} + \mathbf{u} \times \mathbf{B}}{\sqrt{1 - u^2/c^2}}$$

$$\mathbf{B}' = \frac{\mathbf{B} - (\mathbf{u}/c^2) \times \mathbf{E}}{\sqrt{1 - u^2/c^2}}$$

*For  $u \ll c$ :*

$$\mathbf{E}' = \mathbf{E} + \mathbf{u} \times \mathbf{B}$$

induced  
electric field

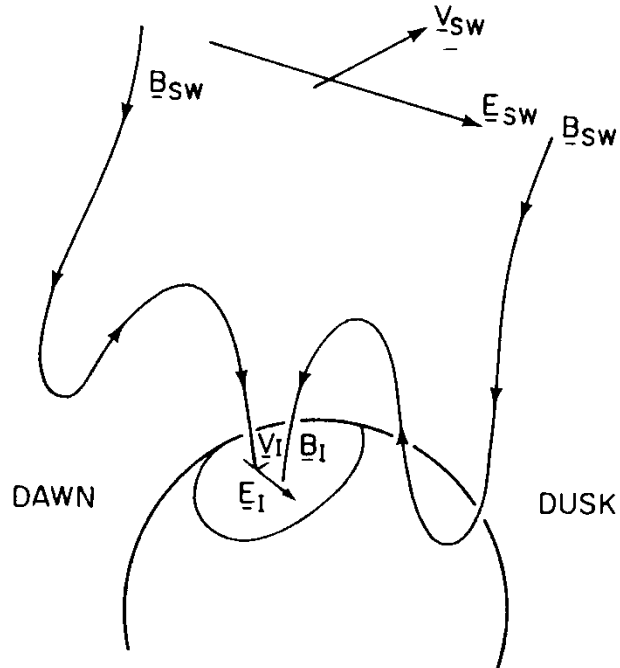
$$\mathbf{E} = \mathbf{E}' - \mathbf{u} \times \mathbf{B}$$

$$\mathbf{B}' = \mathbf{B}$$

# Magnetospheric dynamics

## *open magnetosphere*

### *Viewpoint 1*



The solar wind generates an electric field

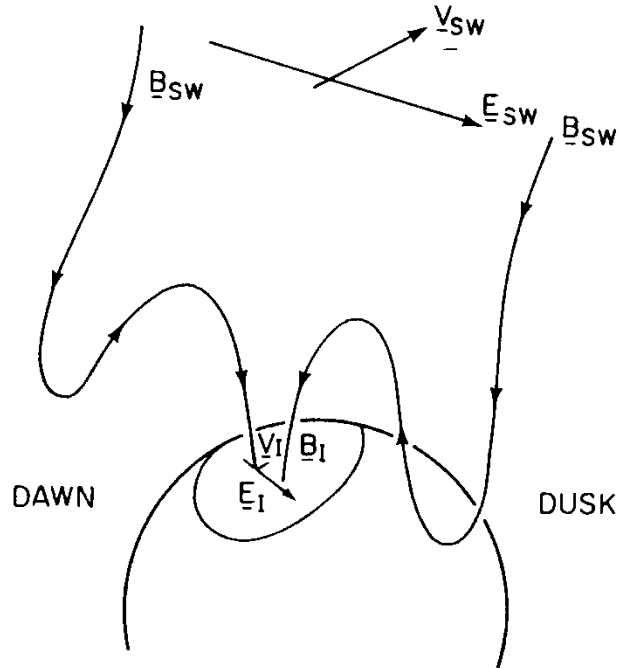
$$\mathbf{E}_{SW} = - \mathbf{v}_{SW} \times \mathbf{B}_{SW}$$

which maps down to the ionosphere, since the field lines are very good conductors

# Magnetospheric dynamics

## *open magnetosphere*

### *Viewpoint 2*



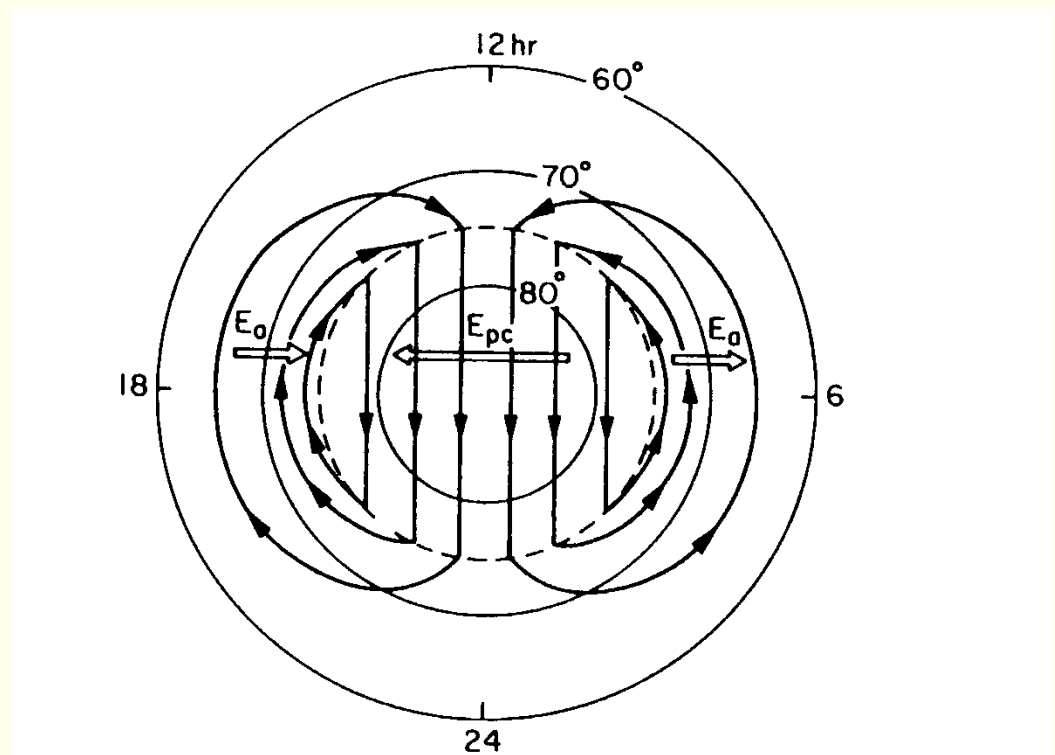
The solar wind magnetic field draws the ionospheric plasma with it, since the field is frozen into the plasma. This motion induces an ionospheric electric field

$$\mathbf{E}_I = - \mathbf{v}_I \times \mathbf{B}_I$$

# Magnetospheric dynamics

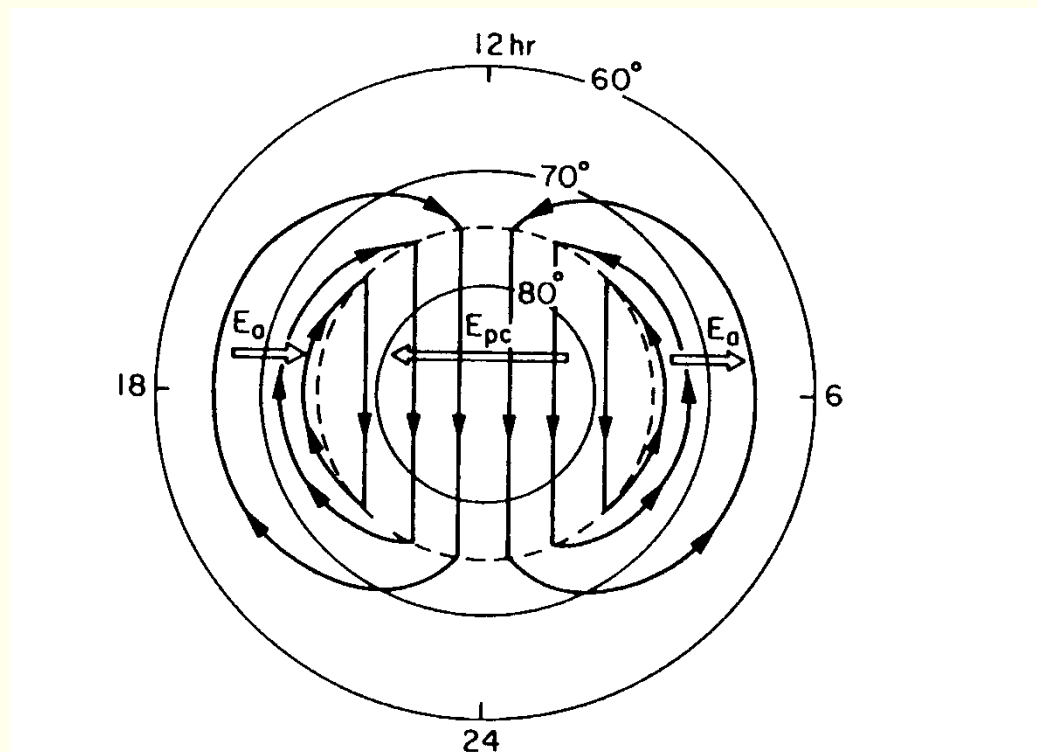
## *Plasma convection in the ionosphere*

The electric field "propagates" to the ionosphere, since the field lines are good conductors, and thus equipotentials



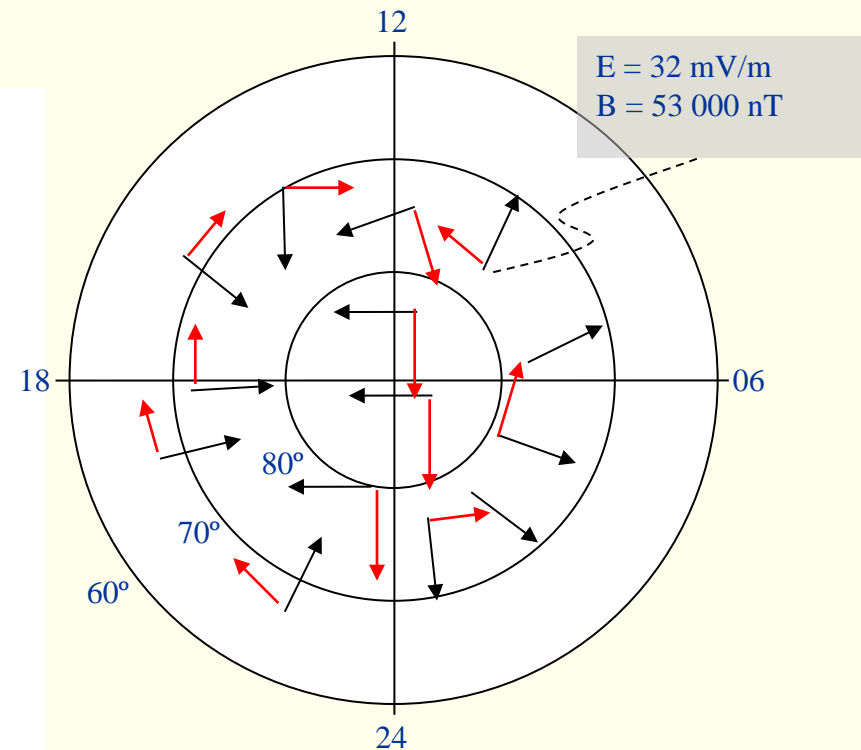
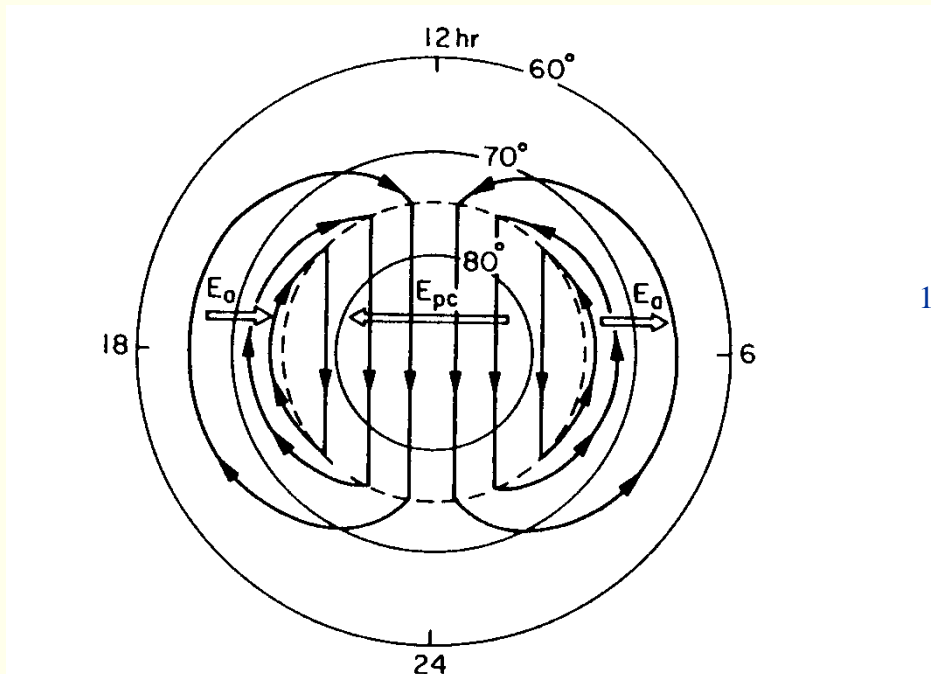
# Do you recognize this pattern?

*Plasma convection in the ionosphere*



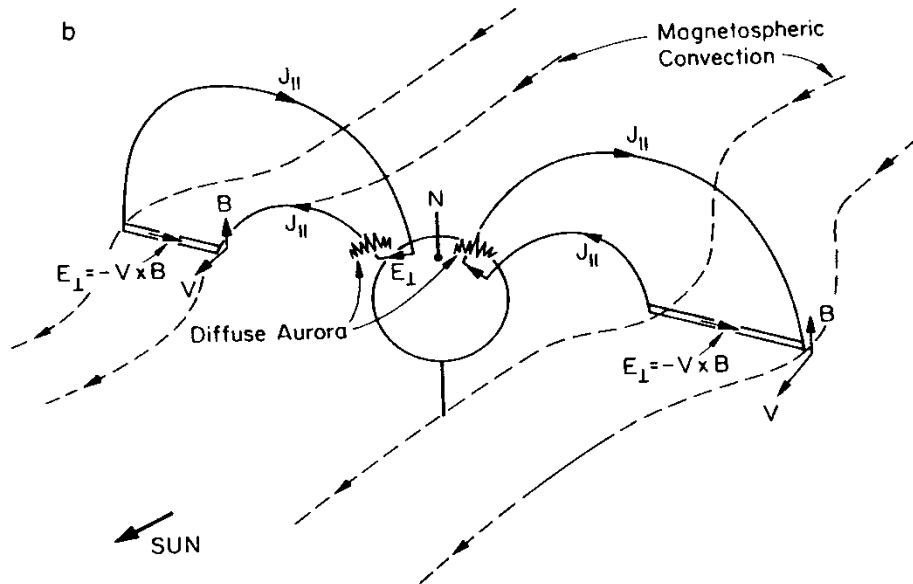
# Do you recognize this pattern?

## *Plasma convection in the ionosphere*



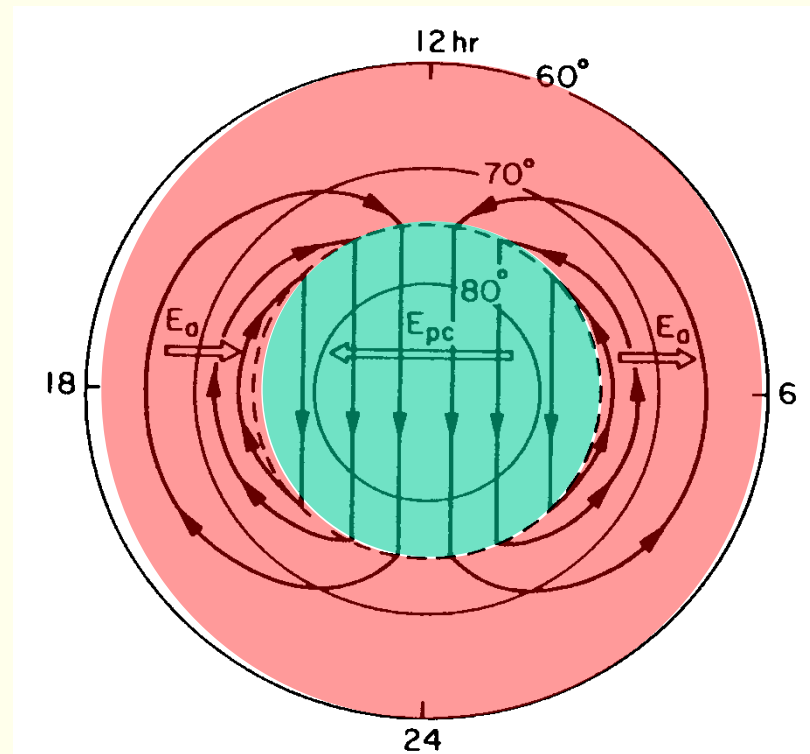
# Static, large-scale MI-coupling

## Magnetospheric and ionospheric convection



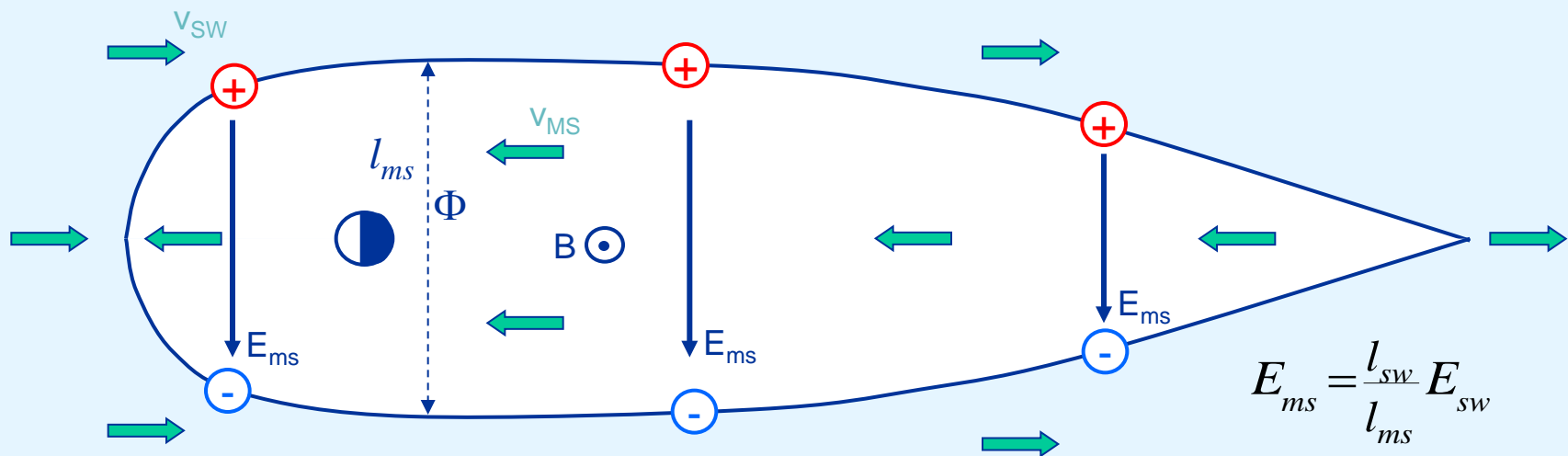
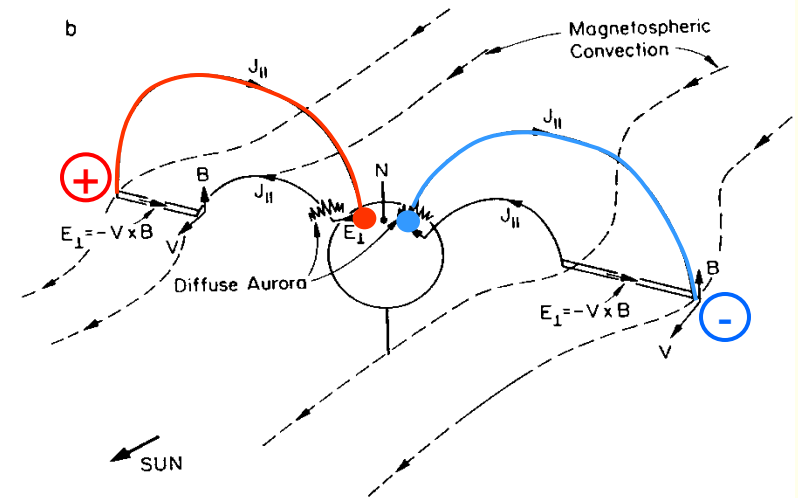
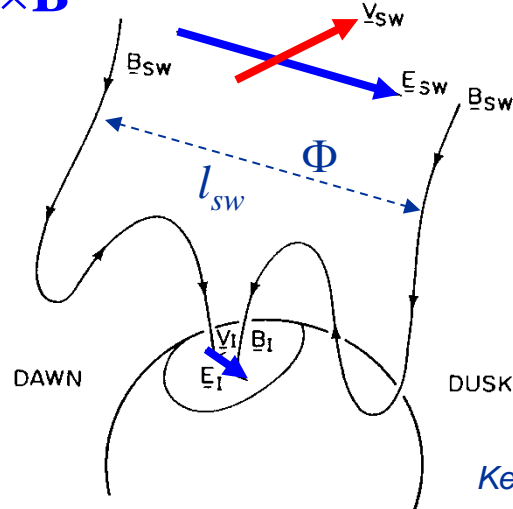
Kelley, 1989

### Ionospheric convection



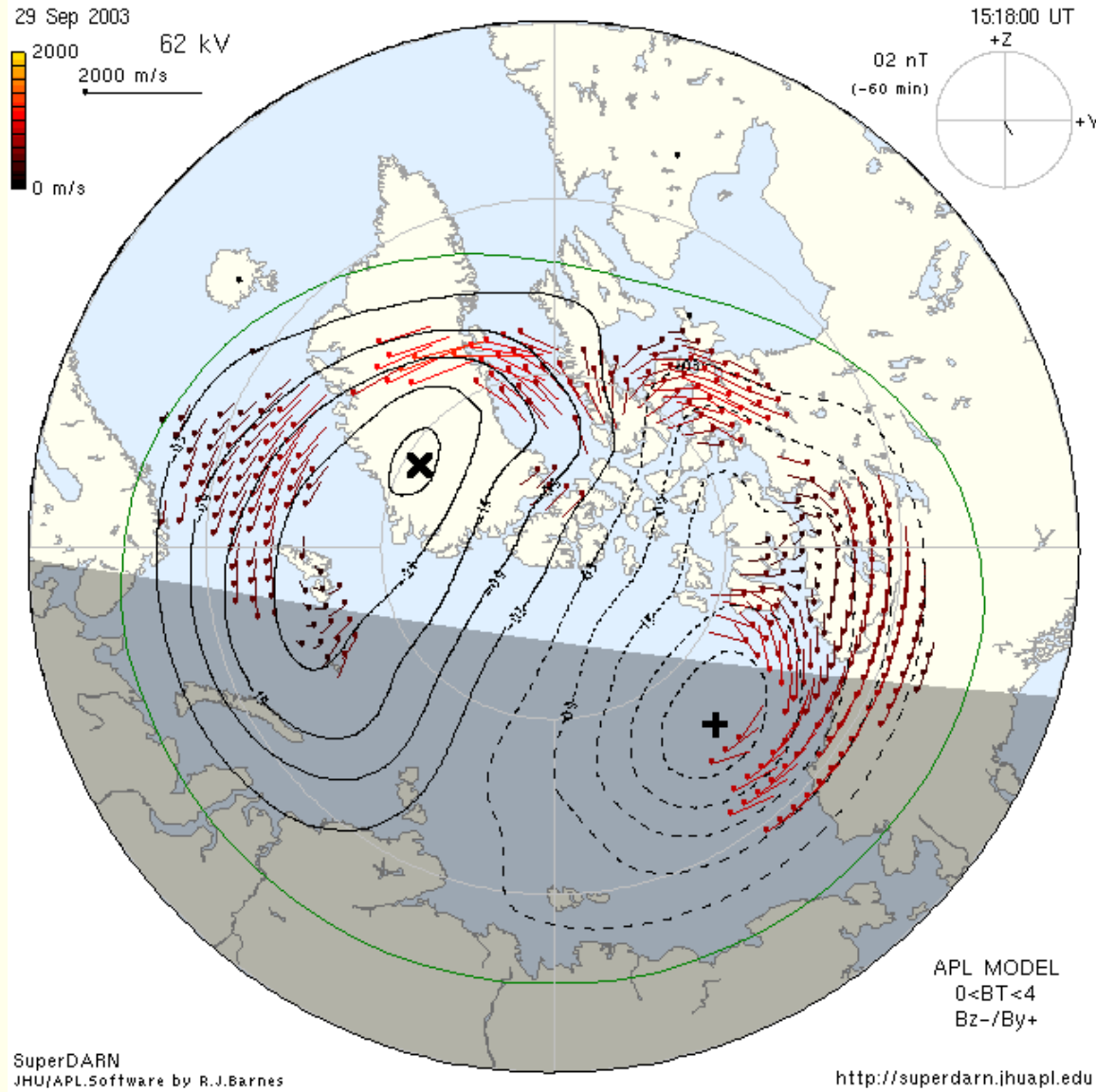
# Magnetospheric plasma convection

$$\mathbf{E}_{sw} = -\mathbf{v} \times \mathbf{B}$$





# Measurements of plasma convection in the magnetosphere





# ***Last Minute!***



# Last Minute!

- What was the most important thing of today's lecture? Why?
- What was the most unclear or difficult thing of today's lecture, and why?
- Other comments